

Contents

I. Classification of Nuclear, Simple C^* -algebras

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II. A Survey of Noncommutative Dynamical Entropy

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I. Classification of Nuclear, Simple C^* -algebras

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