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**Franz Baader and Ralf Küsters**

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<sup>†</sup> The endless cycle of death and rebirth to which life in the material world is bound. (OED)

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