

# Contents

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## Part I Theory

### Overview of Stochastic Optimization Algorithms

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## Applications A

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