

Contents

Fractional Integrals and Extensions of Selfdecomposability	1
Ken-iti Sato	
1 Introduction	2
1.1 Characterizations of Selfdecomposable Distributions	2
1.2 Nested Classes of Multiply Selfdecomposable Distributions	4
1.3 Continuous-Parameter Extension of Multiple Selfdecomposability	4
1.4 Stable Distributions and the Class L_∞	5
1.5 Fractional Integrals	6
1.6 The Classes $K_{p,\alpha}$ and $L_{p,\alpha}$ Generated by Stochastic Integral Mappings	8
1.7 Remarkable Subclasses of ID	10
2 Fractional Integrals and Monotonicity of Order $p > 0$	11
2.1 Basic Properties	11
2.2 One-to-One Property	15
2.3 More Properties and Examples	19
3 Preliminaries in Probability Theory	26
3.1 Lévy–Khintchine Representation of Infinitely Divisible Distributions	26
3.2 Radial and Spherical Decompositions of σ -Finite Measures on \mathbb{R}^d	27
3.3 Weak Mean of Infinitely Divisible Distributions	29
3.4 Stochastic Integral Mappings of Infinitely Divisible Distributions	31
3.5 Transformation of Lévy Measures	36
4 First Two-Parameter Extension $K_{p,\alpha}$ of the Class L of Selfdecomposable Distributions	37
4.1 Φ_f and Φ_f^L for $f = \varphi_\alpha$	37
4.2 $\bar{\Phi}_{p,\alpha}$ and $\bar{\Phi}_{p,\alpha}^L$	41
4.3 Range of $\bar{\Phi}_{p,\alpha}^L$	45
4.4 Classes $K_{p,\alpha}$, $K_{p,\alpha}^0$, and $K_{p,\alpha}^e$	47
5 One-Parameter Subfamilies of $\{K_{p,\alpha}\}$	57
5.1 $K_{p,\alpha}$, $K_{p,\alpha}^0$, and $K_{p,\alpha}^e$ for $p \in (0, \infty)$ with Fixed α	57
5.2 $K_{p,\alpha}$, $K_{p,\alpha}^0$, and $K_{p,\alpha}^e$ for $\alpha \in (-\infty, 2)$ with Fixed p	65

6	Second Two-Parameter Extension $L_{p,\alpha}$ of the Class L of Selfdecomposable Distributions	68
6.1	$\Lambda_{p,\alpha}$ and $\Lambda_{p,\alpha}^L$	68
6.2	Range of $\Lambda_{p,\alpha}^L$	73
6.3	Classes $L_{p,\alpha}$, $L_{p,\alpha}^0$, and $L_{p,\alpha}^e$	74
6.4	Relation Between $K_{p,\alpha}$ and $L_{p,\alpha}$	77
7	One-Parameter Subfamilies of $\{L_{p,\alpha}\}$	78
7.1	$L_{p,\alpha}$, $L_{p,\alpha}^0$, and $L_{p,\alpha}^e$ for $p \in (0, \infty)$ with fixed α	78
7.2	$L_{p,\alpha}$, $L_{p,\alpha}^0$, and $L_{p,\alpha}^e$ for $\alpha \in (-\infty, 2)$ with Fixed p	87
	References	89

Packing and Hausdorff Measures of Stable Trees

Thomas Duquesne

1	Introduction	93
2	Notation, Definitions and Preliminary Results	102
2.1	Hausdorff and Packing Measures on Metric Spaces	102
2.2	Height Processes and Lévy Trees	103
2.3	Estimates	113
3	Proofs of the Main Results	117
3.1	Proof of Theorem 1.1	117
3.2	Proof of Proposition 1.5	121
3.3	Proof of Proposition 1.9	122
3.4	Proof of Theorems 1.6 and 1.10	123
	References	135

Numerical Analysis of Additive, Lévy and Feller Processes

with Applications to Option Pricing

Oleg Reichmann and Christoph Schwab

1	Introduction	138
2	Markov Processes	140
2.1	Time-Homogeneous Processes	140
2.2	Time-Inhomogeneous Processes	144
3	Function Spaces	145
4	Multivariate Model Setting	148
4.1	Copula Functions	148
4.2	Sector Condition	151
4.3	A Class of Admissible Market Models	154
5	Variational PIDE Formulations	156
5.1	European Options	157
5.2	American Options	160
5.3	Greeks	164
6	Wavelets	168
6.1	Spline Wavelets on an Interval	169
6.2	Tensor Product Spaces	173
6.3	Space Discretization	174
6.4	Wavelet Compression	177

7	Computational Scheme	178
7.1	Time Discretization	178
7.2	Numerical Quadratures	179
8	Alternative Pricing Approaches	181
8.1	Monte Carlo Simulation	181
8.2	Fourier Pricing	183
9	Numerical Examples	185
9.1	Univariate Case	186
9.2	Multidimensional Case	190
	List of Symbols	192
	References	193
	Index	197

Lévy Matters I

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