

# Chapter 3

## Fracture Behavior of Concrete using Cohesive Crack and Size-Effect Models

### 3.1 Introduction

This chapter gives an idea of the nonlinear fracture behavior of concrete using cohesive crack and size-effect models. Initially, the formulation and development of cohesive crack model for three-point bending test and compact tension specimen are presented. Then a systematic study on the several cohesive crack fracture parameters for the TPBT and CT specimen with various softening functions is carried out. Toward the end, with reference to cohesive crack model, the size-effect study from size-effect law is investigated using three-point bending test. The contribution in this chapter is mainly based on work done by Kumar (2010) and Kumar and Barai (2008, 2009).

### 3.2 Cohesive Crack Model for Three-Point Bending Test

#### 3.2.1 Formulation Based on Energy Principle

Assuming that under condition of proportional and monotonic loading in mode I crack propagation, no unloading occurs in the fracture process zone and the process zone boundary can be defined by only one variable, i.e., the crack length  $a$ . The potential energy  $\Pi$  of a cracked body as shown in Fig. 3.1 is written as (Li and Liang 1994)

$$\Pi(u_i, P, a) = \int_V W(\varepsilon_{ij}) dV - \int_V F_i u_i dV - P \int_{A_T} b_i u_i dA + \int_{A_P} \phi(w) dA \quad (3.1)$$

where  $W$  is the strain energy density function defined in the body,  $\varepsilon_{ij}$  is the strain field,  $F_i$  is the body force,  $u_i$  is an admissible displacement field for the system,  $b_i$  is the boundary force distribution defined in the part of boundary  $A_T$ . The potential  $\phi$  can be defined for any given cohesive law  $\sigma = f(w)$  as

stress in the process zone. The basic feature of cohesive crack model is represented by Eq. (3.5). The equation states that the algebraic summation of stress intensity factors at the crack tip due to the external loading, constant body force, boundary force, if any and the cohesive stress distribution in the process zone is zero. This statement eliminates the stress singularity at the crack tip of the structure and a finite stress acts near the crack tip.

### 3.2.2 Basic Assumptions

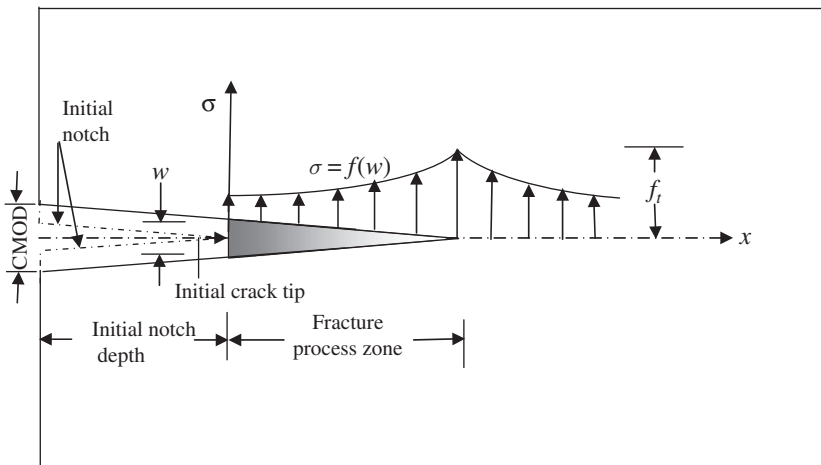
The following assumptions are considered in the development of cohesive crack model (Petersson 1981, Carpinteri 1989a–c, Carpinteri and Colombo 1989, Carpinteri et al. 2006):

1. The bulk of material behaves in a linear elastic and isotropic manner.
2. The cohesive process zone begins to develop when the maximum principal stress becomes equal to the tensile strength.
3. The material is in partially damaged condition and is still able to transfer the stress known as cohesive stress  $\sigma$  after formation of cohesive fracture zone. The cohesive stress depends on the crack opening displacement  $w$ . For mode I opening,  $\sigma$  acts normal to the crack faces as shown in Fig. 3.2 and is related to  $w$  as below:

$$\sigma = f(w) \quad (3.6)$$

Also from the definition of softening function of concrete

$$f_t = f(0) \quad (3.7)$$



**Fig. 3.2** Stress distribution and cohesive crack growth in mode I opening for concrete

- Nallathambi P, Karihaloo BL, Heaton BS (1984) Effect of specimen and crack size, water/cement ratio and coarse aggregate texture upon fracture toughness of concrete. *Magn Concr Res* 36 (129): 227–236.
- Nallathambi P, Karihaloo BL, Heaton BS (1985) Various size effects in fracture of concrete. *Cement Concr Res* 15: 117–126.
- Petersson PE (1981) Crack growth and development of fracture zone in plain concrete and similar materials. Report No. TVBM-100, Lund Institute of Technology.
- Planas J, Elices M (1990) Fracture criteria for concrete: Mathematical validations and experimental validation. *Eng Fract Mech* 35: 87–94.
- Planas J, Elices M (1991) Nonlinear fracture of cohesive material. *Int J Fract* 51: 139–157.
- Reinhardt HW, Cornelissen HAW, Hordijk DA (1986) Tensile tests and failure analysis of concrete. *J Struct Eng ASCE* 112 (11): 2462–2477.
- RILEM Draft Recommendations (TC89-FMT) (1990) Size-effect method for determining fracture energy and process zone size of concrete. *Mater Struct* 23 (138): 461–465.
- Roesler J, Paulino GH, Park K, Gaedicke C (2007) Concrete fracture prediction using bilinear softening. *Cement Concr Compos* 29: 300–312.
- Tada H, Paris PC, Irwin G (1985) *The Stress Analysis of Cracks Handbook*. Hellertown, PA, Del Research Corporation.
- Wittmann FH, Rokugo K, Bruhwiler E, Mihashi H, Simopnin P (1988) Fracture energy and strain softening of concrete as determined by compact tension specimens. *Mater Struct* 21 (1): 21–32.
- Xu S, Reinhardt HW (1999) Determination of double- $K$  criterion for crack propagation in quasi-brittle materials, Part II: Analytical evaluating and practical measuring methods for three-point bending notched beams. *Int J Fract* 98: 151–177.
- Xu S, Zhang X (2008) Determination of fracture parameters for crack propagation in concrete using an energy approach. *Eng Fract Mech* 75: 4292–4308.



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