

Contents

Part I Nonlinear Schrödinger Models: Continuum and Discrete

Solitons and Their Ghosts in \mathcal{PT}-Symmetric Systems with Defocusing Nonlinearities	3
V. Achilleos, P.G. Kevrekidis, D.J. Frantzeskakis, and R. Carretero-González	
1 Introduction	4
2 The Model and Some Analytical Insights	5
3 Ground State and Single Dark Soliton	8
3.1 Ground State	8
3.2 Single Dark Soliton	9
4 Multiple Dark Soliton States and Nonlinear \mathcal{PT} Phase Transitions	13
4.1 Two-Dark-Soliton State	13
4.2 Three-Dark-Soliton State	17
4.3 Nonlinear \mathcal{PT} Phase Transitions	19
4.4 The “Free Space” Case	21
5 Dark Soliton Dynamics	22
6 Ghost States and Their Dynamical Role	26
7 Symmetry Breaking and Nonlinear \mathcal{PT} Phase Transitions in Two Dimensions	30
8 Conclusions	40
References	41
Coding of Nonlinear States for NLS-Type Equations with Periodic Potential	43
G.L. Alfimov and A.I. Avramenko	
1 Introduction	43
2 Bounded and Singular Solutions of Stationary States	45
2.1 Some Definitions	45
2.2 Some Statements About Collapsing Points	46

3	Periodic Potential: Poincaré Map	48
3.1	Poincaré Map	48
3.2	Symbolic Dynamics: Theory	49
3.3	Symbolic Dynamics: Application	51
4	Steady States with Cosine Potential	52
4.1	Hypothesis 1	55
4.2	Hypothesis 2	56
4.3	Hypothesis 3	57
4.4	Examples	58
5	Conclusion	60
	References	60

Nonreciprocal Wave Propagation Through Open, Discrete

Nonlinear Schrödinger Dimers 63

Stefano Lepri and Giulio Casati

1	Introduction	63
2	The Model	65
3	Stability of Scattering Solutions	68
4	Scattering of Wave Packets	71
5	Summary and Conclusions	72
	References	74

Breather Solutions of the Discrete p -Schrödinger Equation 77

Guillaume James and Yuli Starosvetsky

1	Introduction and Main Results	78
2	Two-Dimensional Mappings Equivalent to the Stationary DpS Equation	81
2.1	Force Variables	82
2.2	Mixed Variables	83
3	Stable and Unstable Manifolds	84
3.1	Heuristics	85
3.2	Stable Manifold Theorem	85
3.3	Stable and Unstable Manifolds for the Maps M, T, F	87
4	Homoclinic Solutions of the Stationary DpS Equation	90
4.1	Homoclinic Solutions of Generalized DNLS Equations	90
4.2	Application to the DpS Equation	93
5	Analytical Approximations of Stable and Unstable Manifolds	96
5.1	Method of Local Approximation and Backward Iterates	97
5.2	Continuum Limit for Weak Nonlinearities	103
6	Breather Stability and Mobility	107
7	Discussion	112
	References	114

Part II Bose-Einstein Condensates (BECs) and Nonlinear Optics

Fragmentation of a Bose-Einstein Condensate Through Periodic Modulation of the Scattering Length	119
Antun Balaž and Alexandru I. Nicolin	
1 Introduction	119
2 Classification of Density Waves	121
3 Results and Discussion	123
4 Conclusions	127
References	128
Contact Intensity and Extended Hydrodynamics in the BCS-BEC Crossover	131
Luca Salasnich	
1 Contact Intensity	131
1.1 Uniform Superfluid Fermi Gas at Zero Temperature	133
1.2 Contact Intensity in the BCS-BEC Crossover	134
1.3 Trapped Superfluid Fermi Gas	135
2 Extended Superfluid Hydrodynamics	137
2.1 Extended Hydrodynamics in Terms of Goldstone Field	140
2.2 Application: The Unitary Fermi Gas	141
2.3 Nonlinear Sound Waves, Static Response Function and Structure Factor	142
3 Conclusions	145
References	145
<i>N</i>-Soliton Interactions for the Manakov System: Effects of External Potentials	147
V.S. Gerdjikov and M.D. Todorov	
1 Introduction	147
2 Preliminaries	150
2.1 Derivation of the CTC as a Model for the Soliton Interaction of VNLS Systems	150
3 Effects of the Polarization Vectors on the Soliton Interaction	153
4 Derivation of the PCTC as a Model for the Soliton Interactions	155
5 Comparison of the PCTC with the Perturbed Manakov Model	158
5.1 The Periodic Potentials	158
5.2 The Quadratic Potentials	159
5.3 The Quartic Potentials	161
6 Discussion	164
7 Conclusions	165
References	166
Wave Modes Trapped in Rotating Nonlinear Potentials	171
Yongyao Li, Wei Pang, and Boris A. Malomed	
1 Introduction	172
2 The Model	174
3 Numerical Results	176

3.1	The Classification of Trapped Modes.....	176
3.2	The Self-Focusing Nonlinearity.....	177
3.3	The Self-Defocusing Nonlinearity	181
3.4	The Alternating Self-Focusing: Self-Defocusing Nonlinear Potential	183
4	The Analytical Approach	184
4.1	The Two-Mode Approximation	184
4.2	The Self-Focusing Nonlinearity.....	184
4.3	The Self-Defocusing Nonlinearity	185
4.4	The Alternating Self-Focusing: Self-Defocusing Nonlinearity.....	187
5	Conclusions	188
	References	189

Light Propagation in Two Dimensional Plasmonic Arrays..... 193

Danhua Wang and Alejandro B. Aceves

1	Introduction	193
2	Theoretical Model and Dispersion Properties: Case 1	194
3	Theoretical Model and Dispersion Properties: Case 2	198
4	Modulation Instability	200
4.1	Numerical Simulations	203
5	Solitary Wave Solutions	204
6	Conclusion	207
	References	208

Part III Nonlinear Dynamical Lattices

**Localized Excitations and Anisotropic Directional Ordering
in a Two-Dimensional Morse Lattice Model of Cuprate Layers..... 213**

Manuel G. Velarde, Werner Ebeling, and Alexander P. Chetverikov

1	Introduction	213
2	Model Hamiltonian and Visualization of Local and Collective Atom (Lattice Units) Motions	216
3	Simulation of the Oxygen Dynamics	220
4	Discussion and Conclusions.....	220
	References	223

**Variational Approximation to Electron Trapping
by Soliton-Like Localized Excitations in One-Dimensional
Anharmonic Lattices..... 225**

Luis A. Cisneros-Ake, Antonmaria A. Minzoni,
and Manuel G. Velarde

1	Introduction	225
2	Formulation of the Problem and Numerical Results	227
3	Traveling Polaron/Solectron Solutions.....	232
4	Conclusions	234
	References	235

Stability of Mode-Locked Kinks in the AC Driven and Damped Sine-Gordon Lattice	237
Yaroslav Zolotaryuk	
1 Introduction	237
2 The Model and Equations of Motion	238
2.1 The DSG Equation.....	238
2.2 Linear Stability and the Floquet Theory	239
3 Kinks in the High-Frequency Driven DSG Equation	240
3.1 The Numerical Scheme.....	241
3.2 The Existence Diagram.....	241
3.3 Floquet Spectrum and the Destabilizing Bifurcations	244
4 Discussion and Conclusions.....	249
References	250

Spatio-Temporal Dynamics in a Ring of Coupled Pendula: Analogy with Bubbles	251
V.J. Sánchez-Morcillo, N. Jiménez, J. Chaline, A. Bouakaz, and S. Dos Santos	
1 Introduction	252
2 The Ring of Coupled Pendula	253
2.1 The Model.....	253
2.2 Experimental Setup	254
3 Localized Excitations	256
3.1 Lower Cutoff Modes	256
3.2 Upper Cutoff Modes	258
4 Defect-Induced Localization	259
5 Analogy with Gas Bubbles in an Ultrasound Field.....	260
6 Conclusions	261
References	262

Part IV Quodons and Muscovite Mica

Theory of a Quodon Gas with Application to Precipitation Kinetics in Solids Under Irradiation	265
V. Dubinko and R. Shapovalov	
1 Introduction	265
2 Gas of Quodons and Its Effect on Reaction Rates in Solids	267
2.1 Gas of Quodons	268
2.2 Modification of Reaction Rates in Solids Under Irradiation.....	270
3 Modeling of the Precipitation Kinetics Under Irradiation in the Modified Rate Theory	274
3.1 Classical Rate Theory of the Precipitation Kinetics	275
3.2 Quodon-Induced Solubility Limit Change	279
3.3 Quodon-Induced Interfacial Energy Change	282
3.4 Diffusivity of Cu Under Irradiation	283

3.5	Evolution of Cu Precipitates and the Matrix Concentration of Cu Under Electron Irradiation	285
4	Summary	287
	References	288
	Energy Gain by Discrete Particle Non-linear Lattice Excitations	289
	F.M. Russell	
1	Introduction	290
2	Experimental Methods	292
3	Layered Structure Effects	294
4	Molecular Dynamics Simulations of Cascades	296
5	Numerical Modelling in 2D Arrays	298
6	Structure of Non-linear Intrinsic Localised Modes	301
7	Energy Gain by Kink Pulses	304
8	Creation of Coordinated Kink Pulses	306
9	Evidence for Multiple Kink Pulses from Nuclear Scattering	307
10	Defect Sweeping	310
11	Inner Structure of Fans	310
12	Discussion	311
13	Conclusion	313
	References	314
	Supersonic Kinks in Coulomb Lattices	317
	Juan F.R. Archilla, Yuriy A. Kosevich, Noé Jiménez, V́ctor J. Sánchez-Morcillo, and Lús M. Garća-Raffi	
1	Introduction	318
2	Model Equations	319
3	Phonons	321
4	Localized Travelling Solutions	323
	4.1 Tail Analysis	323
	4.2 Oscillating Tails	324
	4.3 Supersonic Solitons and Kinks	325
5	Kink Characteristics Within the Rotating Wave Approximation: Magic Wave Number	326
6	Numerical Results	328
7	Effect of the Interaction with Several Neighbors	330
8	Conclusions	330
	References	331
	Part V Magnetic Metamaterials	
	Travelling Waves in Nonlinear Magnetic Metamaterials	335
	J. Diblík, M. Fečkan, M. Pospíšil, V.M. Rothos, and H. Susanto	
1	Introduction	336
2	Existence Results on Periodic Solutions	337
3	Bifurcation Results for Periodic Travelling Waves	343

4	Bifurcation Results for Asymptotic Travelling Waves	348
5	Numerical Results	354
	References	357

Stability of Discrete Breathers in Magnetic Metamaterials 359

Dmitry Pelinovsky and Vassilis Rothos

1	Introduction	359
2	Formalism	360
3	Existence of Multi-site Discrete Breathers	362
4	Stability of Multi-site Breathers	365
4.1	Adjacent Excited Oscillators	366
4.2	Oscillators at Rest Between Excited Oscillators	369
5	Discussion	372
	References	374

Part VI Other Nonlinear Models

Checking the Validity of Truncating the Cumulant Hierarchy

Description of a Small System 377

Manuel Morillo, José Gómez-Ordóñez, and José M. Casado

1	Introduction	377
2	The Model	379
3	Numerical Simulations	380
4	Conclusion	386
	References	387

Shape-Invariant Solitons in Nematic Liquid Crystals:

The Influence of Noise 389

Milivoj R. Belić, Milan S. Petrović, Aleksandra I. Strinić,
and Najdan B. Aleksić

1	Introduction	389
1.1	Fundamental Solitons	389
1.2	Nonlocality	390
1.3	Status of the Field	390
1.4	Contents of the Chapter	391
2	The Model	391
2.1	Scalar Nonlocal Model of Nematic Liquid Crystals	391
2.2	Model Equations	392
3	Computations	393
3.1	Numerical Procedure	393
3.2	Modified Petviashvili Procedure	394
3.3	The Stability of Fundamental Solitons	395
4	The Influence of Noise	397
4.1	The Breathing Problem	397
4.2	Propagation in the Presence of Noise	397
4.3	Destructive Influence of Noise	399

5	Conclusion	400
	References	400
Conservation Laws of a Family of Reaction-Diffusion-Convection Equations		403
M.S. Bruzón, M.L. Gandarias, and R. de la Rosa		
1	Introduction	403
2	Formal Lagrangian and Adjoint Equation	405
3	Lie Symmetries	406
4	Nonlinear Self-Adjoint Equations.....	409
5	Conservation Laws for a Subclass of Nonlinear Self-Adjoint Equations	411
6	Conclusions	416
	References	417
Effects Induced in Complex Biological Systems by High Density Green Photons		419
Sorin Comorosan, Silviu Polosan, Marian Apostol, Irinel Popescu, Ileana Farcasanu, Liliana Paslaru, and Elena Ionescu		
1	Introduction	420
2	Experimental Evidence	421
	2.1 Mass Spectroscopy	422
	2.2 Enzyme Reactions	424
3	Discussion and Conclusion: A Physical Model	426
	References	427
	Index	429

Localized Excitations in Nonlinear Complex Systems

Current State of the Art and Future Perspectives

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