

# A Closed Loop Supply Chain Inventory Model for the Deteriorating Items with JIT Implementation

S. R. Singh and Neha Saxena

**Abstract** In the past recent years, a growing environmental consciousness has been shaping the way society looks on green. Society's attitude towards environmental issues has been changing and hence recoverable product environments are becoming an increasingly important segment of the overall push in industry. We have proposed a model for the design of a closed loop supply chain with green components. We have investigated a joint economic production quantity model for a single vendor, single buyer system considering lot-splitting. The effect of deterioration is taken into consideration. Here we have assumed that the vendor fulfils the buyer's demand with the produced and remanufactured units, where the remanufactured items are considered as good as those of new items. Mathematical and numerical analysis are presented to describe the situation.

**Keywords** Inventory model • Production • Remanufacturing • Deterioration • JIT implementation

## 1 Introduction

Owing to increased public concern about the environment, most developed countries have made legislations, mandating manufacturers and importers to take back used products at the end of their useful lives. Consumers can now return goods within warranty period as part of the after-sales service if the products fail to meet their needs or when the products have reached the end of their useful lives.

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S. R. Singh (✉) • N. Saxena  
Department of Mathematics, D. N. College, Meerut, India  
e-mail: shivrajpundir@gmail.com

N. Saxena  
e-mail: nancineha.saxena@gmail.com

The returned products may then be refurbished or remanufactured to extend their periods of usage or recycled to recapture value. For sustainable development, a good supply chain strategy enables manufacturing plant to rescue and recover many parts and components from used products through reverse logistics activities of remanufacturing and reuse. It considers impacts of environmental protection and green image. Closed-loop supply chains comprising forward and reverse logistics can be combined to achieve more sustainable production and consumption.

There have been numerous studies and research on reverse logistics. The initial approach in the field of reverse logistics is made by Schrady [18]. He analyzed a traditional Economic Order Quantity (EOQ) model for repairable items with the joint coordination of reverse manufacturing with the forward supply chain by assuming that the manufacturing and recovery (repair) rates are instantaneous. His work was generalized by Nahmias and Rivera [12] with finite repair rates. This model is further extended by Koh et al. (2002) for limited repair capacity. Richter [13–15], and Richter and Dobos [16] have investigated the reverse logistics model. In these problems the return rate has been taken as a decision variable. Authors have examined problem with pure or bang-bang policy (total repair or total wastage disposal). Richter [15] concluded in his paper that the bang-bang policy is optimal when compared to mixed (production + remanufacturing) policy, while in later study (El Saadany and Jaber [5]) it was observed that mixed strategy is optimal, rather than a pure strategy; either pure remanufacturing or pure production. The model developed by Ishii et al. [6] confirms that life-cycle design seeks to maximize the life-cycle value of a product at the initial stages of design. Savaskan et al. [17] developed a RL model by assuming the returned rate dependent to the Collection investment. In this model they investigated a closed-loop supply chain that includes reverse logistics in times of product recovery of the retailer. Dekker et al. [4] proposed a quantitative model for closed loop supply chain. He analyzed that the amount of returns is highly uncertain and this uncertainty greatly affect the collection and inventory decisions. El Saadany and Jaber [5] developed a model assuming that the collection rate of returned items is dependent on the purchasing price and the acceptance quality level of these returns. Konstantaras and Skouri [8] developed a model of supply chain by considering a general cycle pattern in which a variable number of reproduction lots of equal size are followed by a variable number of manufacturing lots of equal size. They also have studied the case where shortages are allowed in each manufacturing and reproduction cycle. Alamri [1] investigate the optimal returned quantity for a general Reverse Logistics inventory model for the deteriorated items. Green supply chain inventory model with short life cycle product is developed by Chung and Wee [3]. Singh and Saxena [20] investigated a reverse logistics inventory model with time dependent rates under shortages considering the returned rate and holding capacity as a decision variable. Along the same line as Singh and Saxena [20], Singh et al. [19] developed there model for the flexible manufacturing under the stock out situation.

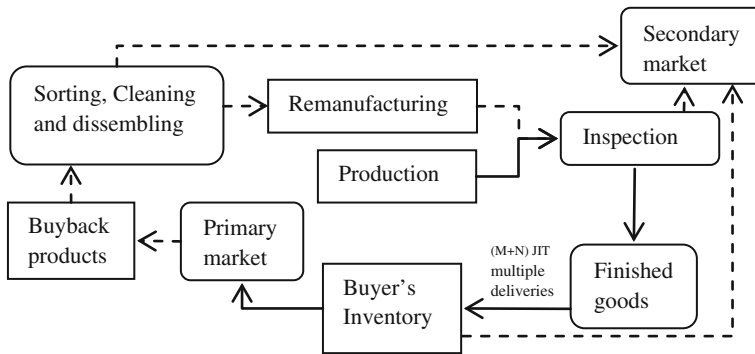
With growing focus on supply chain management firms realize that inventories across the entire supply chain can be more sufficiently managed through great cooperation and better coordination in just in time production system, multiple deliveries is the one way to reduce the inventory level and the total cost. The main goal of this study is to analyse under what conditions (capacity, return rate, remanufacturing rate) a reverse-logistics system should be introduced at a company that uses a JIT production-management system. Numerous researches have been done on the integrated inventory models implementing JIT. Lu [11] proposed a lot splitting model implementing JIT deliveries assuming equal sized multiple shipments. A joint economic lot size model for a single vendor single buyer system has been developed by Benerji [2]. Kim and Ha [9] have developed a lot splitting model and discussed how and when the optimal policy for buyer and supplier can be achieved. Chang and Wee [3] have investigated a green supply chain model implementing JIT delivery.

In this paper we determined the coordination of reverse manufacturing with the forward supply chain in the inventory management. Reverse logistics operations deals with the collection of returns, cleaning of the collected returns and remanufacturing of the reusable collected items, while in the forward supply chain we have taken the single setup and multiple JIT deliveries (SSMD) strategy. The vendor fulfilled buyer's demand with newly produced and remanufactured items of quality standard "as good as those of new products". The produced/remanufactured items are passing through the process of inspection. After inspection the innocent products are delivered to the buyer in  $M + N$  deliveries and the rest (deteriorated items or unacceptable for the primary market) are shipped to a secondary market in as-in condition. A general framework of such a system is shown in Fig. 1. In the next Sect. 2, assumptions and notation are provided for model development. In Sect. 3, the study develops an integrated buyer-vendor model with single setup and multiple deliveries. The model considers JIT deliveries, reverse-manufacturing costs and other costs, and derives the optimal replenishment. A numerical example is presented in Sect. 4. Concluding remarks are shown in Sect. 5.

## 2 Notations and Assumptions

### 2.1 Notations

$C_{if}$	Fixed inspection cost
$C_{iv}$	Variable inspection cost per setup
$C_{ins}$	The unit variable inspection cost
$L_{fs}$	The cost of less flexibility
$H_B$	Unit holding cost for the buyer
$T_B$	Delivery cycle time for the buyer



**Fig. 1** Material flow in the green supply chain

$q$	Delivery size per delivery
$A$	Ordering cost per cycle
$P_m$	The production rate
$D$	The demand rate
$\theta$	Deterioration rate
$M$	Number of deliveries delivered by the producer
$U_m$	Unit item cost
$K_m$	Fixed unit production cost
$C_m$	Variable unit production cost
$H_m$	Unit holding cost for the produced material
$C_s$	Selling price for the secondary market
$S_s$	Selling price for the primary market
$P_r$	Remanufacturing rate
$R$	Returned rate
$N$	The number of deliveries delivered by the remanufacturer
$\eta$	Scaling parameter, returned formulation
$K_r$	Fixed unit reproduction cost
$C_r$	Variable unit reproduction cost
$H_r$	Unit holding cost for the remanufactured items
$\gamma$	The scaling parameter, returned rate formulation
$U_R$	Unit returned item cost
$H_R$	Unit holding cost for the returned items
$CI$	Collection investment
$F_{cl}$	Fixed cost including cleaning and disassembly cost during the collecting process
$C_{cl}$	Variable cost including cleaning and disassembly cost during the collecting process

## 2.2 Assumptions

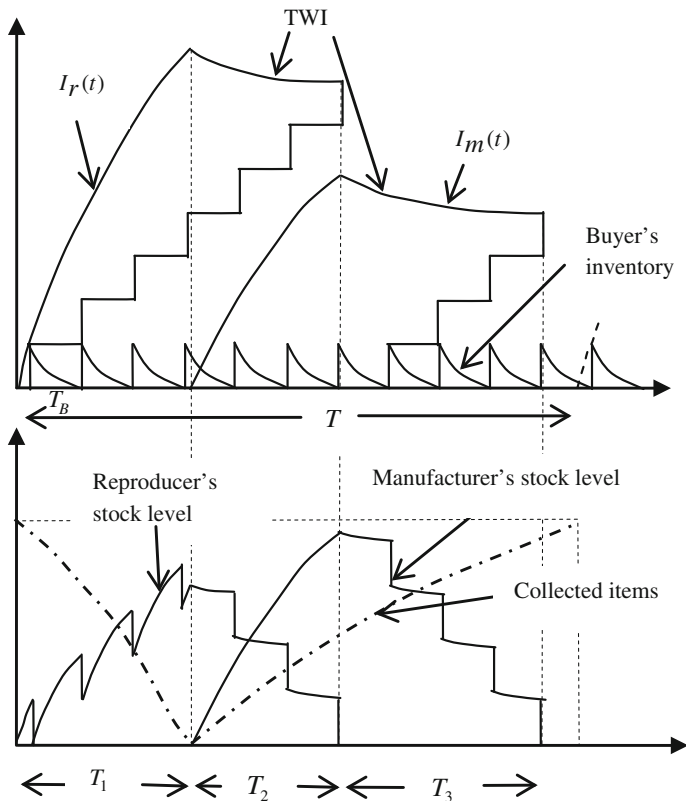
- Vendor fulfilled buyer's demand by the newly produced and remanufactured items.
- The buyback products are subject to the cleaning and disassembling process, where the products that confirm to certain quality standard (At a rate of  $\left(\frac{1}{\eta}\right)R$ ) is delivered to remanufacturing unit and the rest  $\left\{1 - \left(\frac{1}{\eta}\right)R\right\}$  are shipped for the secondary market in as-in condition.
- Items deteriorate while they are in storage, and production, remanufacturing and demand.
- After the production/remanufacturing products though the inspection process and the deteriorated items are shipped to the secondary market.
- The returned rate  $R$  is determined by the collection investment CI. The collection investment represents the monetary amount of effort (e.g., promotion, marketing) that the recycled-material vendor applies to the end-user market to create the necessary incentive to receive targeted returns. We model the return rate similar to the work by Savaskan et al. [17] in which,  $R = \left(\sqrt{\frac{CI}{\gamma}}\right)$ , where  $\gamma$  is a scaling parameter and  $\left(\sqrt{\frac{CI}{\gamma}}\right) < D$
- We shall require that

$$P_r > D, P_m > D, P_r > R, D \neq 0, R \neq 0$$

## 3 Mathematical Modelling and Analysis

The items are ordered by buyer in  $M + N$  shipments (equal lots of size  $q$ ). The model assumes that the successive delivering batch arrives at the store as soon as the previous batch has been depleted. For each cycle, the system starts operating at time zero by which the reproduction process starts and the inventory level increases until time  $T_1$ , where the stock-level reaches its maximum, and the reproduction process stopped. At the same instant of time production starts and the stock level of remanufactured items decreases continuously due to the demand and deterioration, while production is in process by the time  $T_2$  where it reaches its maximum and the production process stopped. Then the inventory level decrease continuously by the time  $T_3$ . The inventory level in returned process decreases until time  $T_1$  where the inventory level becomes zero. After that the inventory level increases until the time  $T_1 + T_2 + T_3$  where, the inventory level reaches its maximum. The process is repeated (Fig. 2).

The changes in the inventory levels depicted in Fig. 2 are governed by the following differential equations:



**Fig. 2** Inventory variation of an inventory model for reverse logistics systems

$$I'_B(t) = -d - \theta I_B(t), \quad 0 \leq t \leq T_B \quad I_B(T_B) = 0 \quad (1)$$

$$I'_{r1}(t_{r1}) = P_r - \theta I_{r1}(t_{r1}), \quad 0 \leq t_{r1} \leq T_1 \quad I_{r1}(0) = 0 \quad (2)$$

$$I'_{r2}(t_{r2}) = -\theta I_{r2}(t_{r2}), \quad 0 \leq t_{r2} \leq T_2 \quad I_{r2}(T_2) = Nq \quad (3)$$

$$I'_{m1}(t_{m1}) = P_m - \theta I_{m1}(t_{m1}), \quad 0 \leq t_{m1} \leq T_2 \quad I_{m1}(0) = 0 \quad (4)$$

$$I'_{m2}(t_{m2}) = -\theta I_{m2}(t_{m2}), \quad 0 \leq t_{m2} \leq T_3 \quad I_{m2}(T_3) = Mq \quad (5)$$

$$I'_R(t_R) = \frac{1}{\eta} R - P_r, \quad 0 \leq t_R \leq T_1 \quad I_R(T_1) = 0 \quad (6)$$

$$I'_R(t_R) = \frac{1}{\eta} R \quad T_1 \leq t_R \leq (N + M)T_B \quad I_R(T_1) = 0 \quad (7)$$

The solutions of the above differential equations are

$$I_B(t) = \left\{ \frac{d}{\theta} \right\} (e^{\theta(T_B-t)} - 1) \quad 0 \leq t \leq T_B \quad (8)$$

$$I_{r1}(t_{r1}) = \left\{ \frac{P_r}{\theta} \right\} (1 - e^{-\theta t_{r1}}) \quad 0 \leq t_{r1} \leq T_1 \quad (9)$$

$$I_{r2}(t_{r2}) = qNe^{\theta(T_2 - t_{r2})} \quad 0 \leq t_{r2} \leq T_2 \quad (10)$$

$$I_{m1}(t_{m1}) = \left\{ \frac{P_m}{\theta} \right\} (1 - e^{-\theta t_{m1}}) \quad 0 \leq t_{m1} \leq T_2 \quad (11)$$

$$I_{m2}(t_{m2}) = qMe^{\theta(T_3 - t_{m2})} \quad 0 \leq t_{m2} \leq T_3 \quad (12)$$

$$I_R(t_R) = \left( P_r - \frac{1}{\eta} R \right) (T_1 - t_R), \quad 0 \leq t_R \leq T_1 \quad (13)$$

$$I_R(t_R) = \left\{ \frac{R}{\eta} \right\} (t_R - T_1), \quad T_1 \leq t_R \leq (N + M)T_B \quad (14)$$

Respectively

Using the boundary conditions  $I_B(0) = q$  so that from Eq. (1), when  $\theta \ll 1$  the delivery size is

$$q = dT_B \left( 1 + \frac{\theta T_B}{2} \right) \quad (15)$$

As depicted in Fig. 2 we have

$$T_3 = MT_B \quad (16)$$

and

$$T_1 + T_2 = (N - 1)T_B + \frac{q}{P_r} \quad (17)$$

By which, we get

$$T_1 + T_2 + T_3 = (M + N - 1)T_B + \frac{q}{P_r} \quad (18)$$

Assuming the cycle time  $T$  so we have

$$T = (M + N)T_B \quad (19)$$

Using the boundary conditions, from Eqs. (13) and (14) we get

$$\left( P_r - \frac{1}{\eta} R \right) T_1 = \frac{1}{\eta} R ((M + N)T_B - T_1)$$

By which the remanufacturing period is

$$T_1 = \frac{R(M + N)T_B}{\eta P_r} \quad (20)$$

From Eq. (17) the production period

$$T_2 = (N - 1)T_B + \frac{q}{P_r} - \frac{R(M + N)T_B}{\eta P_r} = \left( (N - 1) - \frac{R(M + N)}{\eta P_r} \right) T_B + \frac{q}{P_r} \quad (21)$$

Now the per cycle cost components for the given inventory system are as follows.

Sales Revenue from the secondary market

$$= c_s \left[ (q - dT_B) + \{P_r T_1 + P_m T_2 - q(N + M)\} + \left\{ (M + N) \left( 1 - \frac{1}{\eta} \right) \sqrt{\frac{CI}{\gamma}} \right\} T_B \right]$$

Sales Revenue from the primary market

$$= S_s d(M + N)T_B$$

Buyer's ordering cost and holding cost is as follows

$$= A + (M + N)H_B \int_0^{T_B} I_B(u) du$$

$$\text{Production and remanufacturing cost} = K_m + K_r + C_m \int_0^{T_2} P_m du + C_r \int_0^{T_1} P_r du = K_r + K_m + C_r T_1 P_r + C_m P_m T_2$$

Procurement and acquisition cost

$$= U_m \int_0^{T_2} P_m du + U_R \int_0^{(M+N)T_B} R du = U_m P_m T_2 + U_R (M + N) \sqrt{\frac{CI}{\gamma}} T_B$$

$$\text{Inspection cost} = \frac{C_{if}}{M+N} + (M + N)C_{iv} + C_{ins}(P_r T_1 + P_m T_2)$$

The Vendor's cost of less flexibility of implementing JIT delivery is  $= (M + N)L_{fs}$

As depicted in Fig. 2 the inventory holding cost is

$$\begin{aligned} &= H_m \left[ \int_0^{T_2} \left\{ \frac{P_m}{\theta} \right\} (1 - e^{-\theta u}) du + \int_0^{T_3} q M e^{\theta(T_3 - u)} du - T_B(q + 2q \dots + (M - 1)q) \right] \\ &+ H_r \left[ \int_0^{T_1} \left\{ \frac{P_r}{\theta} \right\} (1 - e^{-\theta u}) du + \int_0^{T_2} q N e^{\theta(T_2 - u)} du - T_B(q + 2q \dots + (N - 1)q) \right] \\ &+ H_R \left[ \int_0^{T_1} \left\{ P_r - \frac{1}{\eta} \sqrt{\frac{CI}{\gamma}} \right\} (T_1 - u) du + \int_{T_1}^{(M+N)T_B} \frac{1}{\eta} \sqrt{\frac{CI}{\gamma}} (u - T_1) du \right] \\ &+ H_B \int_0^{T_B} \left\{ \frac{d}{\theta} \right\} (e^{\theta(T_B - t)} - 1) du \end{aligned}$$

$$\text{Cleaning cost} = F_{cl} + C_{cl} \sqrt{\frac{CI}{\gamma}} T_B (M + N)$$

Total profit is calculated here,



$$\begin{aligned}
TP = \frac{1}{T} & \left\{ S_s D(M+N)T_B + c_s \left[ (q - DT_B) + \{P_r T_1 + P_m T_2 - q(N+M)\} + (M+N) \left(1 - \frac{1}{\eta}\right) \sqrt{\frac{CI}{\gamma}} \right] T_B \right. \\
& - (M+N)H_B \left[ \frac{DT_B^2}{2} \left(1 + \frac{\theta T_B}{3}\right) \right] \\
& - A - (U_m + C_m)P_m T_2 - \frac{C_{if}}{M+N} - (M+N)C_{iv} - C_{ins}(P_r T_1 + P_m T_2) - (M+N)L_{fs} \\
& - U_R(M+N) \sqrt{\frac{CI}{\gamma}} T_B - C_r T_1 P_r - F_{cl} - C_{cl} \sqrt{\frac{CI}{\gamma}} T_B (M+N) \\
& - H_m \left[ \frac{P_m T_2^2}{2} \left(1 - \frac{\theta T_2}{3}\right) + MDT_B T_3 \left(1 + \frac{\theta T_B}{2} - \frac{\theta T_3}{2}\right) - \frac{1}{2} \left( DT_B^2 \left(1 + \frac{\theta T_B}{2}\right) M(M-1) \right) \right] \\
& - H_r \left[ \frac{P_r T_1^2}{2} \left(1 - \frac{\theta T_1}{3}\right) + NDT_B T_3 \left(1 + \frac{\theta T_B}{2} - \frac{\theta T_2}{2}\right) \right. \\
& \left. - \frac{1}{2} \left( DT_B^2 \left(1 + \frac{\theta T_B}{2}\right) N(N-1) \right) \right] \\
& \left. - H_R \left[ \left( P_r - \frac{1}{\eta} \sqrt{\frac{CI}{\gamma}} \right) \frac{T_1^2}{2} + \frac{1}{\eta} \sqrt{\frac{CI}{\gamma}} \left( \frac{1}{2} (N+M)^2 T_B^2 - \frac{T_1^2}{2} - (N+M)T_B T_1 + T_1^2 \right) \right] - CI - K_m - K_r \right\} \quad (22)
\end{aligned}$$

### 3.1 Solution Procedure

From Eqs. (15)–(22), the total profit function can be determined in terms of  $N$ ,  $M$  and  $T_B$ .

Hence the purpose of this study is to derive the optimal number of deliveries and the replenishment cycle time by determining the optimal values of  $N$ ,  $M$  and  $T_B$  that maximize the total profit. The model has been solved using Algorithm given below.

### 3.2 Algorithm

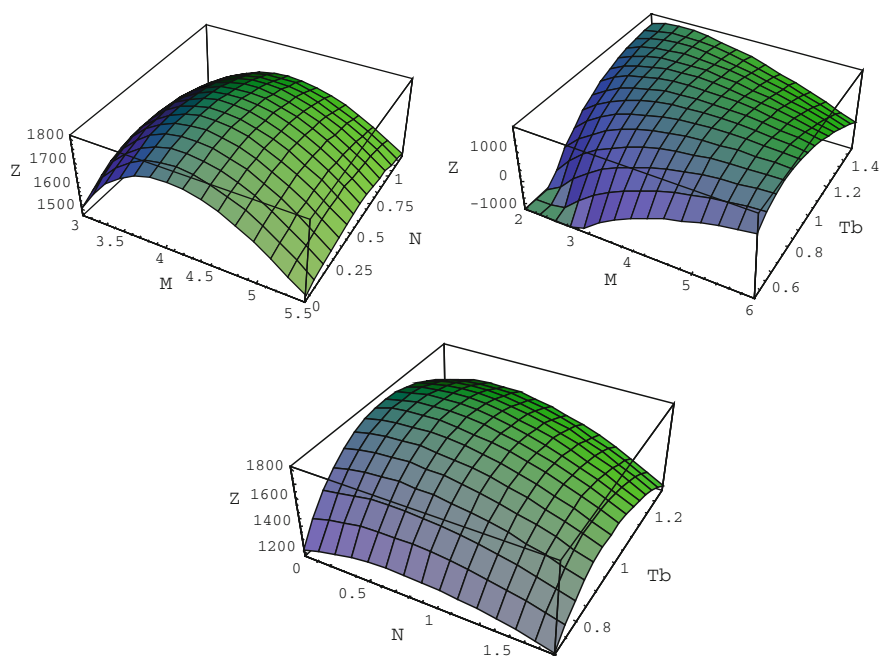
- Step 1: Taking the first derivative of the total profit function w.r.t. to  $T_B$ , equate it equals to zero and then determine the value of  $T_B$
- Step 2: Putting the value of  $T_B$  in Eq. (25) and then derive the value of  $N$  and  $M$  by using the following conditions for maximizing the supplier's profit.

$$\begin{aligned}
TP(N, (M-1)|T_B) & \leq TP(N, M|T_B) \geq TP(N, (M+1)|T_B) \\
TP((N-1), M|T_B) & \leq TP(N, M|T_B) \geq TP((N+1), M|T_B)
\end{aligned}$$

- Step 3: Using the optimum values of  $N$ ,  $M$  and  $T_B$  determine the maximum profit for the system.

**Table 1** Optimal results for integrated cost minimization problem

$M$	$N$	$T_B$	$q$	$T_1$	$T_2$	$T_3$	$TC$
4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98



**Fig. 3** Convexity of the closed loop supply chain

**4 Numerical Analysis and Sensitivity Analysis**

**Example 1** The above theoretical results are illustrated through the numerical verification, to illustrate the proposed model we have considered the following input parameters in appropriate units

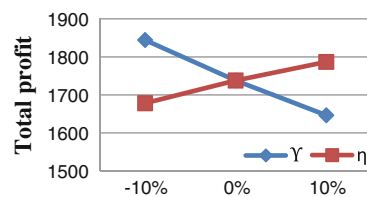
$P_r = 2500$ ,  $P_m = 1200$ ,  $d = 1000$ ,  $\theta = 0.01$ ,  $\eta = 5$ ,  $CI = 8000$ ,  $\gamma = 0.01$ ,  $A = 500$ ,  $H_B = 1$ ,  $H_r = 1$ ,  $H_R = 0.8$ ,  $H_m = 1$ ,  $K_m = 1000$ ,  $K_R = 1000$ ,  $C_m = 6$ ,  $C_r = 3$ ,  $U_R = 3$ ,  $U_m = 4$ ,  $C_S = 6$ ,  $S_S = 12$ ,  $C_{if} = 3000$ ,  $C_{iv} = 500$ ,  $C_{ins} = 0.5$ ,  $L_{fs} = 100$ ,  $C_{cl} = 0.2$ ,  $F_{cl} = 1500$ .

Mathematica 8.0 is used to derive the optimal solution and results are presented in Table 1.

The convexity of the reverse logistics inventory model is shown in Fig. 3. The three dimensional graph shows that the integrated expected total profit is concave, and that there exists a unique solution maximizing the integrated expected total profit.

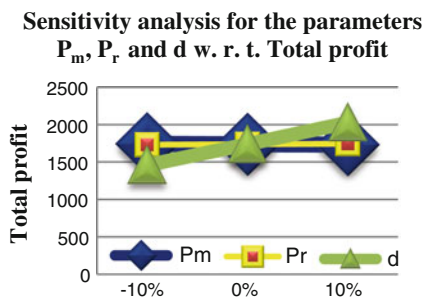
**Table 2** Sensitivity analysis for the production, remanufacturing and demand rate parameters  $F_{cl}$ ,  $C_{iv}$ ,  $A$ ,  $\eta$ ,  $\gamma$ ,  $P_m$ ,  $P_r$  and  $d$ 

		$M$	$N$	$T_B$	$q$	$T_1$	$T_2$	$T_3$	$TP$
$\gamma$	-10 %	4	1	1.00837	1013.45	0.38028	0.0251014	4.03348	1844.32
	0 %	4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98
	+10 %	4	1	1.01315	1018.28	0.345606	0.0617059	4.05259	1646.42
$\eta$	-10 %	4	1	1.00566	1010.72	0.399773	0.00451352	4.02264	1678.06
	0 %	4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98
	+10 %	4	1	1.01525	1020.41	0.330207	0.0779554	4.06101	1786.73
$P_m$	-10 %	4	1	1.01098	1016.09	0.361698	0.0447368	4.04391	1742.78
	0 %	4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98
	+10 %	4	1	1.0109	1016.01	0.36167	0.0447332	4.0436	1733.18
$P_r$	-10 %	4	1	1.01061	1015.72	0.401741	0.0496887	4.04244	1730.9
	0 %	4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98
	+10 %	4	1	1.01121	1016.32	0.328891	0.0406795	4.04483	1743.76
$d$	-10 %	4	1	1.05883	957.989	0.378817	0.00437826	4.23531	1459.25
	0 %	4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98
	+10 %	4	1	0.968789	1070.83	0.346605	0.0817275	3.87516	2027.14
$A$	-10 %	4	1	1.00936	1014.45	0.361118	0.0446618	4.03743	1747.88
	0 %	4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98
	+10 %	4	1	1.01252	1017.64	0.362249	0.0448081	4.05007	1728.09
$C_{iv}$	-10 %	4	1	1.003	1008.03	0.358845	0.044368	4.01201	1787.63
	0 %	4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98
	+10 %	4	1	1.01881	1024.00	0.364499	0.0450992	4.07523	1688.71
$F_{cl}$	-10 %	4	1	1.00619	1011.25	0.359984	0.0445151	4.02474	1767.72
	0 %	4	1	1.01094	1016.05	0.361684	0.044735	4.04375	1737.98
	+10 %	4	1	1.01567	1020.83	0.363376	0.0449539	4.06267	1708.37

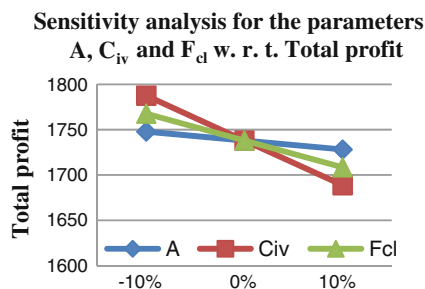
**Fig. 4** Effect of returned rate on total profit**Sensitivity analysis for the parameters  $\gamma$  and  $\eta$  w. r. t. Total profit**

**Example 2** We now study the effects of changes in the values of the system parameters  $F_{cl}$ ,  $C_{iv}$ ,  $A$ ,  $\eta$ ,  $\gamma$ ,  $P_m$ ,  $P_r$  and  $d$  on the optimal total profit and number of reorder. The sensitivity analysis is performed by changing each of the parameters by -10, 0 and 10 %, taking one parameter at a time and keeping the remaining parameters the same as in Example 1. The sensitivity analyses of the different parameters are shown in Table 2. The graphical representation of the sensitivity of decision variables is provided in Figs. 4, 5 and 6.

**Fig. 5** Effect of production, remanufacturing and demand on total profit



**Fig. 6** Effect of ordering, inspection and cleaning cost on total profit



#### 4.1 Observations

- 1) Table 2 reveals that the total profit is positive sensitive to the changes in parameter  $\eta$  while negative sensitive to the changes in parameter  $\gamma$  hence it seems that to procure the used products from the user is profitable but resell them in the secondary market in as-is condition is better than the remanufacturing.
- 2) From the table it is observed that the total profit is slightly negative sensitive to the changes in parameter  $P_m$  while slightly positive sensitive to the changes in parameter  $P_r$ . Hence it can be said that remanufacturing is more profitable than the production.
- 3) Table 2 reveals that the total profit is moderately positive sensitive to the changes in demand parameter. This is a logical tendency since it allows the vendor and buyer to get more cost savings from accumulated revenue.
- 4) From the table it is observed that the total profit is moderately positive sensitive to the changes in parameters  $F_{cl}$ ,  $C_{iv}$  and  $A$  which is obvious. But if we compare the behaviour of these three parameters it is noted that the cleaning cost is more sensitive than the ordering cost while less sensitive than the inspection cost.

## 5 Conclusion

In the presented paper we have discussed the effect of JIT on a green supply chain inventory model. Here we have determined the model for the deteriorating products where the deteriorated products are delivered to the secondary market. In

this article we derived a profit function for the mathematical model developed here and hence determine the optimal results with the help of a numerical example. The results shows that the reselling the used products in the secondary market is profitable than the remanufacturing. In the further study the model can be developed for the remanufactured items whose quality standard is not as good as those of new products.

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