

From Ice to Penguins: The Role of Mathematics in Antarctic Research

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Abstract Mathematics underpins all modern Antarctic science as illustrated by numerous activities carried out during the international year “Mathematics for Planet Earth”. Here, we provide examples of some ongoing applications of mathematics in a wide range of Antarctic science disciplines: (1) Feeding and foraging of marine predators; (2) Fisheries management and ecosystem modelling; and (3) Climate change research. Mathematics has allowed the development of diverse models of physical and ecological processes in the Antarctic. It has provided insights into the past dynamics of these systems and allows projections of potential future conditions, which are essential for understanding and managing the effects of fishing and climate change. Highly specific methods and models have been developed to address particular questions in each discipline, from the detailed analyses of remote-sensed predator tracking data to the assessment of the outputs from multiple global climate models. A key issue, that is common to all disciplines, is how to deal with the inherent uncertainty that arises from limited data availability and the assumptions or simplifications that are necessary in the analysis and modeling of interacting processes. With the continued rapid development of satellite-based and remote observation systems (e.g. ocean drifters and automatic weather stations), and of new methods for genetic analyses of biological systems, a step-change is occurring in the magnitude of data available on all components of Antarctic systems. These changes in data availability have already led to the development of new methods and algorithms for their efficient collection, validation, storage

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and analysis. Further progress will require the development of a wide range of new and innovative mathematical approaches, continuing the trend of world science becoming increasingly international and interdisciplinary.

1 Introduction

The Polar Regions are the cornerstones of the global ecosystem, barometers of the health of the planet, and messengers of global processes [49, 56]. Because it strongly influences the global climate and harbours unique and diverse biological communities, the Antarctic plays a distinct and critical role in both the physical Earth system and the ecosystem that it supports. Antarctica is renowned as being the highest, driest, windiest and coldest continent, boasting the lowest recorded temperature on Earth, -93.2°C , on the East Antarctic Plateau (<http://www.nasa.gov/press/2013/december/nasa-usgs-landsat-8-satellite-pinpoints-coldest-spots-on-earth/#.UqndqvwoYt>, accessed 12/12/13), but it is surrounded by the Southern Ocean which, in contrast, is very thermally stable (with some locations varying as little as 0.2°C over a year) [25]. Some of the key science on globally important issues is conducted in the Antarctic, often coordinated by the Scientific Committee on Antarctic Research and various the bodies that administer the Antarctic Treaty System. These issues include sea level rise, climate change, ocean acidification, biodiversity change, the ozone hole and global ocean circulation [3, 25, 56, 72, 89, 91, 92, 97, 98]. Furthermore, the Antarctic continues to spark the curiosity and imagination of people around the world. It appeals to the sense of adventure and fear of the unknown. These are perfect ingredients for education and outreach [52, 102, 103, 117], providing an excellent way to transmit basic concepts about a wide range of Science, Technology, Engineering and Mathematics (STEM) disciplines. During the international year “Mathematics for Planet Earth”, numerous activities related to mathematics were carried out throughout the world, including the International Conference and Advanced School Planet Earth, Mathematics of Energy and Climate Change, held in Lisbon (Portugal), in 21–28 March 2013. Here, we follow discussions at that conference with a selective review of how mathematics is applied in a wide range of Antarctic science disciplines

2 The Scope of Mathematical Analyses in Antarctic Science

Mathematics underpins all modern Antarctic science. It is central to of the data collection process, for example in generating efficient algorithms to allow data storage and transfer, and for the calibration and validation of data from in-situ and remote instrumentation (e.g. automatic weather stations and satellite-based instruments). Mathematics is used in analyses and modeling of all aspects of Antarctic science including weather and climate, ice sheet and sea ice dynamics,

ocean circulation, biogeochemical cycles and ecosystem processes. The range and complexity of applications is wide, from simple analyses of small scale experiments to high resolution satellite-based studies that provide circumpolar views, and from simple theoretical to fully coupled atmosphere-ocean-ice models. Here, we illustrate the development and application of mathematical analyses by considering three major areas of Antarctic science: (1) Feeding and foraging of marine top predators; (2) Fisheries management and ecosystem modeling; and (3) Climate change research. These sections provide illustrations in three distinct types of scientific activity. Studies of the feeding and foraging of marine top predators are strongly field based and require extensive sample collection and analysis and careful design of sampling methods. With the advent of satellite instrumentation, remote tracking now provides high resolution information on position and movement, which has revolutionized analyses of predator foraging. This has been associated with the development of a range of other remote devices, and has generated a step-change in the size of datasets available. The second area, fisheries management and ecosystem modeling, provides an illustration of the use of mathematical methods in an applied arena to generate robust policy advice. The final area, climate change, illustrates the challenge of developing projections of the impacts of future change that can only be addressed through mathematical analysis and modelling.

3 The Application of Mathematics in the Study of Feeding and Foraging Ecology of Marine Top Predators

In order to understand how the Southern Ocean food web operates, it is essential to understand what animals eat and where they feed. To obtain reliable estimates from the available data requires a wide range of mathematical tools (particularly statistical and modeling tools). The most common source of feeding data is the stomach contents of sampled predators. To characterize the diet of top predators, such as penguins (Fig. 1) or albatrosses, prey in these stomach contents are generally quantified by their frequency of occurrence, or the number or mass of each prey species [87, 112]. To identify the prey (generally fish, cephalopods such as squid and octopods, and crustaceans), scientists often have to use hard structures that are not destroyed by digestion. These structures include the sagittae otoliths (colloquially the “ear bones”) of fish. Otoliths are calcium carbonate structures located directly behind the brain of teleost (bony) fish. For crustaceans, scientists use their carapaces and for cephalopods their beaks. Cephalopod beaks are chitinous structures, whose function is similar to that of teeth in carnivorous mammals: to grasp, kill and dismember their prey.

Allometric regression equations can be derived to describe the relationship between the mass and length of complete individuals of known species and the size of their otoliths, carapaces or beaks. When applied to hard structures found in stomach contents these equations provide a valuable mathematical tool for

Fig. 1 Penguins, such as macaroni penguins, are important components of the Southern Ocean ecosystem and are difficult to directly observe because of the remote and hostile conditions in which they live and the considerable distances that they travel. Nonetheless Antarctic scientists have used mathematical tools to develop ways to study their behavior and ecology in the wild, including their feeding and foraging ecology (photo by José Xavier)



reconstructing what a predator has been consuming [14, 37, 88, 110]. However, numerous prey species do not have allometric equations because they are still poorly known (therefore scientists must rely on equations from closely related species) and many of the available allometric equations are based on a limited number and size range of specimens. Therefore, future work must focus on obtaining more complete fish, crustaceans and cephalopods to improve allometric equations, and on characterizing the uncertainty that is inherent in the application of such methods [112, 113, 115, 116, 118, 119].

One of the key issues that marine ecologists need to address, when assessing the diet and feeding ecology of a predator, is how many samples are needed. This is essential to characterize their diet correctly, and so to provide fundamental data for food web studies, particularly modeling the present ecosystem status and predicting future changes. Mathematically, this is an interesting challenge. A randomization technique was used to estimate the number of stomach samples from albatrosses needed to reach two saturation points: (1) the maximum cumulative number of species; and (2) where each of the five most important species (i.e. >5 % of the diet, by mass) was present in at least one sample [113]. For each sampling event, the program randomly selected one of the samples and checked the species present. If one or more of the required species were absent, the program randomly selected another sample that had not yet been selected, and the process was repeated until one of the two saturation points was reached. The entire process was repeated 100 times. This study also compared different ways of collecting samples (i.e. using stomach contents or voluntary regurgitations, named boluses) which permitted the investigation of biases associated with each sampling method [113].

Other techniques for analyzing diet use tissues from stomach samples to identify prey species, or from predators (e.g. flesh, feathers, blood) to identify their habitat

or trophic level (e.g. DNA analyses, stable isotopes, fatty acids, trace elements, chemical pollutants) with considerable success [21, 28, 28, 53, 86, 96]. Each of these techniques involves its own unique analytical challenges. Mixed data sources (e.g. diet data obtained from stomach contents and data on the stable isotope signatures from predators and prey) can be compared to calibrate different methods. A Bayesian multisource stable isotope mixing model (SIAR: Stable Isotope Analyses in the statistical package R) has been used to estimate the probable contributions of each prey to the diet of each individual and hence the predator's level of specialization on particular prey items [74]. This method indicated that for wandering albatrosses *Diomedea exulans* fish was the main component (56.4 %) of the diet, followed by cephalopods (43.6 %). These proportions were similar to those from analysis of stomach contents, showing the usefulness of these models for future research [20].

Advances in micro-technology (and the decreasing of the size of tracking devices) in the last two decades have revolutionized our understanding of the foraging behavior of predators [12, 12, 36, 77, 79, 79]. Seabirds can travel great distances (hundreds to thousands of kilometres) and exhibit a number of unique physiological adaptations for such highly pelagic lifestyles [29]. Albatrosses and petrels spend the great majority of their lives at sea, and the use of tracking technology is the most effective and, in many respects the only, means for gaining detailed insights into their foraging behaviour [51, 73, 83].

Satellite sensors, combined with “ground truth” data from in situ surveys, are contributing to a better understanding of ocean systems by providing large scale and long-term data on biological bulk parameters such as chlorophyll, and on ecologically relevant physical parameters, such as sea surface temperature or ice cover [97]. These data, combined with tracking technology can be used to answer scientific questions about foraging behavior and how animals use their ocean habitat. For example, satellite-tracking on animals in the late 1990s involved the deployment of a Platform Terminal Transmitter (PTT) that sends a short radio signal typically every 90 s to polar-orbiting NOAA satellites. The precision of the location estimate can vary from meters to hundred of meters, depending on the number of satellites in view at that place and time, the design and power of the transmitter, and the speed of the animal [108]. More recently, Global Positioning System (GPS) loggers have been widely used, mostly because of their higher precision (within 10 m) [107] and ability to record positions at various time intervals, from minutes to days (depending on the amount of time the device is on) [70]. However, if scientists are more interested in knowing where animals are for a longer period of time (e.g. large migration studies), geolocators or Global Location Sensing (GLS) loggers are extremely useful [27, 78]. GLS loggers record ambient light. This allows the estimation of sunset and sunrise times from curve thresholds. These times in turn allow the estimation of latitude from day length, following standard astronomical algorithms, and longitude from the time of local mid-day with respect to GMT and Julian day. The disadvantages are that the animal must be recaptured (as with most GPS loggers), only two locations can be calculated per day, latitude estimation is

impossible for variable periods around the equinoxes, and the precision is relatively low, with an average error of 186 km estimated for free-ranging albatrosses [78].

These examples demonstrate that the reliable estimation of animal location, and its associated error, is a fundamental part of modern animal ecology. There are many existing techniques for handling location error, but these are often *ad hoc* or are used in isolation from each other. There is a Bayesian framework for determining location that uses all the data available, is flexible enough to be used with all tagging techniques, and provides location estimates with built-in measures of uncertainty [95]. Bayesian methods allow the contributions of multiple data sources to be decomposed into manageable components. Sumner et al. [95] showed that many of the problems with uncertainty in archival tag and satellite tracking data can be reduced and quantified using readily available tools.

With these mathematical tools applied to the feeding and foraging of top predators, it has been possible to model potential areas where poorly known organisms may be distributed. Indeed, the distribution of many cephalopod, crustacean and fish species in the Southern Ocean, and adjacent waters, is poorly known, particularly during times of the year when research surveys are rare [16, 35, 90, 111]. Analysing the stomach samples of satellite-tracked higher predators has been advocated as a potential method by which such gaps in knowledge can be filled. This approach showed that wandering albatrosses, *Diomedea exulans*, foraged in up to three different water-masses, the Antarctic zone (AZ), the sub-Antarctic zone (SAZ) and the sub-Tropical zone (STZ) [114]. A probabilistic mathematical model was applied to the tracking and diet data collected from wandering albatrosses to construct a large scale map of where various prey were captured. Furthermore, robustness and sensitivity analyses were used to test model assumptions about the time spent foraging and relative catch efficiencies and to evaluate potential biases associated with the model. The analysts were able to predict the distributions of a multiple cephalopod, crustacean and fish species [114]. This method is likely to be used in the future to predict the distributions of poorly known species, such as large oceanic cephalopods, that are not effectively sampled using nets [109, 115, 119].

In summary, mathematical methods are critically important to studies in marine ecology, including those related to the feeding and foraging ecology of top predators. The many examples range from producing mathematical mixed models to quantify the consumption of prey to providing the algorithms that allow the tracking of top predators in the Southern Ocean.

4 The Application of Mathematics in Fisheries Management and Ecosystem Modelling

4.1 Management of Southern Ocean Fisheries

Fishing is one of the main economic activities in the Southern Ocean, alongside science and tourism [34]. The responsible management of these fisheries is therefore

an important applied ecology problem, which has led to innovative approaches that make extensive use of mathematics and modelling. Fishing removes animals from an ecosystem which would otherwise continue feeding, growing, reproducing and being fed upon. Such removals can reduce the ability of fished populations to replace themselves and they can have wider impacts on other populations by changing the balance of predators and prey. The Southern Ocean ecosystem has already experienced considerable perturbation as a result of past harvesting which started in the late 1770s and led to localised extinctions of Antarctic fur seals *Arctocephalus gazella* and the commercial extinction of many baleen whale species which had previously consumed an estimated 175 Mt yr^{-1} of Antarctic krill *Euphausia superba* [57].

Antarctic krill is a swarming shrimp-like animal that grows to a maximum of about 6 cm, and is now the target of an expanding fishery [39, 71]. There is also commercial harvesting of various fish species including the high-value Antarctic toothfish, *Dissostichus mawsoni*, and Patagonian toothfish, *Dissostichus eleginoides* [34]. Fish products are generally sold for direct human consumption while krill is usually processed to produce fishmeal for aquaculture, and oil which is sold as a health supplement [39, 71]. These fisheries are managed by the Commission for the Conservation of Antarctic Marine Living Resources (CCAMLR), which was established in 1982. CCAMLR is responsible for ensuring that fisheries do not cause long-term damage to fished populations or the wider ecosystem. Consequently fisheries management draws on a much broader research effort which aims to understand the dynamics and structure of Southern Ocean ecosystems.

One of the key challenges faced by the scientists who advise CCAMLR is uncertainty. Assessments of the state of fished populations are affected by sometimes considerable estimation error and there are no failsafe models to indicate how these populations change in response to fishing, environmental variability and changes in other populations. The uncertainty about how fishing will affect complex ecosystems is even greater. Thus many of the major uses of mathematics in Southern Ocean fisheries management and related research address uncertainty in some form. These uses include producing useful estimates of the state of fished stocks from limited observations, identifying safe catch levels, understanding ecosystem structure and dynamics and evaluating potential risks to the wider ecosystem.

CCAMLR uses the precautionary approach to identify catch levels for Southern Ocean fisheries. Hill [39], paraphrasing Garcia [32], states that the precautionary approach aims to “reduce the probability of occurrence of bad events within acceptable limits when the potential for these events is plausible, but not necessarily demonstrated, and the potential costs are significant.” Hill [39] also suggests that the precautionary approach should reduce the risk of harm to the ecosystem by setting low catch limits and protecting areas from fishing until there is evidence that the risks associated with more intensive fishing are acceptable.

4.2 *Analyses and Models for the Management of Fin Fish Stocks*

In order to provide robust management advice to CCAMLR on sustainable catch limits that are consistent with the precautionary approach, fisheries scientists undertake regular (annual or biennial) assessments of exploited fin fish stocks. In common with fisheries management elsewhere, these stock assessments use a vast array of fishery-dependent (e.g. catch rates) and fishery-independent (e.g. local biomass estimates from scientific fishing) data to describe the past and current status of a stock and to project the potential response of the stock to current and future management options (e.g. catch limits). Mathematical techniques lie at the heart of all stock assessments and are used in the construction of assessment models for each fished stock. These models are generally based on population dynamics models that can have varying degrees of complexity. The choice of stock assessment model will depend both on the quality and availability of data on catch and fishing effort and knowledge and availability of information on stock size, geographical stock boundaries, and species-specific life history traits such as growth, natural mortality and sexual maturity. Our understanding of these processes is usually summarized in formal mathematical models (e.g. the von Bertalanffy growth equation) [19].

The two species of toothfish mentioned above are exploited by deepwater demersal longline fisheries in various locations throughout the Southern Ocean [33]. Several of these fisheries have taken place for over two decades and consequently assessments can draw on a large amount of fishery-dependent and ecological data. These “established” fisheries, that include those carried out within the Ross Sea and at a number of sub-Antarctic islands (i.e. South Georgia [48] and the Heard and McDonald islands [18]) are assessed using age—structured, Bayesian “integrated” stock assessment methods. The input data for these assessments include trawl survey estimates of recruitment, commercial catch at length or age data, standardised catch rate data, mark-recapture data from multi-year tagging programmes, and estimates of natural mortality, growth, the length-weight relationship and maturity data. Given the integrated nature of these assessments in which many datasets are used concurrently to estimate parameters, much attention is given to the statistical weighting of each dataset. Bayesian methods are frequently used in the estimation procedure and uncertainty in the dynamics is evaluated using Markov Chain Monte Carlo (MCMC) methods [60, 61].

A number of smaller fisheries for the two toothfish species exist in the high seas areas of the Southern Ocean, in particular on the seamounts of the Indian Ocean sector for which data on stock size and biological parameters is far more sparse [2]. In these new, exploratory and research fishery areas, biomass estimates of the local toothfish population are usually derived from mark recapture data and calculated using the Lincoln -Peterson equation which estimates population size as the product of the numbers of animals captured in each of two events divided by the number that were captured twice (i.e. in both events) [58]. This biomass estimate allows suitable catch limits to be obtained by the application of a conservative exploitation

rate. The scientific purpose of these fisheries, which are considered “data poor”, is the collection of high quality data on abundance and the biological characteristics of the stock with the aim of developing fully integrated stock assessments in the near future. As more abundant and robust data become available for these fisheries, more complex population dynamics models are developed and tested in the transition towards a fully integrated assessment.

As with all biological systems there are varying degrees of uncertainty associated with the data used within the stock assessment models. A suite of mathematical procedures has been developed to address this uncertainty in order to improve model fits within the stock assessments of Southern Ocean fin fish populations. These procedures are part of an integrated approach which aims to reduce the uncertainty in the projections used to evaluate management options. The areas of greatest uncertainty have included the estimation of levels of illegal fishing [1], tagging [120], cetacean depredation [22], unaccounted fishing mortality [106], appropriate model weighting for catch-at-age data, catch [17] and natural mortality [19], among others.

4.3 Analyses and Models for the Management of Antarctic Krill Stocks

Antarctic krill is a highly abundant species. Atkinson et al. [6] used various statistical models to estimate the gross growth potential, the amount of new biomass that would be produced by growth each year if all animals survived. These estimates ranged from 342 to 536 Mt yr⁻¹ depending on the model used. For comparison, total global marine fisheries landings are approximately 80 Mt yr⁻¹ [30]. Of course, Antarctic krill do not achieve their full growth potential because many of them do not survive the year. The vast population of Antarctic krill is continually grazed by an array of predators including pelagic and demersal fish, penguins and other seabirds, whales, seals and even benthic invertebrates. Many of these predators rely on Antarctic krill as their main source of food [57, 104, 112]. For this reason the precautionary approach for Antarctic krill has to consider the indirect effects of fishing on predators since it effectively removes part of their food supply [34]. Management which includes such considerations is sometimes known as Ecosystem Based Management [63].

In a logistic biomass growth model, the per-capita rate of increase is highest at half of the asymptotic biomass. This leads to the hypothesis that fished populations are most productive if reduced to half of their pre-fishing biomass [84]. However, the requirement to explicitly manage potential impacts on Antarctic krill predators led to a more precautionary objective: to ensure that, in the long-term, fishing does not reduce the Antarctic krill population by more than 25 % on average [23, 42]. Scientists use a stochastic population projection model to identify catch levels that meet this criterion. The model runs multiple simulations with random deviates in various population parameters (e.g. recruitment, natural mortality, age at maturity)

and a range of different catch levels, until it finds the correct level. During this process catch levels are also assessed against another criterion: that the risk of the breeding population falling below 20 % of its initial biomass is no more than 10 %. The highest catch level that meets both criteria is selected to manage the fishery [23].

Smith et al. [93] used nine ecosystem dynamics models (that is models of the interacting dynamics of multiple species) to assess the potential impacts of fishing on the rest of the ecosystem. This study considered fisheries for lower trophic level species, such as capelin (*Mallotus villosus*), herring (*Clupea* spp.) and anchovies (e.g. *Engraulis* spp.) in other oceans and did not directly consider the Antarctic krill fishery. Nonetheless it found that allowing a fishery to deplete the biomass of the fished population by no more than 25 % provided reasonable catch levels while achieving “much lower impacts on marine ecosystems” than the higher depletion rates allowed by many fisheries management regimes. This suggests that the general approach used for setting Antarctic krill catch limits might be appropriately precautionary. However, a recent study shows that the catch limits selected using this approach are sensitive to assumed levels of recruitment variability and that recruitment variability in real Antarctic krill stocks might be higher than that assumed in model projections [55]. The ecosystem impacts of fishing depend not just on how much biomass of the fished species it removes, but also where it removes biomass from. Although Antarctic krill is widely distributed throughout the Southern Ocean, the vast majority of the catch (83 % of all reported catch to date) [39] is taken from the Scotia Sea and southern Drake Passage (Fig. 2) and is in fact concentrated in just 26 % of this area [33]. Specifically, fishing occurs in and close to the shallow waters that surround the many islands in this area. Fishing does not generally occur in the more hostile waters of the open ocean where Antarctic krill is still abundant but much less likely to occur in the dense aggregations that the fishery targets [45]. Scientists have used ecosystem dynamics models to assess the risk that such spatially restricted fishing poses to Antarctic krill predators [81, 105]. These models are spatially resolved to distinguish the various shallow water and open ocean areas and they represent the interactions between Antarctic krill, the fishery, and several groups of competing predators. The exact nature of these interactions is uncertain and there is very little information about past dynamics from which to infer the interactions. Consequently, the modelers did not attempt to devise a single best model to project the consequences of future fishing. Instead they attempted to evaluate the uncertainty in such projections and they translated this uncertainty into estimates of the risks associated with candidate management options (Fig. 3).

The approach to this uncertainty about the true nature of the modeled interactions was to use multiple plausible “scenarios” or plausible representations of the system [44]. The word “scenario” here means a model and its data (sensu Rademeyer et al. [85]). The scenarios were based on two different model structures, described in Plagányi and Butterworth [81] and Watters et al. [105] and several alternative parameterizations of each model structure. These alternative parameterizations were chosen specifically to bracket key uncertainties. For example, the speed at which

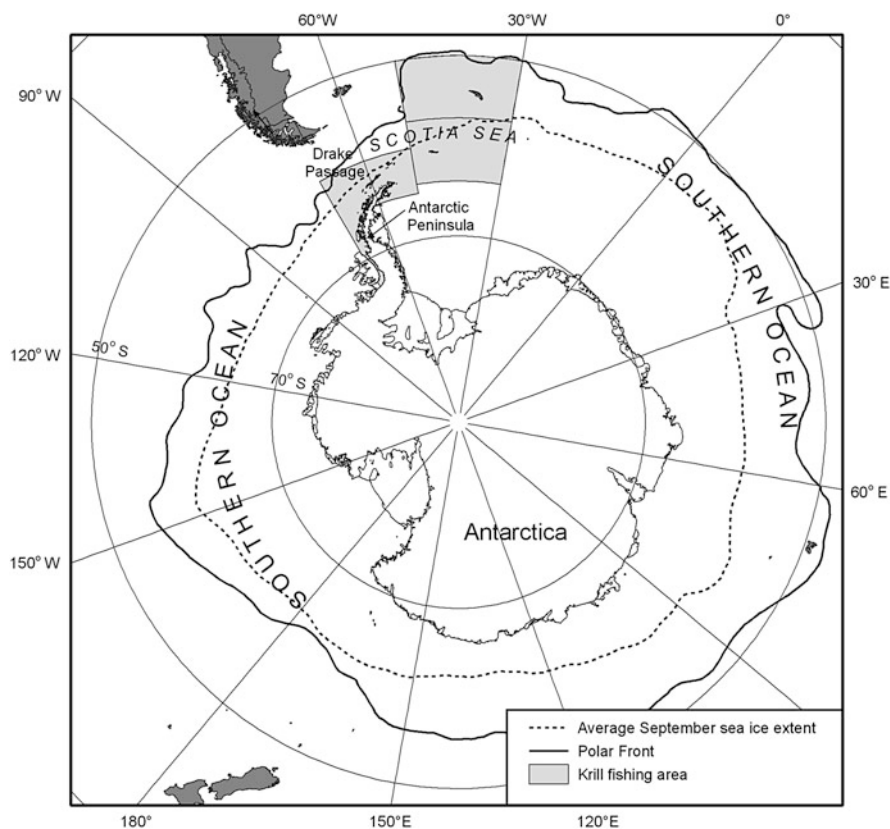


Fig. 2 The Antarctic continent and the Southern Ocean which surrounds it. The Polar Front is the approximate northern limit of the Southern Ocean ecosystem. Antarctic krill is a major component of this ecosystem, the main prey item for a diverse suite of predators and the focus of a developing fishery. Although Antarctic krill fishing is permitted in much of the Southern Ocean, the vast majority of the catch to date has been taken in the Scotia Sea and southern Drake Passage region [39, 71]. Antarctic krill abundance in this region is correlated with September sea ice extent [4], the average position of which (1979–2004) is shown

Antarctic krill are transported on ocean currents is not known, but the actual speed is likely to lie between a minimum of zero and a maximum of the speed of passive particles drifting with the currents, which can be deduced from ocean circulation models [43]. Watters et al. [105] developed four parameterizations, each of which combined one of these extreme values for plausible transport speeds with an extreme plausible value for a second key uncertainty affecting the functional relationship between prey availability and the proportion of the predator population that is able to breed.

Another important innovation recognized the impossibility of predicting with accuracy the future state of the system when it is influenced by multiple interacting

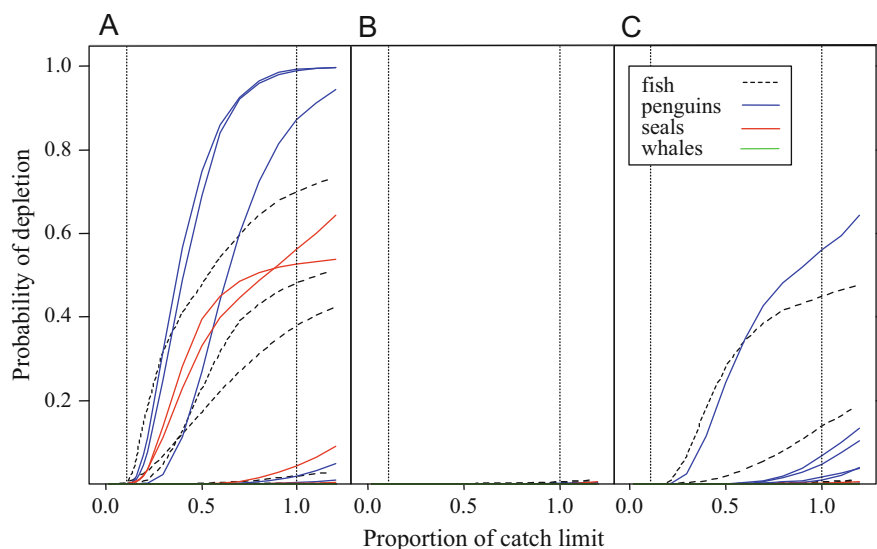


Fig. 3 The format used to present the results of model projections with intentionally high levels of uncertainty [38, 105]. The varied results of multiple simulations were used to calculate the probability of each modelled predator population falling below a threshold level. The results show how this risk increases with catch level (“proportion of catch limit”) and varies between three alternative spatial distributions of the catch limit (labelled A to C)

drivers including climate variability and change, and recovery from historic over-harvesting of whales. The modelers therefore assessed the marginal effects of Antarctic krill fishing in their projections by comparing them to otherwise identical projections without fishing.

The modelers performed 1001 stochastic projections with each scenario for each evaluated management option (consisting of a catch limit and its spatial distribution amongst modeled spatial units). One of the risks evaluated was the probability of each modeled predator population falling below 75 % of its size in comparable projections without fishing. The models generated several thousand projections per management option with which to calculate this probability. The analysts presented results in the format shown in Fig. 3, which shows the coherent accumulation of risk with increasing catch limit, and identifies the least risky spatial distribution (where the catch limit in each spatial unit is proportional to the total predator demand for Antarctic krill in the same unit, labeled “B” in the figure). Hill [38] demonstrated that this distribution remains the least risky even if a different reference level (other than 75 %) or scheme for aggregating modeled predator populations is used.

Because managers need to consider the implications of management options for the fished stock, the fishery and predators in multiple areas, the models assessed each of these risks. One important consideration is that various model outputs (e.g. the biomass of the fished stock versus the biomass of one of its predators) have

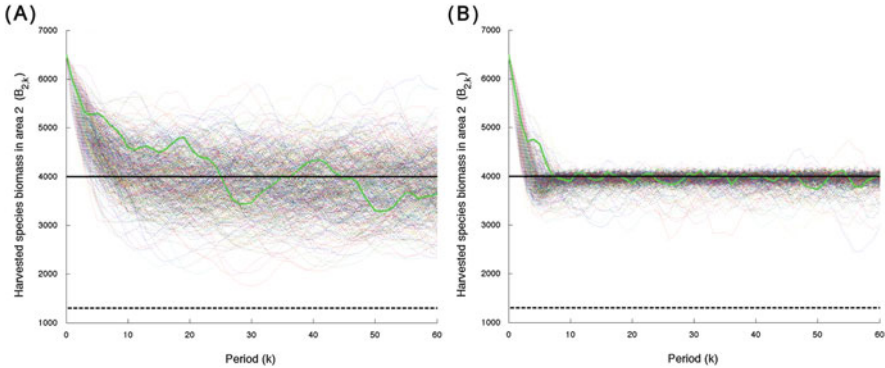


Fig. 4 The biomass of a modelled krill-like species in 500 stochastic simulations using two different harvest control strategies: (a) a fixed catch limit, as is currently used to manage the Antarctic krill fishery, and (b) a feedback method which uses model predictive control (MPC) to adjust catch limits in response to information about the harvested stock and its predators [40]

different levels of sensitivity to perturbations in model parameters, suggesting that uncertainties in these parameters could bias comparisons of different risks [41].

Scientists advising CCAMLR are attempting to develop a feedback management approach for the Antarctic krill fishery that will modify spatially resolved catch limits in response to information about the local and larger-scale state of the ecosystem. Such an approach is difficult to design and implement when there are multiple objectives for multiple connected areas, and when the system’s dynamics are complex and uncertain. Hill and Cannon [40] used a branch of control theory called model predictive control (MPC) to show that such an approach is feasible in principle and more likely than the current fixed catch limit to simultaneously achieve objectives for the state of the Antarctic krill stock, the state of multiple predator populations and the state of fishery catches (Fig. 4). Their study applied MPC to a relatively simple ecosystem dynamics model consisting of two connected areas, each containing a single prey population and a single predator population. Their study also clarified the information requirements of such an approach, which include regular estimates of each of the relevant state variables or, at least, reliable ways of inferring these from the other state estimates and, critically, a clear set of quantitative objectives for each relevant state. Defining such objectives is a major challenge facing CCAMLR and other organizations around the world which seek to implement Ecosystem Based Management [38, 59].

4.4 Ecosystem Modelling

Models exploring the interactions between different populations in the ecosystem are useful for devising and assessing Ecosystem Based Management approaches.

Some pioneering models of this type were developed for the Southern Ocean ecosystem in the 1980s [10, 11] and the modeling effort that continued to develop since then was the subject of a detailed review by Hill et al. [42]. More recent developments include the ecosystem dynamics models described above and a suite of Ecopath-type food web models [7, 26, 46, 80]. Ecopath-type models compile available data on the diet, biomass, and production and consumption rates of the numerous organisms in a particular food web [82]. Modelers generally aggregate these organisms in so-called functional groups to reduce the number of model parameters. The modelers then adjust the parameters to satisfy the “mass balance” constraint that the rate of biomass production by any prey group cannot exceed the rate of consumption of that prey biomass by its predators.

One use of Ecopath-type food web models is to identify which functional groups are likely to be strongly affected by changes in the abundance of fished species [101]. A related use is to explore the potential responses to a plausible change in one part of the food web. For example, Ballerini et al. (in press) converted their model of the winter food web in Marguerite Bay into a bottom-up model, in which consumer biomass increases or decreases with the availability of prey. They increased the modeled biomass of small phytoplankton relative to large phytoplankton while maintaining a constant total phytoplankton biomass. This change is consistent with recently observed effects [65]. The model predicted reduced production of Antarctic krill and its predators as a result of this change. Hill et al. [46] reduced Antarctic krill biomass by 80 % in their model of the South Georgia shelf food web and readjusted the parameters to achieve mass balance. They found that, without compensating effects, this produced a similar decline in the biomass of Antarctic krill predators (fish, seals, penguins and other seabirds). However, a combination of compensating effects (an increase in grazing zooplankton called copepods and a shift in predator diets to take advantage of this increased copepod biomass) could minimize the impacts on Antarctic krill predators. This illustrates the wide range of outcomes that are possible within the current uncertainties on ecological knowledge. Future model development and data collection should aim to better characterize these uncertainties so that it is possible to assess which outcomes are most likely.

The existing suite of food web models for the Southern Ocean provide a valuable resource for comparing the structure and operation of the different regional food-webs [68, 69]. However, each of the existing regional models was developed by a different modeling team, using patchy and uncertain data, and each model was designed and analyzed to address a unique set of research questions. The differences between the models therefore include real underlying ecological differences, differences due to sampling error in the available data, and differences in the assumptions and subjective decisions made by the various modeling groups. The challenge of distinguishing real ecological differences from these sources of uncertainty is likely to be a major theme in future food web modeling.

In summary, mathematics and modeling are critical to understanding ecosystem structure and dynamics, assessing potential responses to change and developing appropriate fisheries management approaches. CCAMLR’s commitment to Ecosystem Based Management and the relative paucity of ecological data for the Southern

Ocean produce some interesting challenges that have led to innovative ecological modeling and analysis. It is practically impossible to identify definitive models of ecosystem structure or dynamics and consequently much of this innovation and many of the ongoing challenges concern the appropriate treatment of uncertainty.

5 The Application of Mathematics in Antarctic Climate Change Research

The analysis and projection of climate change using mathematical modeling currently receives much attention from scientists, politicians, the media and the general public. Due to the increased rates of environmental change in the Antarctic, considerable research effort has been devoted to modeling the Antarctic atmosphere and the Southern Ocean, and to quantifying physical and biological aspects of change. Most global climate models suggest that regional temperature increases will be greatest and most rapid at higher latitudes [49, 98]. Rapid increases are already evident over the Antarctic Peninsula where, in the last half century, air temperatures have risen by 2–3 °C. To the west of the Antarctic Peninsula sea ice has also declined and ocean temperatures have increased by 1 °C over five decades [64, 99]. Although climate models have successfully helped to build a broad picture of the causes of recent regional change, there are still many gaps in knowledge which affect the ability of climate models to reliably represent the Antarctic climate and the behavior of its ice caps and sea ice. A recent study by Turner et al. [100] examined the annual cycle and trends in Antarctic sea ice extent (SIE) for 18 climate models. Many of the models have an annual SIE cycle that differs markedly from that observed over the last 30 years. In contrast to the satellite data, which exhibit a slight increase in SIE, the mean SIE of the models over 1979–2005 shows a decrease in each month [100]. The models have very large differences in SIE over 1860–2005. The negative SIE trends in most of the model runs over 1979–2005 are a continuation of an earlier decline. There are two major gaps in knowledge that hamper the understanding of the observed increase. Possibly the most important is the limited observational record, in which reliable Antarctic-wide estimates of SIE are only available after approximately 1979. It is therefore very difficult to estimate the size of natural fluctuations in ice extent, which may have contributed to the recent changes. Related to this, the other major gap is in understanding the processes for change that need to be mathematically represented in climate models. At present it seems that the processes responsible for the observed SIE increase over the last 30 years are not being simulated correctly [100].

Another important prediction of climate change models is changing patterns of precipitation, altering the water input to terrestrial ecosystems. Spatially detailed predictions are not yet available for Antarctica, although water is possibly the single most important factor limiting the distribution of Antarctic terrestrial biota [25]. In some Antarctic terrestrial systems local environmental changes result in greater

energy input and warming, which may be accompanied by a lengthening of the season in which liquid water is available. There is evidence that such changes might increase production, biomass, population size, community complexity and the rate of colonization by previously absent organisms [13, 25]. However, at fine scales a decrease or total loss of water input could lead to local extinctions and drastic changes in local ecosystem structure [24].

Increases in primary biological productivity are already being seen at the margins of the Antarctic continent. These occur in areas of sea-ice loss where recent ice shelf retreat has occurred [76]. However, Antarctic marine species are generally amongst the least capable of adapting to environmental change. There are three main reasons [75]: (1) The geographical range over which they can live or disperse is restricted; (2) they have evolved to live in a very specific environment and tolerate only a narrow range of environmental conditions; and (3) they have long life histories and consequently slow rates of adaptation. Statistical analysis of experimental research provides evidence that the shallow mega- and macrobenthos are also very sensitive to temperature change (stenothermal). Being warmed by about 5 °C over periods greater than one month kills most species tested to date, but even smaller temperature rises (2 or 3 °C above normal) drastically hinder their ability to perform critical functions, such as avoiding predators [9]. In pelagic waters, changes to key pelagic species have also been notable. Regression analysis indicates a statistically significant relationship between Antarctic krill abundance and winter SIE in the western Scotia Sea, and there were apparent declines in both between the 1970s and 1980s [4, 99]. Further SEI declines would likely lead to more changes in the distribution and abundance of Antarctic krill.

Some studies have combined climate projections from global climate models with statistical models linking ecological processes to environmental variables (e.g. [40, 54, 54]). For example, Hill et al. [40] used sea surface temperature projections from 16 climate models with a statistical model linking Antarctic krill growth [5] to sea surface temperature. They found that plausible future warming is likely to lead to substantial reductions in the ability of Antarctic krill to produce new biomass throughout the northern Scotia Sea (Fig. 5). This is where large populations of Antarctic fur seals, *Arctocephalus gazella*, penguins and flying seabirds feed on Antarctic krill during the summer breeding season. A reduction in Antarctic krill biomass could result in greater predation on alternative prey and therefore negative impacts on some fish species [3]. As mentioned in the previous section, food web models have been used to assess how such changes could propagate through the food web [7, 46]. A key issue taken into account by Hill et al. [47] is that different climate models give different projections, contributing to uncertainty in estimates of future change. Assessing and quantifying this uncertainty is an important mathematical challenge in itself and an active area of research is in developing statistical approaches to combining information from different climate models [15, 94].

The effects of climate change in populations of top predators, such as penguins, have also been considered [8]. Even apparently straightforward tasks, like obtaining an estimate of the total number of penguins, are not easy and require plenty of

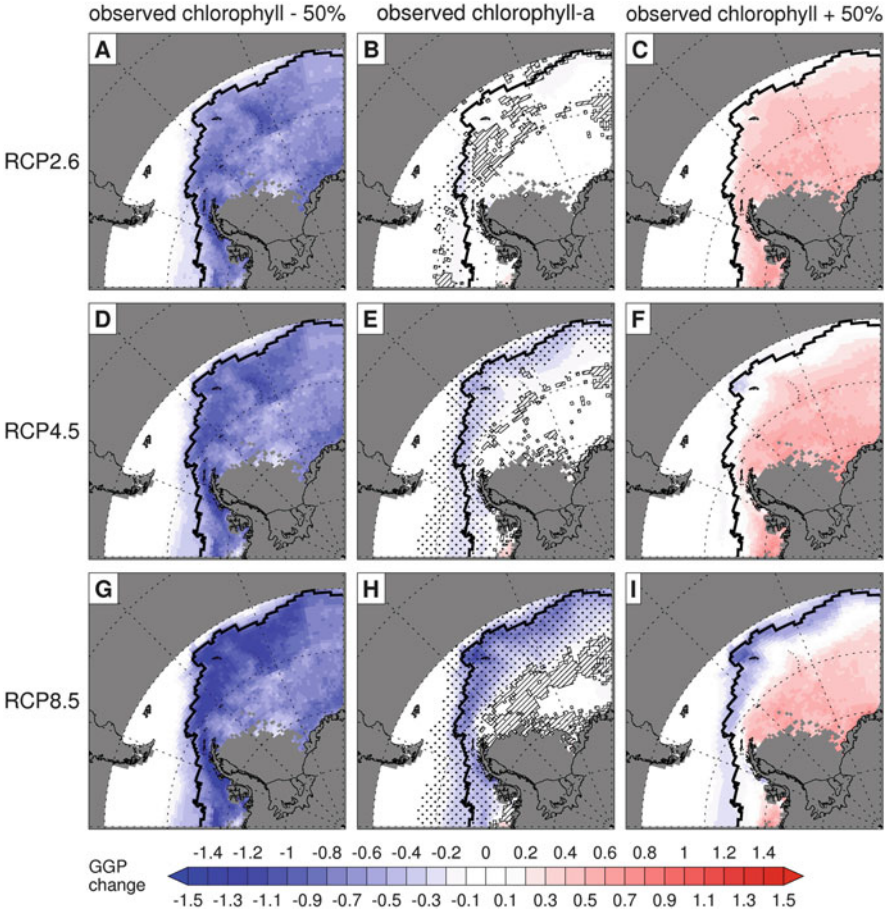


Fig. 5 The results of a study which used projections from multiple climate models to drive a statistical model of Antarctic krill growth [40]. The figure shows the spatial pattern of projected change in gross growth potential (GGP, an indicator of new biomass production) from 1997–2011 to 2070–2099. The growth model represents the influence of both temperature and food availability. The panels are arranged from *top to bottom* in order of increasing projected warming from three different representative control pathways (RCPs, which control the radiative forcing and hence warming in climate models). The figures are arranged from *left to right* in order of increasing final food availability indicated by chlorophyll concentration, including a 50 % decrease and a 50 % increase from current (observed) concentrations. Additionally, the central column shows the degree of agreement between climate models: Cells where 50 % or more of the models project significant GGP change are highlighted with stippling if 90 % or more of models agree on the sign of the change, and are *highlighted* with *hatched lines* if fewer than 90 % agree

mathematical tools. As an example, a recent study aimed to estimate the population of emperor penguins, *Aptenodytes fosteri*, using a single synoptic survey in 2009 [31]. The analysts examined the whole continental coastline of Antarctica using

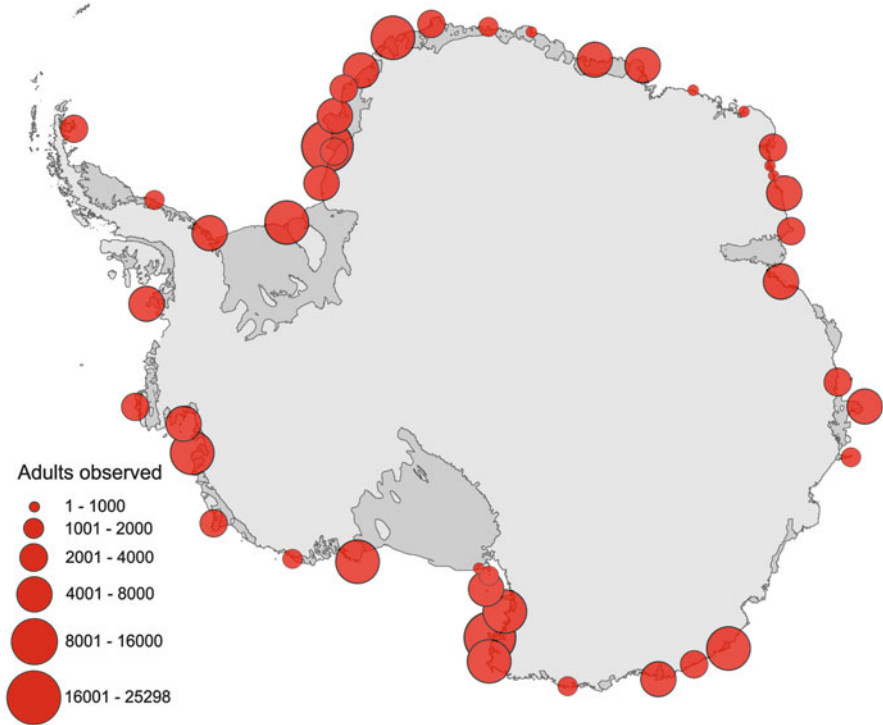


Fig. 6 The location of all known emperor penguin colonies in Antarctica and the estimated number of adults present in each at the time of a 2009 satellite survey [31]

a combination of medium resolution and very high resolution satellite imagery to identify emperor penguin colonies and the area occupied by penguins in each. They obtained actual counts of penguins from eleven ground truthing sites and used robust regression to model the relationship between the number of adult penguins and the area they occupy. They then used the model to estimate of the number of adult penguins at every colony. Finally they scaled this number up to estimate the total population of adults, including those that were absent at the time of the survey, using information about rates of participation in breeding and breeding success (Fig. 6). The final estimate of 238,000 adults present, out of a total population of 595,000 compares with the previously published estimate of 135,000–175,000 breeding pairs [62]. The revised, comprehensive estimate of the total breeding population can be used in population models and will provide a baseline for long-term research [31] which is necessary because global and regional emperor penguin populations are likely to be strongly affected by climate change [8, 50, 98].

In summary, climate research has always depended upon mathematics to build models and implement analyses. These models and analyses have increased our understanding of the past, and are now being used to project future climate

conditions. This is particularly important in the Antarctic where recent changes in some areas are amongst the most extreme on earth. Ecological models are now being linked to climate projections from global climate models, providing a new era of research and bringing disciplines together. Future Antarctic climate research will include foci on characterizing and reducing the uncertainty in model outputs (e.g. by collecting further data and by improving the precision on the variables collected), on improving understanding and representation of climate processes (to improve model performance and the reliability of projections) and on working together with other science disciplines to provide robust evidence on the range of climate impacts, from sea level changes to biodiversity effects, that will inform policy decisions.

6 Final Considerations

Mathematical analyses are crucial in all areas of Antarctic science and central to addressing issues of global importance. In each scientific area highly specific methods and models have been developed to address particular questions, from the detailed analyses of remotely sensed predator tracking data to the assessment of the outputs from multiple climate models to determine the potential impacts of future global climate change. A key issue, that is common to all scientific disciplines, is how to deal with the inherent uncertainty associated with the analysis of process interactions in Antarctic systems. Major uncertainties are often the result of limited data availability, due to the difficulties of operating in remote Antarctic systems. However, over the last decade a series of long-term sampling programmes and large-scale international integrated projects (such as Census of Antarctic Marine Life (<http://www.caml.aq/>), ANDRILL (<http://www.andrill.org>), GLOBEC (<http://www.globec.org/>)), and a rapid increase in the volume of remotely sensed information available, have changed the scale of the data available for analysing these systems. This increase in data availability has led to the development of new methods and algorithms for their efficient collection, validation, storage and analyses. With the continued rapid development of satellite-based and remote observation systems (e.g. ocean drifters and automatic weather stations), and of new methods for genetic analyses of biological systems, a step-change is occurring in the magnitude of data available on all components of Antarctic systems. Dealing with these data will require a similar step-change in the use of mathematics in all aspects of Antarctic science.

Many of the issues of global importance in Antarctic science are at the interfaces between traditional disciplines (e.g. biology and physics or oceans and the cryosphere). In many of these areas new methodological and analytical approaches and models are required. For example, addressing questions about how climate change and direct human impacts (such as fishing) will affect ecosystems requires integrated studies that link knowledge of biogeochemical cycles, species and food webs [68, 69]. This requires integrated whole ecosystem (also termed “end-to-end”) analyses at local (10 s to 100 km), regional (100 s to 100 km) and circumpolar

scales (10,000 s km) [66, 68]. Such whole system integration has become a central focus of international activities in many areas of Antarctic science, and particularly in Southern Ocean studies aimed at linking climate and ecosystem processes [66]. There are major theoretical and analytical challenges in developing such integrated analyses and models. These include questions about how different physical, chemical and biological processes link across a range of scales [67], how different model structures can be coupled together to ensure appropriate feedbacks and system behaviour [68] and how to control and characterize the uncertainty that often multiplies as models integrate more processes [44]. This will require the development of a wide range of new and innovative mathematical approaches.

Acknowledgements We thank Alberto Pinto and his team for organizing such an excellent conference in bringing scientists from a wide range of research disciplines during the year on “Mathematics for Planet Earth”. We also thank Janet Silk and Peter Fretwell for preparing Figs. 2 and 6 respectively. This work has the support of the Ministry of Science and Higher Education in Portugal (Fundação para a Ciência e a Tecnologia) and the research programs CEPH, SCAR AnT-ERA, PROPOLAR and ICED. It is a contribution to the British Antarctic Survey programmes Ecosystems and Climate which are funded by the Natural Environment Research Council.

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Mathematics of Energy and Climate Change
International Conference and Advanced School Planet
Earth, Portugal, March 21-28, 2013

Bourguignon, J.-P.; Jeltsch, R.; Pinto, A.A.; Viana, M.
(Eds.)

2015, XVI, 430 p. 120 illus., 78 illus. in color., Hardcover
ISBN: 978-3-319-16120-4