

Contents

1	Introduction	13
2	Basic cryptosystems	19
2.1	Goals of cryptography	20
2.2	Advanced Encryption Standard (AES)	22
2.3	The AES key schedule	34
2.4	Asymmetric vs. symmetric cryptography	37
2.5	The RSA cryptosystem	38
2.6	The Diffie-Hellman key exchange	42
2.7	Block ciphers	48
2.8	Stream ciphers and modes of operation	50
2.9	Secret sharing	51
2.10	Visual cryptography	53
	Notes	54
	Exercises	56
A	Classical cryptology	61
A.1	Cryptographic primitives	61
A.2	Brief history of cryptography	69
A.3	Simple substitutions	85
A.4	Frequency analysis	87
A.5	Information theory	95
	Notes	103
	Exercises	105
3	The RSA cryptosystem	109
3.1	Analysis of RSA	109
3.2	Primality testing	110
3.3	Finding prime numbers	118
3.4	Finding safe prime numbers	121
3.5	Security of RSA	123
3.6	The Wiener attack	127

3.7	Chinese remainder computation for RSA	128
3.8	Fault attacks	129
3.9	Hard core bit for RSA	130
3.10	Factoring integers	131
3.11	The birthday paradox	132
3.12	Pollard rho with Floyd's trick	133
3.13	Dixon's random squares	136
3.14	Factorization via element order	140
	Notes	143
	Exercises	145
B	Key addition and modular arithmetic	157
B.1	Key addition systems	157
B.2	Claude Comiers d'Ambrun	159
B.3	Later work on arithmetic cryptography	162
	Notes	167
4	Group cryptography and discrete logarithms	169
4.1	Groups for cryptography	169
4.2	The ElGamal encryption scheme	174
4.3	Baby-step giant-step algorithm	176
4.4	The birthday attack	178
4.5	The Pollard rho algorithm	179
4.6	Chinese distribution of discrete logarithms	184
4.7	The Pohlig-Hellman algorithm	188
4.8	Index calculus	191
4.9	Arithmetic circuits for discrete logarithms	194
	Notes	200
	Exercises	202
5	Elliptic curves	207
5.1	Elliptic curves as groups	207
5.2	The geometric background	213
5.3	The size of an elliptic curve	217
5.4	Elliptic curve cryptography	219
5.5	Empirical cryptographic security	222
5.6	The NIST curves	225
5.7	Computing the size of an elliptic curve	227
5.8	Division polynomials	230
	Notes	232
	Exercises	234

C	Breaking the unbreakable	241
C.1	Kasiski's attack on Vigenère	241
C.2	Friedman's index of coincidence	250
C.3	Polygram substitutions	254
C.4	Polyalphabetic substitutions	257
	Notes	258
	Exercises	259
6	Differential and linear cryptanalysis	263
6.1	Baby-AES	264
6.2	Differential cryptanalysis	268
6.3	Linear cryptanalysis	279
6.4	Countermeasures and near-optimality of SUBBYTES . .	290
	Notes	295
	Exercises	297
7	Hash functions	301
7.1	Hash functions	301
7.2	A discrete logarithm hash function	306
7.3	Hashing long messages	310
7.4	Time stamps	313
7.5	The MD and SHA hash function families	313
7.6	The SHA-2 hash functions	314
	Notes	314
	Exercises	316
D	Codebooks	321
D.1	Nomenclators 14th century	321
D.2	Codebooks 15th century	324
D.3	Codebooks 16th century	326
D.4	Codebooks 18th century	332
D.5	Commercial codebooks	334
D.6	Unicity distance for codebooks	335
	Notes	342
	Exercises	343
8	Signatures	347
8.1	Digital signatures	347
8.2	ElGamal signatures	349
8.3	Forging ElGamal signatures	351
8.4	Schnorr signatures and the <i>Digital Signature Algorithm</i>	353
8.5	The Gennaro-Halevi-Rabin signature (GHR) scheme . .	357

Notes	359
Exercises	359
9 Security and reductions	369
9.1 When can we consider a system “secure”?	369
9.2 Security of encryption schemes	373
9.3 One-way and trapdoor functions	374
9.4 Perfect security: the one-time pad	375
9.5 Taxonomy of security reductions for signatures	377
9.6 Security of the GHR signature scheme	380
9.7 Security reductions for encryption	384
9.8 ElGamal encryption and decisional Diffie-Hellman	389
9.9 Hofheinz-Kiltz-Shoup (HKS) encryption	391
9.10 Security of HKS	395
Notes	400
Exercises	403
E Steganography	409
E.1 Invisible ink	409
E.2 Steganographic images	414
E.3 Bacon’s biliteral cipher	414
Notes	416
10 Identification and authentication	419
10.1 Identification schemes	419
10.2 Schnorr identification scheme	420
10.3 Okamoto identification scheme	422
10.4 RSA-based identification	425
10.5 Message authentication codes	426
10.6 Authenticated key agreement	428
Notes	429
Exercises	429
F Transposition ciphers	433
F.1 The skytale tale	433
F.2 Columnar transpositions	435
F.3 Breaking a columnar transposition	439
F.4 Grilles	440
Notes	442
Exercises	443

11 Random generation	447
11.1 True random generators	448
11.2 Pseudorandom generators	452
11.3 Distinguishers	456
11.4 Predictors	461
11.5 From short to long generators	470
11.6 The Nisan-Wigderson generator	474
11.7 Construction of good designs	478
11.8 The Blum-Blum-Shub generator	479
Notes	489
Exercises	490
G Some cryptographers	499
G.1 Arab cryptology	499
G.2 Cicco Simonetta	503
G.3 Johannes Trithemius	504
G.4 Marin Mersenne	520
G.5 Athanasius Kircher and Kaspar Schott	521
G.6 John Wallis	523
Notes	524
12 Proof systems and zero knowledge	529
12.1 Interactive proof systems	530
12.2 Zero knowledge	535
12.3 Bit commitment	543
12.4 Computational zero knowledge	545
Notes	549
Exercises	550
H People using cryptography	555
H.1 Interception, Black Cabinets, and Martin Luther	555
H.2 Hernán Cortés	556
H.3 Margaret Kennedy	559
H.4 Christopher Layer	563
H.5 José Martí	571
Notes	572
13 Integral lattices	575
13.1 Lattices and short vectors	575
13.2 Lenstra, Lenstra & Lovász' lattice basis reduction	578
13.3 Cost estimate for basis reduction	582
13.4 Breaking subset sum cryptosystems	588

13.5	Truncated linear congruential pseudorandom generators	595
13.6	Close vectors	604
13.7	The hidden number problem	609
13.8	Security of Diffie-Hellman	613
13.9	The Coppersmith method	616
13.10	Security of leading bits of an RSA prime	621
13.11	Security of leading bits of a secret CRT-RSA exponent .	623
13.12	The complexity of short vector problems	625
13.13	Lattice cryptography: the Regev cryptosystem	627
	Notes	648
	Exercises	651
I	The Zimmermann telegram	661
I.1	Capturing the <i>Magdeburg</i> 's codebooks	661
I.2	The telegram	664
I.3	Transmission and cryptanalysis	669
I.4	The drama unfolds	674
	Notes	677
14	Quantum computation	681
14.1	Qubits	681
14.2	Quantum circuits	687
14.3	The quantum Fourier transform	694
14.4	Polynomial-time integer factorization	699
14.5	Discrete logarithms	707
14.6	Outlook on quantum computation	712
	Notes	714
	Exercises	715
J	ENIGMA, Turing, and COLOSSUS	719
J.1	ENIGMA	719
J.2	Bletchley Park	725
J.3	Rotor cryptanalysis	728
	Notes	733
	Exercises	736
15	The computer algebra toolbox	741
15.1	Addition and multiplication	743
15.2	Homomorphisms and permutations	746
15.3	Division with remainder	748
15.4	The Extended Euclidean Algorithm	750
15.5	Modular inverses	755

15.6	Cost of algorithms and complexity of problems	757
15.7	Worst case vs. average case	760
15.8	The cost of arithmetic	761
15.9	Uniqueness of rational approximations	763
15.10	Polynomial interpolation	765
15.11	The Chinese Remainder Algorithm	766
15.12	Efficient exponentiation	770
15.13	Fermat, Euler, and Lagrange	772
15.14	Squares and the Jacobi symbol	780
15.15	Linear algebra	785
15.16	Finite probability spaces	788
	Notes	796
	Exercises	799
Notation and sources of quotations, images, and ornaments		807
	Notation	807
	Sources of quotations	808
	Sources of images	815
	Sources of ornaments	817
Bibliography		819
Index		863

By this contrivance, the most ignorant person, at a reasonable charge, and with a little bodily labor, may write books in philosophy, poetry, politics, law, mathematics, and theology, without the least assistance from genius or study.

JONATHAN SWIFT (1726)

'Tis pleasant sure to see one's name in print;
A Book's a Book, altho' there's nothing in't.

LORD BYRON (1809)

In these cursory observations we have by no means attempted to exhaust the subject of Cryptography. With such object in view, a folio might be required.

EDGAR ALLAN POE (1840)

Die Kunst stille zu schweigen, geneigter leser, ist gar ein edles Ding; noch edler aber wird meines Erachtens seyn die Kunst redend zu schweigen und solche lehret dich meine alhier in unserer Muttersprache an das Licht gegebene *Cryptographia*, oder Kunst verborgene Brieffe und Schrifften zu machen.¹

JOHANNES BALTHASAR FRIDERICI (1685)

I went into the Army at Fort Devens in Massachusetts and was sorted into the Signal Corps, and so got in the Signal Corps training camp at Fort Monmouth in New Jersey. They took everybody who had no visible talent or aptitude whatsoever for electrical work, or communications in the technological sense, and if they had a certain level of testing score under the Army General Classification Test, bing! Crypt School before you could sneeze.

WILLIAM P. BUNDY (1987)

Will the study of cryptology become an epidemic that even all the government's resources will be unable to stem?

DAVID KAHN (1979)

¹The art of being quietly silent, estimated reader, is a truly noble thing; even nobler is in my view the art of being silent while talking, and this art is taught to you by my *Cryptographia*, or the art of making hidden letters and writings, brought here to the light of day in our mother tongue.

Lectures on Functor Homology

Franjou, V.; Touzé, A. (Eds.)

2015, VI, 149 p. 140 illus., 1 illus. in color., Hardcover

ISBN: 978-3-319-21304-0

A product of Birkhäuser Basel