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Dyadic Walsh Analysis from 1924 Onwards

Walsh-Gibbs-Butzer Dyadic Differentiation in Science

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A Monograph Based on Articles of the Founding

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