

## Chapter 2

# Utility Functions and Radio Resource Allocation

The world of radio resource allocation for wireless communications has had numerous directions relying chiefly on miscellaneous methods from linear algebra, machine learning, queuing theory, and so forth. An overwhelming of QoS-based radio resource allocation works that have been formulated as optimization problems in the realm of linear algebra and leverage application utility functions to define traffic requirements. Thus, a rudimentary familiarity of the application utility functions and optimization theory is consequential to understanding the radio resource allocation mechanisms introduced in this book. In this regard, this chapter presents the background information on material needed to understand the work in this book. Furthermore, a literature survey of the salient radio resource allocation methods is presented in Sect. 2.3 of this chapter. In this chapter

- We provide with the background information on application utility functions as an application QoS modeling measure.
- We present some popular resource allocation formulations in the context of cellular communications systems.
- we introduce fundamentals of the Frank Kelly Algorithm.
- we develop a literature survey on topical research papers about resource allocation in mobile systems.

The rest of this chapter proceeds as follows. Section 2.1 introduces application utility functions; Sect. 2.2 presents resource allocation formulations and presents two prevalent proportional fairness and max-min techniques germane to resource allocation. Section 2.3 illustrates a literature survey about resource allocation in modern cellular communications systems. Formulation of utility functions and QoS appears in recent works such as [1–6]

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## 2.1 Application Utility Functions

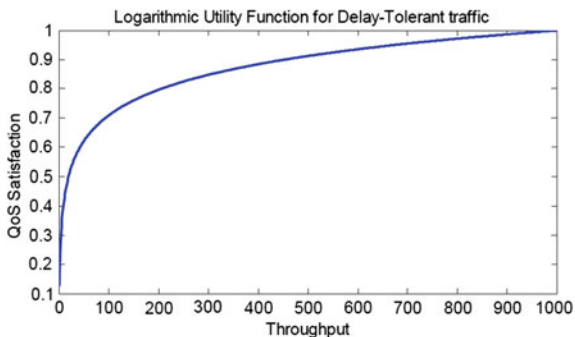
Application utility functions have been used in a wide variety of researches which model characteristic features of the system. For example, [8, 9] leveraged utility functions to model the modulation schemes in a power allocation problem. Additionally, sensors with prespecified utility functions can ensure optimal performance for machine-to-machine communications system [10–15] which outperform conventional schedulers [16–18]. For modern cellular network, resource of applications running on the smart devices should account for QoS requirements for the traffic generated by the running applications. The degree to which the QoS requirements of application traffic are fulfilled can be expressed by the concept of application utility function, which maps a feasible rate allocation to a utility function value that is the QoS fulfillment percentage for that particular application.

There exists little evidence about the precise shape of application utility functions [19–22]; however, we can conjecture about their qualitative behaviors. Traditional applications such as File Transfer Protocol (FTP) and Simple Mail Transfer Protocol (SMTP) applications produce elastic traffic characterized by adapting its rate in the face of congestion and delays in the network [23, 24]. Applications producing such an elastic traffic are delay-tolerant. Intuitively, the QoS satisfaction for delay-tolerant applications has a decreasing marginal return for an increasing rate allocation.

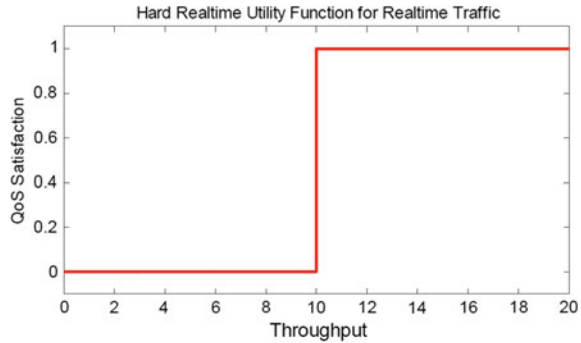
The application utility functions modeling the QoS satisfaction of the elastic traffic generated by delay-tolerant applications look like Fig. 2.1. Here, we can observe a decreasing return in the value of the application utility function as the allocated rate is increased. As we can see, the application utility function is convex everywhere

Other applications like telephony generate an inelastic traffic which needs rate in order to arrive within a given delay bound even though it does not care if the data arrives earlier. The application performs poorly if the data packets arrive later than the delay bound. Such applications, denoted as real-time applications, are mainly those expecting circuit-switched services and ask for a minimum throughput before observing an acceptable performance. The application utility function for the inelastic traffic produced by real-time applications is like Fig. 2.2, from which we can observe

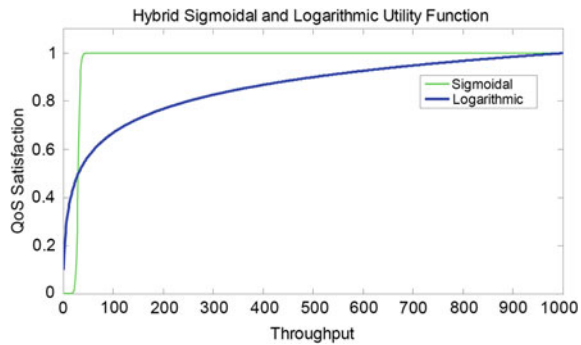
**Fig. 2.1** Utility function  $U(x)$  for delay-tolerant applications versus rate allocation  $x$



**Fig. 2.2** Utility function  $U(x)$  for hard real-time applications versus rate allocation  $x$



**Fig. 2.3** Utility function  $U(x)$  for soft real-time applications versus rate allocation  $x$



so long as the delay bounds are met, the performance is satisfaction almost constant while once the throughput drops below what is required to meet the required delay bounds, the performance plummets to zero sharply.

While audio and video applications have hard requirements, they can be implemented to be rather tolerant of occasional delay/packet loss violations. The intrinsic throughput requirements for real-time applications are due to the fact that the inelastic traffic data generation rate is independent of network congestion. Hence, the QoS performance degrades severely as the share for the application becomes less than the intrinsic generation rate for that traffic. Such soft real-time applications can have utility functions like Fig. 2.3.

Here, the performance satisfaction is mainly constant after meeting the delay bounds whereas it drops close to zero when the application throughput goes below what is needed to meet the delay bounds. In comparison to hard real-time applications, the performance deterioration of the delay-adaptive, real-time application is not as dramatic as the hard real-time application depicted in Fig. 2.2. As we can observe, the shape of the utility is convex in the vicinity of zero and is concave after the minimum throughput for the application is realized. From now on, unless it is explicitly stated, this book refers to an application performance satisfaction as a function of rate as application utility function, which is denoted as  $U(r)$  for the allocated rate  $r$ . Application utility functions have the following main properties [25–27].

- $U(0) = 0$ .
- $U(r)$  is an increasing function  $r$ .
- $U(r)$  is twice differentiable in  $r$ .
- $U(r)$  is upper-bounded.

The first and the second statements of the properties imply the nonnegativity of the application utility functions. This is expected as they represent application performance satisfaction whereas the third and fourth statements reveal the more assigned the rates, the higher the satisfaction for the application performance. On the other hand, the third and fourth predicate indicate that the application utility functions are continuous. A hybrid traffic includes both inelastic and elastic traffic streams emerged from real-time and delay-tolerant applications, whose QoS is conductively modeled by sigmoidal and logarithmic utility functions in Eqs. (2.2) and (2.1) in that order [28, 29].

$$U(r) = c \left( \frac{1}{1 + e^{-a(r-b)}} - d \right) \quad (2.1)$$

Here,  $d = \frac{1}{1+e^{ab}}$  and  $c = \frac{1+e^{ab}}{e^{ab}}$ . It can be verified that  $U(\infty) = 1$  and  $U(0) = 0$ , where the latter is one of the formerly mentioned utility function properties and the former indicates that an infinite resource assignment leads to 100 % satisfaction. Moreover, it can be derived that the inflection point of the function in Eq. (2.1) is at  $r = r^{\text{inf}} = b$  where the superscript “inf” stands for “inflection.” This can be done by differentiating  $U(r)$  with respect to  $r$  twice and setting the second derivative equal to zero, i.e.,  $\frac{\partial^2 U}{\partial r^2} = 0 \rightarrow r = b$ .

Here,  $r^{\text{max}}$  is the maximum rate where the application QoS is satisfied fully (100 % utility) and  $k$  is the utility function increase with increasing the rate  $r$ . It can be investigated that  $U(r^{\text{max}}) = 1$  and  $U(0) = 0$  where the latter is the basic property of the utility functions and the former indicates that a 100 % QoS satisfaction is at  $r = r^{\text{max}}$ . The normalized logarithmic function inflection point occurs at  $r = r^{\text{inf}} = 0$ .

$$U(r) = \frac{\log(1 + kr)}{\log(1 + kr^{\text{max}})} \quad (2.2)$$

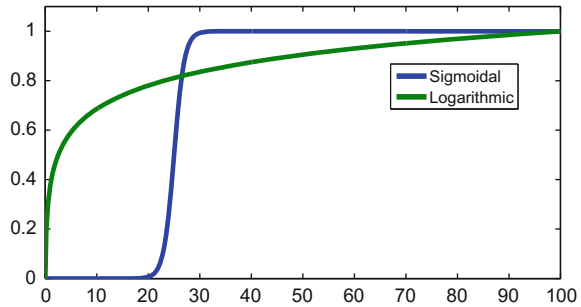
The application utility functions with the parameters in Table 2.1 are considered. Here, the sigmoidal application utility with parameter  $a = 1, b = 25$  estimate another real-time application with the inflection point  $r = 25$  which suites high definition video streaming. Moreover, the logarithmic application utility functions with  $r^{\text{max}} = 100$  and different  $k_i$  parameters approximate delay-tolerant FTP applications.

The application utility functions with parameters in Table 2.1 are shown in Fig. 2.4. We can see that the real-time applications need a minimum rate, which is the inflection point beyond that the application QoS is fulfilled to a large degree. The logarithmic application utility function is provided with certain QoS at low rates appropriate for the delay-tolerant applications. Furthermore, we can see from Fig. 2.4 that the plotted utility functions are strictly increasing continuous functions and are zero

**Table 2.1** Example applications utility function parameters

Applications utilities parameters—diagrams in Fig. 2.4	
Real-time	Sigmoid $a = 1, b = 25$
Delay-tolerant	Logarithmic $k = 15, r^{\max} = 100$

**Fig. 2.4** Delay-tolerant and real-time applications have respectively logarithmic and sigmoidal utility functions  $U_{ij}$  plotted against the application-assigned rates  $r_{ij}$ . Here, the sigmoidal application utility with parameter  $b = 25$  is a good model for high definition video streaming



valued for zero rates. These comply the aforementioned mathematical properties for the application utility functions.

Because sigmoidal utility functions gain a slight QoS satisfaction only after the allocated rates exceed the utility functions inflection points whereas the logarithmic utility functions get some QoS fulfillment even for a small throughput, these behaviors bring about sigmoidal and logarithmic utility functions appropriate models for real-time and delay-tolerant applications QoS satisfaction respectively. Mathematical analyses germane to this matter appear in [28, 30–32] in more details.

Next, Sect. 2.2 explains some points regarding various factors that affect resource allocation formulation.

## 2.2 Resource Allocation Formulations

In the mathematics literature germane to utility functions and resource allocation, a wide variety of formulations have been presented and numerous solutions have been proposed. Amidst various formulations, max-min fairness [33–40] and proportional fairness [41] have received attention as they can yield in optimal and/or efficient solutions [42–44]. Moreover, the authors in [45–47] define a solution to be either Pareto inefficient, Pareto optimal, or infeasible solutions. The last item indicate that an allocation is not feasible based on the resources available and the network demand. However, [45] defined Pareto inefficiency as a rate assignment which does not assign resources and it also defines Pareto optimality as assigning all available resources. In the resource allocation work in Chaps. 3 and 4 of this book, we will be leveraging formulations leading to Pareto optimal solutions.

### 2.2.1 Max-Min Resource Allocation

A feasible resource allocation achieves max-min fairness if an attempt for increasing a rate assignment to an entity in the system leads to reducing the assignment in another entity which do not have more resources than the entity which got more resources. Hence, this method obtains the highest utility value with the lowest values of utility [45, 48, 49]. Using max-min fairness, we can shape the traffic, versus a First-Come First-Serve (FCFS) multiplexing, by not allowing a heavy flow of large packages block serving other flows in the network. In particular, for the utility function  $U(r)$  where  $r$  is the allocated rate, the max-min fairness can be formalized as Eq. (2.3). Water filling [50–52] can be deployed to solve the max-min fairness problems. [33] proved that a max-min fairness policy cannot deal with bottlenecks in the network. Next, we look at the proportional fairness policy for resource allocation.

$$r = \operatorname{argmax}_r \min_r U(r) \quad (2.3)$$

### 2.2.2 Proportional Fairness

A feasible resource allocation achieves proportional fairness if it maximizes the system overall utility while providing with a minimal service to system entities needing resources. This is performed by assigning each flow a rate inversely proportional to its resource need [53, 54]. For the utility function  $U_i(r_i)$ , where  $r_i$  is the allocated rate to the  $i^{\text{th}}$  UE, proportional fairness can be formalized as Eq. (2.4). According to the properties of application utility functions in Sect. 2.1, we see that  $U_i(r_i = 0) = 0$  which zeros the system utility, i.e.,  $\prod_{i=1}^N U_i(r_i)$ . So, no UE will be assigned a zero rate under this formulation. Various methods of solving proportional fairness optimizations have been introduced in literature and the salient of them are the Weighted Fair Queuing (WFQ) [55–57] and Frank Kelly algorithm [58]. Frank Kelly algorithm is an iterative that allows UEs bid for resources until the algorithm reaches optimal allocation and the shadow price (amount of consumed resources per data bit) [58]. On the other hand, proportional fairness can be obtained by setting the inverse shadow price as the weights used for the WFQ. We will be using a proportional fairness formulation for our radio resource allocation work presented in Chaps. 3 and 4. However, we would tailor the formulation to include UE priorities and application temporal usage percentages in addition to the application utility function constituents which represent the traffic.

$$r_i = \operatorname{argmax}_{r_i} \prod_{i=1}^N U_i(r_i) \quad (2.4)$$

### 2.2.3 Frank Kelly Algorithm

Frank Kelly algorithm was a seminal work to achieve proportional fairness and was introduced in [58]. [58] proved that their method brings about Pareto optimal resource allocation for a proportional fairness formulation. In accordance to [58], the procedure commences as UEs send their bids  $w_i$  to a resource allocation manager entity that obtains the shadow price as addition of the bids averaged on the whole resources  $R$  available for the manager entity, i.e.,  $p = \frac{\sum_i^N w_i}{R}$ . The bids to the shadow price ratio,  $r_i = \frac{w_i}{p}$ , derives the rates. Next, users check whether the rate are optimal by solving  $r_{i, \text{texopt}} = \arg \max_{r_i} (U_i(r_i) - pr_i)$  and if  $r_i \neq r_{i, \text{opt}}$ , they transmit new bids  $w_i = r_{i, \text{opt}} p$  to the resource allocation manager and the procedure iterates until a convergence occurs; that is the utility function derivative equals the shadow price  $\frac{\partial U_i}{\partial r_i} |_{r_i=r_{i, \text{opt}}} = p$  [45, 58]. This procedure is summarized in Algorithm 1. We will be using a method based on the Frank Kelly algorithm to solve the proportional fairness resource allocation formulation that will be developed in Chaps. 3 and 4 of the book.

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**Algorithm 1** Frank Kelly Algorithm
 

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Send initial bid  $w_i (n = 1)$  to the resource allocation managing entity.
loop
  Calculate shadow price  $p(n) = \frac{\sum_i^N w_n}{R}$ .
  Receive shadow price  $p(n)$  from the resource allocation managing entity.
  Calculate allocated rate  $r_i = \frac{w_i(n)}{p(n)}$ .
  Solve  $r_{i, \text{opt}} = \arg \max_{r_i} (U_i(r_i) - p(n)r_i)$ .
  if  $r_i \neq r_{i, \text{opt}}$  then
    Calculate  $w_i = r_{i, \text{opt}} p$ .
    Send the bid  $w_i(n)$  to the resource allocation managing entity.
  end if
end loop

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Next, Sect. 2.3 presents the previous studies about radio resource allocation.

## 2.3 Previous Studies on Resource Allocation

The resource allocation optimization research area has received a significant interest after the seminal network utility maximization study in [58] which assigned UE rates via a utility proportional fairness maximization solved by the Lagrange Multipliers [59]. Soon after, an iterative solution algorithm based on the optimization duality was proposed [60–62]. While the traffic in these early research works had an elastic nature which was common for wired communication systems and are modeled by concave utility functions, the emergence of high-speed wireless networks have

entailed produced an increased usage of real-time applications whose utility functions are non-concave [25]. For example, the utility of a VoIP application can be modeled as a step function whose utility is zero before a threshold rate and achieves 100 % for rates larger than the threshold. Another example is a video streaming application for which the utility function is a sigmoidal function convex/concave for rates below/above its inflection point. As such, the approaches presented in [58, 60] have the proceeding drawbacks: (a) Reaching optimal solutions for concave utility functions, these are not applicable to the escalating inelastic traffic volume of modern networks; (b) Neither do they render any priority to real-time applications with stringent QoS requirements, nor they give any attention for the application usage changes, nor they attend to subscribers varied importance which pivotal from a business standpoint.

Later, the authors in [28, 63, 64] introduced distributed rate allocation algorithms based on concave and sigmoidal utility functions representing applications. Despite approximating optimal solution closely, the proposed methods dropped UEs to maximize the system utility and could not guarantee a minimal QoS. The authors in [65–67] proposed a utility proportional fairness resource allocation for a single carrier communications system and cast the formulation as a convex optimization with logarithmic and sigmoidal utility functions modeling delay-tolerant and real-time applications respectively. Even though their schemes prioritized the real-time applications over the delay-tolerant applications, they neither considered the application status or UE differentiation treatments, nor they regarded the hybrid traffic common in modern communications networks.

The authors in [68, 69] and [70–72] considered a similar multicarrier optimal resource allocation aware of the subscriber priorities. However, no attention was rendered to the temporal changes in the application usage or UE quantities. In [73], the authors adopted a non-convex optimization formulation to maximize the system utility in wireless networks consisting of applications with logarithmic and sigmoidal utility functions. A distributed process was employed to obtain the rates under a zero duality gap; but, the algorithm did not converge for a positive duality gap leading to compounding a heuristic to ensure the network stability. In [45], the author considered a weighted aggregation of logarithmic and sigmoidal utilities approximated to the nearest concave utility function via a minimum mean-squared error measure inside UEs. The approximate utility function solved the rate allocation optimization through a variation of the conventional distributed resource allocation approach in [58] such that rate assignments essentially estimated optimal ones. However, the rate were only approximations and no consideration was given to user or application priorities. This work was extended by Shajaiah et al. [74, 75] to allow for the application of the resource allocation in a multicarrier network in public safety.

In a similar work [76–78], the authors proposed a utility proportional fairness optimization which assigned optimal UE rates in a cellular infrastructure coexistent with radars by leveraging the Lagrange multipliers. [79–82] presented a subcarrier allocation in orthogonal frequency division multiplexed systems focusing on delay constrained data and leveraged network delay models [83–85] for the subcarrier assignment. The authors of [86, 87] created a utility max-min fairness for the



hybrid traffic which share a single path in a communications network. Similarly, [30, 88, 89] presented a utility proportional fairness optimization for the high signal-to-interference-plus-noise ratio (SINR) wireless networks using a utility max-min formulations, contrasted against the proportional fairness algorithms [90–93] and gave a closed-form solution that eschewed from network oscillations. However, neither methods cared for any traffic or user priorities in assigning the spectrum. In [7, 94, 95], the authors created a utility proportional fairness resource block allocation as an integer optimization problem. They obtained the continuous optimal rates and then took on a boundary mapping technique to extracted a pool of valid resource blocks tantamount to inferred optimal continuous rates, albeit neither hybrid traffic, nor application status, nor user importance was accounted for. The authors of [96] investigated the WiMAX-radar mutual interference and concluded that large geographic separations between the two systems are required, precluding WiMAX deployability in the coastline. Cotton et al. [97–102] performed tests, using a shipborne radar in San Diego littoral waters, measuring the temporal band occupancy and found that the 3.5 GHz spectrum is not often occupied by radar transmissions, underlining the potential of the germane band for spectrum sharing. Lackpour et al. [103] suggested a general spectrum sharing scheme based on time, space, frequency, and system-level modifications, inappropriate to real-world implementation. Sanders et al. [104] performed experiments with RF hardlines to observe the interference effects from radar waveforms into a 3.5 GHz LTE base station (BS). They observed the throughput loss and block error rate (BLER) for the LTE system in the UL direction; however, their results were varied as some waveforms did not have any effect on the LTE while others undermined the performance drastically. Neither did they consider any propagation models, nor did they perform any simulation of realistic radar or LTE system. Furthermore, Bjornson has extensively written on resource allocation [105–113], and a lot of theoretical contributions are provided by [64, 114–123, 123–125]. And last but not the least, [87] proposed a context-aware source allocation in cellular networks; but, they did not consider the temporal changes in the application usage percentage, the number of UEs in the system, or subscribers' priority.

## 2.4 Chapter Summary

In this chapter, we introduced the concept of application utility functions and their relationship to satisfying the QoS requirement of various delay-tolerant and real-time applications. We illustrated appropriate mathematical models for the application utility functions of real-time and delay-tolerant applications as respectively sigmoidal and logarithmic utility functions. Furthermore, we explained about prevalent resource allocation frameworks in modern resource allocation studies in cellular systems. We introduced max-min and proportional fairness optimizations as common approaches to resource allocation optimization formulation. And, we provided a literature survey on topical resource allocation works in the context of cellular communications systems.

## 2.5 MATLAB Code

The following code plots the application utility functions given in Fig. 2.4. Lines 1–12 initializes the parameters of the application utility functions according to Table 2.1. This code requires the Symbolic Toolbox of MATLAB. If the reader does not have access to this toolbox, you should declare  $x$  as a vector such as  $x = 0.1 : 1000$ ; and eliminate “syms  $x$ .”

```

1 syms x
2 k = 15;
3 a = 1;
4 b = 25;
5 c = (1 + exp(a .* b)) ./ (exp(a .* b));
6 d = 1 ./ (1 + exp(a .* b));
7 s
8 %%%Application Utility Functions%%%
9 for i = 1: length(a)
10
11     % Sigmoid utility function
12     y(i) = c(i).*(1./(1+exp(-a(i).*(x-b(i))))-d(i));
13
14     % Logarithmic utility function
15     y2(i) = log(k(i).*x+1)./(log(k(i).*100+1));
16     m(i) = exp(-a(i).*(x-b(i)));
17     dy_log(i) = k(i)./((1+k(i).*x).*log(1+k(i).*x));
18 end
19
20 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Plot%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
21 yy(1) = 0;
22 yy2(1) = 0;
23 for j = 2:1: 1000
24     x0(j) = 0.1 * j ;
25     yy(j) = subs(y(i),x0(j));
26     yy2(j) = subs(y2(i),x0(j));
27 end
28 plot(x0,yy,x0,yy2);
29 legend('Sigmoidal', 'Logarithmic');
```

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