

# Positronium Decay Rates

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## 1. Introduction

In this paper we briefly review all positronium (Ps) decay rate measurements (including those of the excited states and the Ps negative ion) that have been completed to date. The results are compared with theoretical values. The Ps system represents the most rigorous confrontation with theoretical decay rate calculations for any QED system.

2. Measurement of the  $1^3S_1$  decay rate of Ps In a recent publication [1], a new 200 ppm measurement of the vacuum decay rate,  $\lambda_T$  of triplet Ps formed in a gas was presented. The result,  $\lambda_T = 7.0516 \pm 0.0013 \mu s^{-1}$ , represents a factor of four improvement over previous measurements and is in substantial agreement with existing experimental results, the most recent of which are (see bibliography in reference 1)  $7.056 \pm 0.007 \mu s^{-1}$ ,  $7.045 \pm 0.006 \mu s^{-1}$ ,  $7.051 \pm 0.005 \mu s^{-1}$ , and  $7.050 \pm 0.013 \mu s^{-1}$ . These latter values are all 1-2.5 standard deviations above the present theoretical value and the new measurement exceeds theory by 10 experimental standard deviations.

The theoretical value of  $\lambda_T$  may be expressed as the sum of decay rates into three gammas ( $\lambda_3$ ), five gammas ( $\lambda_5$ ), etc.:  $\lambda_T = \lambda_3 + \lambda_5 + \dots$ . The contribution of  $\lambda_5$  has been calculated [2], [3] to be  $\lambda_5 \sim 10^{-6} \lambda_3$ , and is thus negligible. The leading term is:

$$\lambda_3 = \frac{\alpha^6 m c^2}{\hbar} \frac{2(\pi^2 - 9)}{9\pi} \left[ 1 + A_3 \left( \frac{\alpha}{\pi} \right) - \frac{1}{3} \alpha^2 \ln \alpha^{-1} + B_3 \left( \frac{\alpha}{\pi} \right)^2 + \dots \right]. \quad (1)$$

The two most recent calculations give  $A_3 = -10.266 \pm 0.011$  [4] and  $A_3 = -10.282 \pm 0.003$  [5]. The coefficient  $B_3$  is still uncalculated, and one obtains through order  $\alpha^2 \ln \alpha$ ,  $\lambda_3 = 7.03830 \pm 0.00005 \mu s^{-1}$  [ $1 \times (\alpha/\pi)^2$  adds only  $0.00005 \mu s^{-1}$  to  $\lambda_3$ ]. If one assumes that the disagreement between the theoretical and experimental values of  $\lambda_T$  is due

to the  $(\alpha/\pi)^2$  term, then  $B_3 = 340 \pm 33$  is required to bring theory and experiment into agreement. We note here that it may be more appropriate [6] to write the second order term as a coefficient times  $\alpha^2$  rather than  $(\alpha/\pi)^2$ , so that the (still rather large) coefficient of 34 would explain the difference. Exotic, non-QED decay modes of o-Ps have been considered [7], [8] to account for the discrepancy but recent axion searches place severe restrictions on such decays [9].

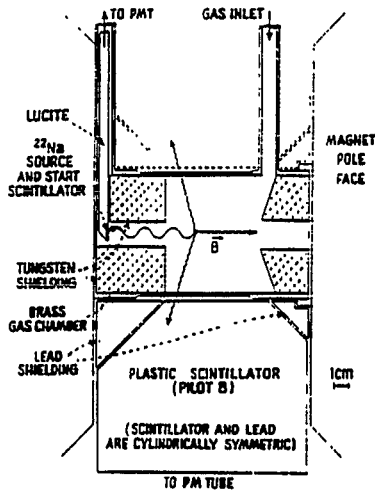


Fig. 1. The gas-filled Ps formation chamber and detector arrangement.

In the experimental technique used in our new measurement [1] Ps is formed in a gas in a magnetic field of 6.8 kG (Fig. 1). The field confines positrons to the axis of the chamber and reduces the  $1^3S_1(m=0)$  lifetime to 13 ns. The  $1^3S_1(m=\pm 1)$  states are unperturbed and continue to decay in the field with a rate,  $\lambda$ , which depends on the particular gas and its density. The decay rate is determined by fitting of the annihilation lifetime spectrum and  $\lambda_T$  is then determined by extrapolating  $\lambda$  to zero gas density. The results of this extrapolation are: isobutane  $7.0524 \pm 0.0013 \mu s^{-1}$ , neopentane  $7.0551 \pm 0.0026 \mu s^{-1}$ , nitrogen  $7.0487 \pm 0.0018 \mu s^{-1}$ , and neon  $7.0501 \pm 0.0023 \mu s^{-1}$  with the weighted average value being  $7.0514 \pm 0.0013 \mu s^{-1}$ . The uncertainty is obtained from the isobutane result with the other gases treated as systematic tests.

The measurement of  $\lambda_T$  has included extensive systematic tests [1]. These include: i) measurement of  $\lambda_T$  to at least  $\pm 0.0026 \mu s^{-1}$  (350 ppm) in four different gases, ii)

use of two independent digital timing systems with, and without, electronic noise rejection, iii) use of different positron source strengths to search for effects related to the signal-to-noise ratio. A detailed discussion of possible systematic errors related to physical effects in the gases has been published [10]. The most important of such effects include: 1) any non-linearities in  $\lambda$  vs. gas density, 2) formation of long-lived excited states of Ps, and, 3) incomplete thermalization of Ps that could result in time dependent collisional quenching ("pickoff") of Ps. With these systematics in mind we have recently performed an extrapolation of  $\lambda$  vs. gas density using only high density (pressure greater than one atmosphere)  $N_2$  and Ne gases where Ps thermalization and excited state quenching should be rapid. Using only our data with  $P > 1$  atmosphere and published [11] high pressure data for  $N_2$  (7-36 atmospheres) and Ne (7-39 atmospheres) we extrapolate to zero density to find  $\lambda_T = 7.0491 \pm 0.0021 \mu s^{-1}$  and  $7.0483 \pm 0.0029 \mu s^{-1}$  respectively. The close agreement of these values with the values measured entirely below two atmospheres is a strong systematic check on the gas related effects mentioned above.

All of the systematic tests [1, 10] to date support the results of reference [1]. The 1900 ppm difference with theory remains unresolved at this time. A new and systematically very different experiment designed to reach  $\sim 100$  ppm accuracy [12] using a slow positron beam with Ps formation in an evacuated cavity is now underway. Results are expected within one year.

3. Measurement of the  $1^1S_0$  Ps Decay Rate There is only one precision measurement of the singlet ground state (parapositronium) decay rate [13] with sufficient accuracy to test the first order radiative connections to  $\lambda_S$ . The singlet decay rate may be expressed as  $\lambda_S = \lambda_2 + \lambda_4 + \lambda_6 \dots$ . Since  $\lambda_4 (\sim 1.5 \times 10^{-6} \lambda_2)$  is small, [3, 14] we need only concentrate on  $\lambda_2$  in the present discussion. The expression [4] for  $\lambda_2$  is:

$$\lambda_2 = \frac{mc^2}{2\hbar} \alpha^5 \left[ 1 + A_2 \left( \frac{\alpha}{\pi} \right) + \frac{2}{3} \alpha^2 \ln \alpha^{-1} + B_2 \left( \frac{\alpha}{\pi} \right)^2 \dots \right] \quad (2)$$

where  $A_2 = -(5 - \pi^2/4) = -2.532$  and  $B_2$  is, as yet, uncalculated. Through order  $\alpha^2 \ln \alpha^{-1}$  the decay rate is  $\lambda_2 = 7.9866 \text{ ns}^{-1}$  [ $1 \times (\alpha/\pi)^2$  would add  $0.0004 \text{ ns}^{-1}$ ].

In the experiment, Ps is formed in isobutane gas in a uniform magnetic field of about 4 kG (the experimental arrangement is almost identical to that shown for  $\lambda_T$  in

Fig. 1). The magnetic field mixes the  $m=0$  triplet and singlet states and, as a result, the  $m=0$  triplet decay rate is increased to

$$\lambda'_T = \frac{1}{1+y^2} \lambda_T + \frac{y^2}{1+y^2} \lambda_S, \quad \text{where} \quad y = \frac{x}{1+\sqrt{1+x^2}}, \quad \text{and} \quad x = \frac{2g'\mu_B B}{h\Delta\nu} \approx \frac{B(\text{kG})}{36.287}. \quad (3)$$

Thus the annihilation lifetime spectrum has two exponential components: the unperturbed decay from the  $m=\pm 1$  states; and the "quenched" decay from the  $m=0$  state (at 4 kG the lifetime is about 30 nsec). Measurement of these decay rates,  $\lambda_T$  and  $\lambda'_T$ , at gas pressures ranging from 200 – 1400 torr allows one, after extrapolation to zero gas density, to solve (3) for  $\lambda_S$ . Measurements were made at three different magnetic fields and the average result is  $\lambda_S = 7.994 \pm 0.011 \text{ nsec}^{-1}$ , in agreement with the  $\lambda_2$  calculation at the 1400 ppm level.

Considering the 1900 ppm difference between the measured value of  $\lambda_T$  and  $\lambda_3$ , it would be interesting to measure  $\lambda_S$  at comparable precision ( $\sim 200$  ppm). The current  $\lambda_S - \lambda_2$  difference is  $(1100 \pm 1400)$  ppm and cannot distinguish such an effect. A measurement at the 200 ppm level would be of immediate interest since the computationally simpler  $B_2$  will probably be calculated before  $B_3$ . We will shortly begin construction of a  $\lambda_S$  experiment that is designed to reach the 200 ppm level of precision.

**4. Measurement of the  $\text{Ps}^-$  Decay Rate** The Ps negative ion, consisting of two electrons and one positron, is a relatively simple system for testing many-electron calculational schemes [15]. There is recently additional interest in measuring the ground state decay rate of  $\text{Ps}^-$ ,  $\Gamma$ , [16] to see if the 1900 ppm discrepancy surrounding  $\lambda_T$  enters into  $\Gamma$  by way of  $\lambda_S$ . Approximately 98% of  $\Gamma$  is given simply by the spin average,  $\Gamma \approx 0.25\lambda_S + 0.75\lambda_T$ . Thus, if there is a sizable discrepancy in  $\lambda_S$  (see previous discussion) it would show up at the same level in  $\Gamma$ .

The best theoretical value [17, 18] of  $\Gamma$  is  $2.0861 \text{ ns}^{-1}$ . This two photon, Hylleras-type calculation also includes order- $\alpha$  corrections for 3-photon annihilation and 2-photon radiative corrections [17].

The  $\text{Ps}^-$  ion was first observed by Mills [19], who has reported the only measurement of  $\Gamma$  to date [20]. In this experiment,  $\text{Ps}^-$  is formed on a thin carbon film and

accelerated by applying a constant potential,  $V$ , to two grids separated by a distance,  $d$ . Measurements of the number of ions reaching the second grid as a function of  $d$  (and hence the proper time since  $\text{Ps}^-$  emission) yields  $\Gamma = 2.09 \pm 0.09 \text{ ns}^{-1}$ . A remeasurement [16] of  $\Gamma$  using an improved variation of this time-of-flight technique is presently underway with the goal of achieving 1000 ppm accuracy.

##### 5. Measurement of the Radiative Decay Rate of Ps in the $2^3\text{P}_J$ ( $J = 0, 1, 2$ ) States

The radiative decay rate  $\gamma$  of  $2^3\text{P}_J$  Ps was measured as a byproduct of an experiment [21] to determine the frequency intervals  $\nu_J$  between the  $2^3\text{S}_1$  and  $2^3\text{P}_J$  states ( $J=0,1,2$ ). The  $2^3\text{P}_J$  states decay to the  $1^3\text{S}_1$  state by emission of a Lyman- $\alpha$  photon at 243 nm. To lowest order in  $\alpha$ , the expected decay rate

$$\gamma = 1/\tau = \frac{5\pi}{64} \alpha^3 \frac{Ry}{h} = 313.8 \mu\text{s}^{-1} \quad (4)$$

is half that for the corresponding transition in hydrogen.

In this experiment Ps in the  $2^3\text{S}_1$  state is irradiated with microwaves of varying frequency and a resonant increase in  $2^3\text{P}_J$  states is observed as the result of stimulated emission. The signature for the  $2^3\text{P}_J$  state is its emission of a Lyman- $\alpha$  photon leaving the Ps in the  $1^3\text{S}_1$  state which subsequently annihilates to three gammas with a lifetime  $\lambda_T^{-1} = 142 \text{ ns}$ .

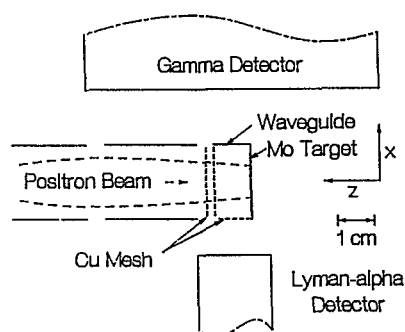


Fig. 2 Experimental Apparatus. (See text for a detailed description.)

A schematic representation of the apparatus [21] is shown in Fig. 2. An electrostatically focused beam ( $10^5 \text{ e}^+/\text{s}$  at 65 eV) enters a section of waveguide ( $2.3\text{cm} \times 1.0\text{cm}$ ) and strikes a polycrystalline molybdenum target attached to the opposite inner wall

of the waveguide. A fraction ( $3 \times 10^{-4}$ ) of the incident positrons is emitted from the target as  $n = 2$  Ps. Assuming equal distribution in all of the  $n = 2$  magnetic substates, 3/16 of them will be in the  $2^3S_1$  state, and 9/16 will be in the  $2^3P_J$  ( $J = 0, 1, 2$ ) states. Lyman- $\alpha$  photons are detected in a solar-blind photomultiplier with an overall detection efficiency of 1%. One or more of the gamma rays from the subsequent annihilation of the  $1^3S_1$  states are detected in two Pilot-B plastic scintillators with a combined detection efficiency of 15%.

In the absence of rf in the waveguide, only those  $2^3P_J$  states originally formed contribute to the signal rate  $R(0, \nu)$  of a Lyman- $\alpha$  photon with a delayed  $\gamma$  ray. As the rf frequency is scanned the signal rate  $R(I, \nu)$  will increase resonantly at the transition frequencies,  $\nu_J$ . The theoretical expression [21] for the ratio  $r \equiv [R(I, \nu) - R(0, \nu)]/R(0, \nu)$  is fitted to data taken in the vicinity of all three transition frequencies and at a variety of rf intensities  $I$ . The results are displayed in Table 1. In addition to the results for the  $\nu_J$ , this fit provides the first measurement of the natural width  $\gamma$  of the  $2^3P_J$  states. The value of  $\gamma$  is taken to be the same for all three  $2^3P_J$  states (in theory the largest difference among the decay rates for different  $J$  states due to their energy splittings is 25 ppm) resulting in an averaged value for  $\gamma$ .

Table 1. Results of fit to  $r$ .  $T$  is the  $2^3S_1$  transit time across the waveguide and  $\gamma$  is the radiative decay rate of  $2^3P_J$  Ps.

| Parameter | Value            | $\sigma_{stat}$ | $\sigma_{syst}$ | Theory             |
|-----------|------------------|-----------------|-----------------|--------------------|
| $\nu_0$   | 18504.1 MHz      | 10.0 MHz        | 1.7 MHz         | 18496.1 MHz        |
| $\nu_1$   | 13001.3 MHz      | 3.9 MHz         | 0.9 MHz         | 13010.9 MHz        |
| $\nu_2$   | 8619.6 MHz       | 2.7 MHz         | 0.9 MHz         | 8625.3 MHz         |
| $T$       | 17.3 ns          | 1.2 ns          | 4.0 ns          | —                  |
| $\gamma$  | $284 \mu s^{-1}$ | $24 \mu s^{-1}$ | $63 \mu s^{-1}$ | $313.8 \mu s^{-1}$ |

The systematic error assigned to  $\gamma$  is due to a simplification in the fitting function used. The fitting function was generated with the assumption that a single time  $T$  described the transit of  $2^3S_1$  Ps across the waveguide, when, in fact, there is an unknown distribution of transit times. Two fits were made with multiple-value distributions (one with two equally likely transit times and the other with a Gaussian distribution of transit times), and the 5 MHz error was accordingly assigned as a conservative estimate of this error.

The result is in good agreement with the theory. The presence of the above systematic error makes the use of this technique to measure  $\gamma$  to better than the  $10 \mu\text{s}^{-1}$  level dependent on detailed knowledge or control of the  $2^3\text{S}_1$  velocity spectrum.

## 6. Summary

The decay rates of Ps discussed in this paper are summarized in Table 2 below.

Table 2. Positronium Decay Rates (Units -  $\mu\text{s}^{-1}$ , Ex=Experiment, Th=Theory)

### n = 1

|   |                                       |
|---|---------------------------------------|
| $\lambda_{\text{Ex}}(1^1\text{S}_0 \rightarrow 2\gamma) \equiv \lambda_{\text{S}} = 7994(11)$   | Gidley, Rich, Sweetman, West (1982)   |
| $\lambda_{\text{Th}}(1^1\text{S}_0 \rightarrow 2\gamma) \equiv \lambda_{\text{S}} = 7986.6(0.1)$  | Caswell, Lepage (1979), Adkins (1983) |
| $\lambda_{\text{Th}}(1^1\text{S}_0 \rightarrow 4\gamma) \sim 1.5 \times 10^{-6} \lambda_{\text{Th}}(1^1\text{S}_0 \rightarrow 2\gamma)$ | Adkins, Brown (1983)                  |
| $\lambda_{\text{Ex}}(1^3\text{S}_1 \rightarrow 3\gamma) \equiv \lambda_{\text{T}} = 7.0514(13)$   | Gidley, Westbrook, Conti, Rich (1987) |
| $\lambda_{\text{Th}}(1^3\text{S}_1 \rightarrow 3\gamma) \equiv \lambda_{\text{T}} = 7.03830(5)$   | Caswell, Lepage (1979), Adkins (1983) |
| $\lambda_{\text{Th}}(1^3\text{S}_1 \rightarrow 5\gamma) = 10^{-6} \lambda_{\text{Th}}(1^3\text{S}_1 \rightarrow 3\gamma)$               | Lepage et al. (1983), Adkins (1983)   |

### n = 2

|   |                              |
|---|------------------------------|
| $\lambda_{\text{Ex}}(2^3\text{P} \rightarrow 1^3\text{S}_1 + h\nu) \equiv \gamma = 284(72)$ | Hatamian, Conti, Rich (1987) |
| $\lambda_{\text{Th}}(2^3\text{P} \rightarrow 1^3\text{S}_1 + h\nu) \equiv \gamma = 313.8$   |                              |

### Ps<sup>-</sup>

|  |                                    |
|--|------------------------------------|
| $\lambda_{\text{Ex}}(1^1\text{S}^e \rightarrow 2\gamma) = 2090(90)$    | Mills (1983)                       |
| $\lambda_{\text{Th}}(1^1\text{S}^e \rightarrow 2\gamma) = 2086.1(0.2)$ | Bhatia, Drachman (1983), Ho (1983) |

## 7. Acknowledgements

This work has been supported by National Science Foundation Grants No. PHY-8403817 and PHY-8605544 and by grants from the office of the Vice President for Research of the University of Michigan.

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