

Asynchronous ASMs

Ring Load Balance

Egon Börger

Dipartimento di Informatica, Università di Pisa

<http://www.di.unipi.it/~boerger>

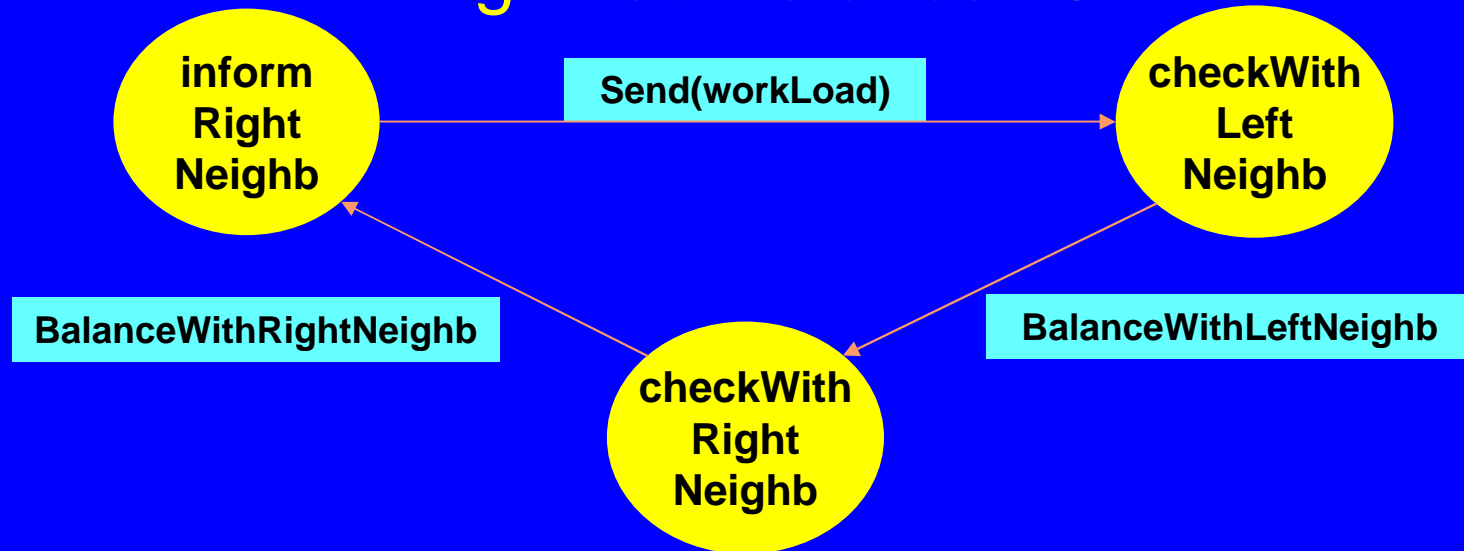
Ring Load Balance: problem statement

- Goal: Design a distributed algorithm for reaching workload balance among the agents of a ring (using only communication between right/left neighbors)
 - keeping message passing mechanism and effective task transfer abstract, assuming fixed number of agents and total workload
- Algorithmic Idea: every agent (ring node)
 - alternately sends
 - a workload info mssg to his right neighbor
 - a task transfer mssg to his left neighbor, transferring a task to balance the workload with the left neighbor
 - updates his workload to balance it with his right neighbor
- so that eventually the difference between the workload of two nodes becomes ≤ 1

Ring Load Balance ASM: Agent Signature

- **Agent** : a ring of agents equipped with:
 - **leftNeighb**, **rightNeighb**: Agent (external functions)
 - **workLoad**: the current workload
 - **neighbLoad**: current workload of leftNeighb
 - **transferLoad**: workload transfered by rightNeighb
 - **ctl_state** : {**informRightNeighb**,
checkWithLeftNeighb , **checkWithRightNeighb** }
- **Initially**
 - **ctl_state** = **informRightNeighb**
 - **neighbLoad** = **transferLoad** = **undef**

Ring Load Balance ASM



BalanceWithRightNeighb °
 If arrived(transferLoad) then
 accept task from rightNeighb

accept task from rightNeighb °
 workLoad := workLoad + transferLoad
 transferLoad := undef

arrived(l) ° l ≠ undef

BalanceWithLeftNeighb °
 If arrived(neighbLoad) then
 transfer task to leftNeighb

transfer task to leftNeighb °
let transfer = workLoad > neighbLoad **in**
 leftNeighb.transferLoad := transfer
 workLoad := workLoad – transfer
 neighbLoad := undef

Send(workLoad) °
 rightNeighb.neighbLoad
 := workLoad

Ring Load Balance ASM : Correctness property

- Proposition: In every distributed run of agents equipped with the ring load balance ASM, eventually the workload difference between two neighboring nodes becomes ≤ 1 .
- Proof (assuming that every enabled agent will eventually make a move): induction on the weight of run workload differences. Let w = total workload of all nodes, $a = |\text{Agent}|$.
 - Case 1: $t \mid a$. Then eventually $\text{workLoad}(n) = w/a$ for every node n .
 - Case 2: otherwise. Then eventually the workload of some neighboring nodes will differ by 1.

Reference

- W.Reisig: Elements of Distributed Algorithms
Springer-Verlag 1998
 - See Section 37 (in particular Fig. 37.1) and Section 82 for a correctness proof.
- E. Börger, R. Stärk: Abstract State Machines. A Method for High-Level System Design and Analysis
Springer-Verlag 2003, see <http://www.di.unipi.it/AsmBook>
 - See Chapter 6.1