

# A

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## CASL Quick Reference

This appendix provides an overview of the (concrete) syntax of each part of CASL.

### *Basic specifications*

- declarations, definitions:
  - sorts, subsorts
  - functions: total, partial
  - constants: total, partial
  - predicates
  - datatypes
  - sort generation constraints
- variables, axioms
  - formulas
  - terms
- symbols
- comments
- annotations

### *Architectural specifications*

- named architectures, units
- architectural specifications
- unit specifications
- unit declarations, definitions
- unit expressions, terms

### *Structured specifications*

- specification structure
  - translation
  - hiding, revealing
  - union, extension
  - free extension, initiality
  - hiding local symbols
  - reference
  - instantiation
- named, generic specifications
  - fitting arguments
- named, generic views
  - fitting views
- symbol lists, maps

### *Libraries*

- named libraries
- downloadings
- library names, versions

## A.1 Basic Specifications

$\dots; \dots$	list of items (‘;’ optional)
<b>sorts</b> $\dots$	sort declarations and definitions
<b>ops</b> $\dots$	operation declarations and definitions
<b>preds</b> $\dots$	predicate declarations and definitions
<b>types</b> $\dots$	datatype declarations and definitions
<b>generated</b> $\{ \dots \}$	sort generation constraint
<b>vars</b> $\dots$	global variable declarations
$\forall \dots \bullet F_1 \dots \bullet F_n$	universally-quantified list of axioms
$\bullet F_1 \dots \bullet F_n$	unquantified list of axioms

### A.1.1 Declarations and Definitions

#### Sort Declarations and Definitions

<b>sort</b> $s$	sort declaration
<b>sorts</b> $s_1, \dots, s_n$	sorts declaration
<b>sorts</b> $s < s'$	subsort declaration
<b>sorts</b> $s_1, \dots, s_n < s'$	subsorts and supersort declaration
<b>sorts</b> $s < s_1; \dots; s < s_n$	subsort and supersorts declaration
<b>sorts</b> $s_1 = \dots = s_n$	isomorphic sorts declaration
<b>sort</b> $s = \{v : s' \bullet F\}$	subsort definition

#### Function Declarations and Definitions

<b>op</b> $f : s_1 \times \dots \times s_n \rightarrow s$	total function declaration
<b>op</b> $f : s_1 \times \dots \times s_n \rightarrow ? s$	partial function declaration
<b>op</b> $f : s \times s \rightarrow s, \textit{assoc}$	associative binary function
<b>op</b> $f : s \times s \rightarrow s', \textit{comm}$	commutative binary function
<b>op</b> $f : s \times s \rightarrow s, \textit{idem}$	idempotent binary function
<b>op</b> $f : s \times s \rightarrow s, \textit{unit } T$	unit term for binary function
<b>op</b> $f : s \times s \rightarrow s, \dots, \dots$	multiple function attributes
<b>ops</b> $f_1, \dots, f_n : \dots$	functions declaration
<b>op</b> $f(v_1 : s_1; \dots; v_n : s_n) : s = T$	total function definition
<b>op</b> $f(v_1 : s_1; \dots; v_n : s_n) : ?s = T$	partial function definition
<b>op</b> $f(\dots v_{i_1}, \dots, v_{i_m} : s_{i_m} \dots) \dots$	abbreviated arguments
<b>ops</b> $\dots; \dots$	multiple declarations/definitions

#### Constant Declarations and Definitions

<b>op</b> $c : s$	constant declaration
<b>op</b> $c : ?s$	partial constant declaration
<b>ops</b> $c_1, \dots, c_n : s$	constants declaration
<b>op</b> $c : s = T$	constant definition
<b>op</b> $c : ?s = T$	partial constant definition
<b>ops</b> $\dots; \dots$	multiple declarations/definitions

## Predicate Declarations and Definitions

<b>pred</b> $p : s_1 \times \dots \times s_n$	predicate declaration
<b>pred</b> $p : ()$	constant predicate declaration
<b>preds</b> $p_1, \dots, p_n : \dots$	predicates declaration
<b>pred</b> $p(v_1 : s_1; \dots; v_n : s_n) \Leftrightarrow F$	predicate definition
<b>pred</b> $p \Leftrightarrow F$	constant predicate definition
<b>pred</b> $p(\dots v_{i_1}, \dots, v_{i_m} : s_i \dots)$	abbreviated arguments
<b>preds</b> $\dots; \dots$	multiple declarations/definitions

## Datatype Declarations

<b>type</b> $s ::= A$	datatype declaration with alternatives
<b>types</b> $s_1 ::= A_1;$ $\dots;$ $s_n ::= A_n$	multi-sorted datatype declaration
<b>generated types</b> $\dots$	generated datatype declaration
<b>free types</b> $\dots$	free datatype declaration

## Alternatives (A)

$f(s'_1; \dots; s'_k)$	total constructor function
$f(s'_1; \dots; s'_k)?$	partial constructor function
$f(\dots f_i : s_i \dots)$	total constructor and selector functions
$f(\dots f_i : ?s_i \dots)$	total constructor, partial selector functions
$f(\dots f_{i_1}, \dots, f_{i_m} : s_i \dots)$	abbreviated selectors
$c$	constant constructor value
$sort\ s$	subsort
$sorts\ s'_1, \dots, s'_k$	subsorts
$A_1 \mid \dots \mid A_m$	multiple alternatives

## Sort Generation Constraints

<b>generated</b> { <b>sorts</b> $\dots$	generated sorts
<b>ops</b> $\dots$	generating operations
<b>preds</b> $\dots$	
<b>types</b> $\dots$	generated sorts
<b>}</b>	and generating constructors

### A.1.2 Variables and Axioms

<b>var</b> $v : s$	global variable declaration
<b>vars</b> $v_1 : s_1; \dots; v_n : s_n$	global variables declaration
<b>vars</b> $\dots v_1, \dots, v_n : s_n \dots$	abbreviated variables declaration
<b>vars</b> $\dots; \dots$	multiple global variable declarations
$\forall v : s \bullet F_1 \dots \bullet F_n$	universally-quantified list of axioms
$\forall v_1, \dots, v_n : s \bullet \dots$	abbreviated quantifications
$\forall \dots; \dots \bullet \dots$	multiple quantifications
$\bullet F_1 \dots \bullet F_n$	unquantified list of axioms

### Formulas ( $F$ )

$\forall \dots \bullet F$	universal quantification on formula
$\exists \dots \bullet F$	existential quantification
$\exists! \dots \bullet F$	unique-existential quantification
$F_1 \wedge \dots \wedge F_n$	conjunction
$F_1 \vee \dots \vee F_n$	disjunction
$F \Rightarrow F'$	implication
$F' \text{ if } F$	reverse implication
$F \Leftrightarrow F'$	equivalence
$\neg F$	negation
<i>true</i>	truth
<i>false</i>	falsity
$p(T_1, \dots, T_n)$	predicate application
$t_0 \ T_1 \ t_1 \dots T_n \ t_n$	mixfix predicate application
$q$	constant predicate
$T = T'$	ordinary (strong) equality
$T \stackrel{e}{=} T'$	existential equality
<i>def</i> $T$	definedness
$T \in s$	subsort membership

### Terms ( $T$ )

$f(T_1, \dots, T_n)$	application
$t_0 \ T_1 \ t_1 \dots T_n \ t_n$	mixfix application
$t_0 \ T_1, \dots, T_n \ t_1$	literal syntax
$c$	constant
$v$	variable
$T : s$	sorted term
$T \text{ as } s$	projection to subsort
$T \text{ when } F \text{ else } T'$	conditional choice

### A.1.3 Symbols

Character set: ASCII (with optional use of ISO Latin-1).

#### Key Words and Signs

Reserved key words (always lowercase):

*and arch as axiom axioms closed def else end exists false fit  
forall free from generated get given hide if in lambda library local  
not op ops pred preds result reveal sort sorts spec then to true  
type types unit units var vars version view when with within*

Reserved key signs:

: ::? ::= = => <=> ¬ . · | |-> \ / \

Unreserved key signs:

< \* × -> ? ! [ ] { }

Key words and signs representing mathematical symbols:

*forall exists exists! not in lambda =e= -> => <=> . · |-> \ / \*  
 $\forall \quad \exists \quad \exists! \quad \neg \in \lambda \quad \overset{e}{=} \rightarrow \Rightarrow \Leftrightarrow \bullet \bullet \mapsto \wedge \vee$

#### Identifiers

Identifiers for sorts and variables are simple words (other than reserved words) possibly containing digits, primes, and *single* underscores:

*Elem Y\_1 Z2' A\_Rather\_Long\_Identifier*

Sort identifiers can also be compound:

*List[Int] Map[Index, Elem]*

Identifier for operations and predicates can moreover be sequences of (unreserved) signs, with any brackets [ ] { } balanced:

$+ - * / \backslash \& = < > [ ] \{ \} ! ? : . \$ @ \# ^ \sim \grave \cdot \times \div \mathcal{L} \odot \pm \P \S ^1 2 3 \cdot \notin \neg \mu |$

or single decimal digits *1 2 3 4 5 6 7 8 9 0*, or single quoted characters *'c'*.

The signs ( ) ; , ‘ ” % are *not* allowed in identifiers, nor are the ISO Latin-1 signs for general currency, yen, broken vertical bar, registered trade mark, masculine and feminine ordinals, left and right angle quotes, fractions, soft hyphen, acute accent, cedilla, macron, and umlaut.

Operation and predicate identifiers can also be compound:

*order[-- < --]*

Function and predicate identifiers can also be infixes, prefixes, postfixes, and general mixfixes, formed from words and/or sequences of signs separated by *double* underscores (indicating the positions of the arguments), with any brackets [ ] { } balanced:

```
--+-- ||--| {[-]} push_onto__ __select1
```

Invisible mixfix identifiers (such as `----`) with two or more arguments are allowed. (Subsort embeddings give the effect of invisible unary functions.)

An operation, or predicate identifier can be compound, with a list of identifiers appended to its final token.

## Literal Strings and Numbers

```
"this is a string" 42 3.14159 1E-9 27.3e6
```

## Library Identifiers

Names of libraries are either paths, e.g.:

```
BASIC/NUMBERS BASIC/ALGEBRA-II
```

or URLs formed from A...ZA...Z0...9\$-@.&+!\*"'(),~ and hexadecimal codes %XX, and prefixed by HTTP://, FTP://, or FILE:///.

Version numbers of libraries are hierarchical: 0, 0.999, 1, 1.0, 1.0.2.

### A.1.4 Comments

```
%% This is a comment at the end of a line...
```

```
...%{ This is an in-line comment }% ...
```

```
...%{ This a comment that might take
      several lines }%
```

```
%[ This is for commenting-out text
```

```
%{ including other kinds of comment }% ]%
```

### A.1.5 Annotations

A label is of the form `%(text)%`.

An end-of-line annotation is of the general form `%word ...` with a space following the word.

A possibly multi-line annotation is of the general form `%word( ... )%` with no space preceding the ‘(’.

## A.2 Structured Specifications

### A.2.1 Specifications (*SP*)

<i>SP</i> with <i>SM</i>	symbol translation
<i>SP</i> hide <i>SL</i>	hiding listed symbols
<i>SP</i> reveal <i>SM</i>	revealing/translating listed symbols
<i>SP</i> <sub>1</sub> and ... and <i>SP</i> <sub><i>n</i></sub>	union
<i>SP</i> <sub>1</sub> then ... then <i>SP</i> <sub><i>n</i></sub>	extension
free <i>SP</i>	free or initial
local <i>SP</i> within <i>SP'</i>	hiding of local symbols
closed <i>SP</i>	self-contained
<i>SN</i>	reference to named specification
<i>SN</i> [ <i>FA</i> <sub>1</sub> ]...[ <i>FA</i> <sub><i>n</i></sub> ]	instantiation of generic specification

### A.2.2 Named and Generic Specifications

spec <i>SN</i> = <i>SP</i> end	named specification ( <b>end</b> optional)
spec <i>SN</i> [ <i>SP</i> <sub>1</sub> ]...[ <i>SP</i> <sub><i>n</i></sub> ] = <i>SP</i> end	generic specification ( <b>end</b> optional)
spec <i>SN</i> [ <i>SP</i> <sub>1</sub> ]...[ <i>SP</i> <sub><i>n</i></sub> ]	generic specification
given <i>SP</i> <sub>1</sub> '', ..., <i>SP</i> <sub><i>m</i></sub> ''	with imports ( <b>end</b> optional)

### Fitting Arguments (*FA*)

<i>SP</i> fit <i>SM</i>	fitting by symbol map
<i>SP</i>	implicit fitting
<i>FV</i>	fitting view

### A.2.3 Named and Generic Views

view <i>VN</i> : <i>SP</i> to <i>SP'</i> = <i>SM</i> end	named view ( <b>end</b> optional)
view <i>VN</i> [ <i>SP</i> <sub>1</sub> ]...[ <i>SP</i> <sub><i>n</i></sub> ]	generic view
: <i>SP</i> to <i>SP'</i> = <i>SM</i> end	( <b>end</b> optional)
view <i>VN</i> [ <i>SP</i> <sub>1</sub> ]...[ <i>SP</i> <sub><i>n</i></sub> ]	generic view
given <i>SP</i> <sub>1</sub> '', ..., <i>SP</i> <sub><i>m</i></sub> ''	with imports
: <i>SP</i> to <i>SP'</i> = <i>SM</i> end	( <b>end</b> optional)

### Fitting Views (*FV*)

view <i>VN</i>	reference to named view
view <i>VN</i> [ <i>FA</i> <sub>1</sub> ]...[ <i>FA</i> <sub><i>n</i></sub> ]	instantiation of generic view

### A.2.4 Symbol Lists (*SL*) and Maps (*SM*)

<i>SY</i> <sub>1</sub> , ..., <i>SY</i> <sub><i>n</i></sub>	lists (maybe with <b>sorts</b> , <b>ops</b> , <b>preds</b> )
<i>SY</i> <sub>1</sub> ↦ <i>SY</i> <sub>1</sub> ', ..., <i>SY</i> <sub><i>n</i></sub> ↦ <i>SY</i> <sub><i>n</i></sub> '	maps (maybe with <b>sorts</b> , <b>ops</b> , <b>preds</b> )
..., <i>SY</i> <sub><i>i</i></sub> , ...	in a map, abbreviates ..., <i>SY</i> <sub><i>i</i></sub> ↦ <i>SY</i> <sub><i>i</i></sub> , ...

## A.3 Architectural Specifications

### A.3.1 Named Architectures and Units

**arch spec**  $ASN = ASP$  **end**                      named arch. spec. (**end** optional)  
**unit spec**  $SN = USP$  **end**                      named unit spec. (**end** optional)

### A.3.2 Architectural Specifications ( $ASP$ )

$ASN$     arch. spec. name  
**units**  $UD_1; \dots; UD_n$  **result**  $UE$               basic arch. spec.

### A.3.3 Unit Specifications ( $USP$ )

$SP$     unit specification  
 $SP_1 \times \dots \times SP_n \rightarrow SP$                       generic-unit specification  
**closed**  $USP$                                       self-contained  
**arch spec**  $ASP$                                       models of arch. spec.

### A.3.4 Unit Declarations and Definitions ( $UD$ )

$UN : USP$                                       unit declaration  
 $UN : USP$  **given**  $UT_1, \dots, UT_n$               importing units  
 $UN = UE$                                       unit definition

### A.3.5 Unit Expressions ( $UE$ )

$UT$     unit term  
 $\lambda UN_1 : SP_1; \dots; UN_n : SP_n \bullet UT$               unit composition

### A.3.6 Unit Terms ( $UT$ )

$UT$  **with**  $SM$                                       symbol translation  
 $UT$  **hide**  $SL$                                       hiding listed symbols  
 $UT$  **reveal**  $SM$                                       revealing/translating listed symbols  
 $UT_1$  **and**  $\dots$  **and**  $UT_n$                       amalgamation  
**local**  $UD_1; \dots; UD_n$  **within**  $UT$               local units  
 $UN$     unit name  
 $UN[UT_1] \dots [UT_n]$                       generic-unit application  
 $UN[UT_1 \text{ fit } SM_1] \dots [UT_n \text{ fit } SM_n]$               with fitting by symbol maps



## A.4 Libraries

**library**  $LN$  ...                      named library of downloadings,  
specifications, views

### A.4.1 Downloadings

**from**  $LN$  **get**  $IN_1, \dots, IN_n$  **end**        downloads listed items  
**from**  $LN$  **get** ...  $IN \mapsto IN'$  ... **end**    renames downloaded items

### A.4.2 Library Names ( $LN$ )

BASIC/NUMBERS                      greatest version registered  
BASIC/ALGEBRA\_II **version**  $0.999$         specified version registered  
HTTP://...                          greatest version unregistered  
HTTP://... **version**  $1.0.2$                 specified version unregistered