

## 52 Cu(HCOO)<sub>2</sub> · 4H<sub>2</sub>O

### 52A Pure compound

#### No. 52A-1 Cu(HCOO)<sub>2</sub> · 4H<sub>2</sub>O, Cupric formate tetrahydrate

(*M* = 225.642; [*D*: 235.70])

|    |  |   |   |   |  |
|----|--|---|---|---|--|
| 1a | Antiferroelectric activity of Cu(HCOO) <sub>2</sub> · 4H <sub>2</sub> O was first reported by Okada in 1965. Antiferromagnetic activity of Cu(HCOO) <sub>2</sub> · 4H <sub>2</sub> O was reported independently by Itoh et al. in 1962 and Kobayashi et al. in 1963. |   |   |   | 65Oka<br>62Ito,<br>63Kob                   |
| b  | phase  | III <sup>c)</sup>   | II <sup>a)</sup>                                  | I <sup>a)</sup>   | <sup>a)</sup> 62Kir1                       |
|    | state  | A <sup>b)</sup> , A <sub>magn</sub> <sup>*)</sup> <sup>c)</sup> | A <sup>b)</sup> , P <sub>magn</sub> <sup>c)</sup> | P <sup>b)</sup> , P <sub>magn</sub> <sup>c)</sup>               | <sup>b)</sup> 65Oka                        |
|    | crystal system   |   |   | monoclinic <sup>d)</sup>  | <sup>c)</sup> 63Kob,<br>62Ito              |
|    | space group  |   |   | P2 <sub>1</sub> /a – C <sub>2h</sub> <sup>5</sup> <sup>d)</sup> | <sup>d)</sup> 54Kir                        |
|    | Θ [K]  | 17 235.5 <sup>a)</sup>  |   |   | <sup>c)</sup> 67Oka                        |
|    | For the deuterated crystal, Θ <sub>I-I</sub> = 245.7 K <sup>c)</sup> .   |   |   |   | <sup>f)</sup> 71Bir                        |
|    | Two different assignments were proposed for the space group of phase II (monoclinic): P2 <sub>1</sub> <sup>f)</sup> and P2 <sub>1</sub> /n <sup>g)</sup> <sup>h)</sup> .   |   |   |   | <sup>g)</sup> 69Sod                        |
|    | Antiferroelectric axis    [010].   |   |   |   | <sup>h)</sup> 73Mak                        |
|    | Transparent, blue. Cleavage plane: (001).  |   |   |   | 65Oka                                      |
|    | Efflorescent.  |   |   |   | 54Kir                                      |
|    | *) The antiferromagnetic phase below 17 K is accompanied by weak ferromagnetism.   |   |   |   | 54Kir                                      |
|    |  |   |   |   | 63Kob                                      |
| 2a | Crystal growth: evaporation or cooling method from aqueous solution.   |   |   |   | 65Oka                                      |
| b  | Crystal form: Fig. 52A-1-001.  |   |   |   |  |
| 3a | Unit cell parameters: <i>a</i> = 8.18(2) Å, <i>b</i> = 8.15(2) Å, <i>c</i> = 6.35(2) Å, β = 101° 5(20)' at RT.   |   |   |   | 54Kir                                      |
| b  | <i>Z</i> = 2 in phase I <sup>a)</sup> , <i>Z</i> = 4 in phase II <sup>b)</sup> .   |   |   |   | <sup>a)</sup> 54Kir<br><sup>b)</sup> 72Kay |
|    | Crystal structure: positional and temperature parameters: Table 52A-1-001, Table 52A-1-002.  |   |   |   |  |
|    | Bond lengths and bond angles: Table 52A-1-003, Table 52A-1-004.  |   |   |   |  |
|    | Projection of crystal structure: Fig. 52A-1-002, Fig. 52A-1-003, Fig. 52A-1-004.   |   |   |   |  |
|    | An approximate structure of phase II has been determined by neutron diffraction technique on the assumption that the space group is P2 <sub>1</sub> /n.  |   |   |   | 72Kay,<br>67Tub                            |
|    | The crystal has a super-structure with the <i>c</i> axis doubled in phase II.  |   |   |   |  |
| 4  | Thermal expansion: Fig. 52A-1-005.   |   |   |   |  |
| 5a | Dielectric constant: Fig. 52A-1-006, Fig. 52A-1-007.   |   |   |   |  |
|    | Dielectric relaxation: Fig. 52A-1-008, Fig. 52A-1-009, Fig. 52A-1-010.   |   |   |   |  |
|    | κ <sub>b</sub> = <i>C</i> /( <i>T</i> – Θ <sub>p</sub> ), where <i>C</i> = 3.2 · 10 <sup>4</sup> K, Θ <sub>p</sub> = 215 K.  |   |   |   | 65Oka                                      |
|    | Phase diagram with regard to <i>p</i> : Fig. 52A-1-011.  |   |   |   |  |
| b  | Nonlinear dielectric properties: Fig. 52A-1-012, Fig. 52A-1-013, Fig. 52A-1-014, Fig. 52A-1-015.   |   |   |   |  |

|     |  |   |
|-----|--|---|
| 6a  | Heat capacity: Fig. 52A-1-016, Fig. 52A-1-017, Fig. 52A-1-018, Fig. 52A-1-019.<br>Transition heat and transition entropy:<br>$\Delta Q_m = 836.0(10) \text{ J mol}^{-1}$ , $\Delta S_m = 3.546(5) \text{ J K}^{-1} \text{ mol}^{-1}$ .<br>For Cu(HCOO) <sub>2</sub> · 4D <sub>2</sub> O: $\Delta Q_m = 936.9(5) \text{ J mol}^{-1}$ , $\Delta S_m = 3.814(2) \text{ J K}^{-1} \text{ mol}^{-1}$ .  | 76Mat<br>76Mat                            |
| b   | Thermal conductivity: Fig. 52A-1-020.  |   |
| 8a  | Elastic compliance and stiffness: Table 52A-1-005; Fig. 52A-1-021, Fig. 52A-1-022.   |   |
| 9a  | Birefringence: Fig. 52A-1-023, Fig. 52A-1-024.   |   |
| 10a | Raman scattering: Fig. 52A-1-025.  |   |
| 11  | Electrical conduction: Fig. 52A-1-026.<br>Protonic conductivity parallel to the water planes (perpendicular to (110)):<br>$\sigma = 4.5(13) \cdot 10^{-15} \Omega^{-1} \text{ m}^{-1}$ at RT.<br>Activation energy: $\Delta U = 54.5 \text{ kJ mol}^{-1}$ ( $T > \Theta_a$ ), $\Delta U = 63.5 \text{ kJ mol}^{-1}$ ( $T < \Theta_a$ ).<br>Protonic conductivity perpendicular to the water layer is small:<br>$\sigma_c \approx 10^{-6} \Omega^{-1} \text{ m}^{-1}$ at RT.<br>Ohmic conductivity at 298 K (protonic): $\sigma_a = 8.5(21) \cdot 10^{-6} \Omega^{-1} \text{ m}^{-1}$ ;<br>$\sigma_b = 5.5(16) \cdot 10^{-5} \Omega^{-1} \text{ m}^{-1}$ ; $\sigma_c = 7(2) \cdot 10^{-6} \Omega^{-1} \text{ m}^{-1}$ .<br>Ohmic and non-ohmic behaviors have been found; for details see | 75Web<br>75Web<br>75Web<br>77Mur<br>77Mur |
| 12  | Magnetic properties: Fig. 52A-1-027, Fig. 52A-1-028, Fig. 52A-1-029, Fig. 52A-1-030.<br>$\Theta_N = 17 \text{ K}$ .  | 63Kob                                     |
| 13a | NMR: Table 52A-1-006, Table 52A-1-007, Table 52A-1-008, Table 52A-1-009;<br>Fig. 52A-1-031, Fig. 52A-1-032, Fig. 52A-1-033, Fig. 52A-1-034.<br>Proton magnetic resonance at 4.2 K [for Cu(HCOO) <sub>2</sub> · 4D <sub>2</sub> O]: see   | 62Kir2,<br>74Mas                          |
| b   | ESR: see   | 68See                                     |

**Table 52A-1-001.** Cu(HCOO)<sub>2</sub> · 4H<sub>2</sub>O. Crystal structure of phase I [54Kir, 66Oka]. Fractional coordinates and temperature parameters. *B* is defined by Eq. (e) in Introduction.

|                                  |          | [54Kir]<br>X-ray    | [66Oka]<br>Neutron diffraction |
|----------------------------------|----------|---------------------|--------------------------------|
| Cu                               | <i>x</i> | 0                   | 0                              |
|                                  | <i>y</i> | 0                   | 0                              |
|                                  | <i>z</i> | 0                   | 0                              |
|                                  | <i>B</i> | 1.35 Å <sup>2</sup> | 1.02(14) Å <sup>2</sup>        |
| C                                | <i>x</i> | 0.238               | 0.237(1)                       |
|                                  | <i>y</i> | 0.270               | 0.269(1)                       |
|                                  | <i>z</i> | 0.018               | 0.024(1)                       |
|                                  | <i>B</i> | 1.35 Å <sup>2</sup> | 1.04(16) Å <sup>2</sup>        |
| O <sub>F</sub> (1) <sup>1)</sup> | <i>x</i> | 0.206               | 0.205(1)                       |
|                                  | <i>y</i> | −0.092              | −0.092(1)                      |
|                                  | <i>z</i> | −0.080              | −0.080(1)                      |
|                                  | <i>B</i> | 1.35 Å <sup>2</sup> | 1.27(16) Å <sup>2</sup>        |
| O <sub>F</sub> (2) <sup>1)</sup> | <i>x</i> | 0.117               | 0.116(1)                       |
|                                  | <i>y</i> | 0.210               | 0.213(1)                       |
|                                  | <i>z</i> | 0.086               | 0.088(1)                       |
|                                  | <i>B</i> | 1.35 Å <sup>2</sup> | 1.34(1) Å <sup>2</sup>         |
| O <sub>W</sub> (1) <sup>1)</sup> | <i>x</i> | 0.423               | 0.430(2)                       |
|                                  | <i>y</i> | 0.399               | 0.401(2)                       |
|                                  | <i>z</i> | 0.647               | 0.641(2)                       |
|                                  | <i>B</i> | 1.35 Å <sup>2</sup> | 1.94(2) Å <sup>2</sup>         |
| O <sub>W</sub> (2) <sup>1)</sup> | <i>x</i> | 0.086               | 0.089(2)                       |
|                                  | <i>y</i> | 0.349               | 0.357(2)                       |
|                                  | <i>z</i> | 0.483               | 0.482(2)                       |
|                                  | <i>B</i> | 1.35 Å <sup>2</sup> | 2.59(22) Å <sup>2</sup>        |

<sup>1)</sup> O<sub>F</sub>: O belonging to formate. O<sub>W</sub>: O belonging to water. Figures in parentheses correspond to those given in Fig. 52A-1-002.

**Table 52A-1-002.** Cu(HCOO)<sub>2</sub> · 4H<sub>2</sub>O. Crystal structure of phase I [75Kay]. Fractional coordinates and temperature parameters. The temperature parameters are defined by Eq. (b) in Introduction.

| Atom                    | <i>x</i>   | <i>y</i>   | <i>z</i>   | <i>b</i> <sub>11</sub> | <i>b</i> <sub>22</sub> | <i>b</i> <sub>33</sub> | <i>b</i> <sub>12</sub> | <i>b</i> <sub>13</sub> | <i>b</i> <sub>23</sub> |
|-------------------------|------------|------------|------------|------------------------|------------------------|------------------------|------------------------|------------------------|------------------------|
|                         |            |            |            | [10 <sup>-4</sup> ]    |                        |                        |                        |                        |                        |
| Copper-Cu               | 0          | 0          | 0          | 35(2)                  | 27(2)                  | 129(4)                 | 1(2)                   | 28(2)                  | -6(2)                  |
| Formate ion             |            |            |            |                        |                        |                        |                        |                        |                        |
| Carbon C                | 0.2387(1)  | 0.2695(2)  | 0.0244(2)  | 54(2)                  | 45(2)                  | 144(4)                 | -7(2)                  | 37(2)                  | -6(2)                  |
| Oxygens OF-1            | 0.2024(2)  | -0.0921(2) | -0.0794(2) | 55(2)                  | 40(2)                  | 198(5)                 | 14(2)                  | 50(2)                  | 19(3)                  |
| OF-2                    | 0.1145(2)  | 0.2119(2)  | 0.0896(2)  | 62(2)                  | 52(2)                  | 183(5)                 | -23(2)                 | 55(2)                  | -23(3)                 |
| Hydrogen H <sub>F</sub> | 0.2037(4)  | 0.6933(4)  | 0.0826(6)  | 190(6)                 | 127(5)                 | 457(13)                | 70(5)                  | 207(7)                 | 106(6)                 |
| Water molecules         |            |            |            |                        |                        |                        |                        |                        |                        |
| OW-1                    | 0.4287(6)  | 0.4006(4)  | 0.6381(4)  | 98(5)                  | 94(5)                  | 156(8)                 | -10(5)                 | 36(5)                  | -17(5)                 |
| OW-2                    | 0.0890(5)  | 0.3596(4)  | 0.4849(6)  | 118(9)                 | 110(8)                 | 202(10)                | -12(7)                 | 55(8)                  | -29(8)                 |
| H-1                     | 0.3107(13) | 0.3920(6)  | 0.5847(8)  | 100(8)                 | 142(8)                 | 200(15)                | -16(11)                | 10(10)                 | -8(8)                  |
| H-2                     | 0.4810(12) | 0.2978(14) | 0.5979(14) | 135(16)                | 136(19)                | 281(27)                | 2(13)                  | 20(13)                 | 21(16)                 |
| H-3                     | 0.4746(10) | 0.4739(8)  | 0.5424(11) | 188(23)                | 103(21)                | 210(43)                | -20(17)                | 41(18)                 | 52(18)                 |
| H-4                     | 0.0880(4)  | 0.3257(4)  | 0.3394(8)  | 149(6)                 | 171(7)                 | 242(11)                | -12(4)                 | 53(7)                  | -29(8)                 |
| H-5                     | 0.0265(12) | 0.4587(9)  | 0.4907(18) | 136(39)                | 111(36)                | 307(28)                | 8(24)                  | 51(25)                 | 33(42)                 |
| H-6                     | 0.2154(69) | 0.3782(35) | 0.5355(50) | 86(52)                 | 157(50)                | 288(83)                | 12(71)                 | -34(66)                | -22(47)                |
| H-7                     | 0.0330(18) | 0.2753(28) | 0.5438(25) | 129(32)                | 132(35)                | 306(48)                | -47(21)                | 89(25)                 | 3(30)                  |

Occupancy parameters  $f_i$  for the hydrogen site H-*i* in the water molecules are assumed as below.  $f_1 = 0.85, f_2 = 1.5 - f_1, f_3 = 0.5, f_4 = 1.0, f_5 = 0.5, f_6 = 1 - f_1, f_7 = f_1 - 0.5$ .

For the hydrogen sites, see Fig. 52A-1-003, Fig. 52A-1-004. See also Fig. 52A-1-002. H<sub>F</sub>: H belonging to formate.

**Table 52A-1-003.** Cu(HCOO)<sub>2</sub> · 4H<sub>2</sub>O. Crystal structure of phase I [75Kay]. Interatomic distances and angles. “Riding correction” is given in brackets for O–H distances. See also Fig. 52A-1-003, Fig. 52A-1-004. Primed atoms are related to unprimed atoms by symmetry operations.

| Bond               |             | Distances [Å]    | Bond                 | Bond angles [°] |
|--------------------|-------------|------------------|----------------------|-----------------|
| Copper octahedron: | Cu–OF(1)    | 1.970(4)         | OF(1)–Cu–OF(2)       | 91.8(2)         |
|                    | Cu–OF(2)    | 1.994(4)         | OF(1)–Cu–OW(1)       | 93.2(2)         |
|                    | Cu–OW(1)    | 2.401(7)         | OW(1)–Cu–OW(1)       | 86.8(2)         |
| Formate ion:       | C–OF(1)     | 1.250(3)         | OF(1)–C–OF(2)        | 122.5(2)        |
|                    | C–OF(2)     | 1.259(3)         | HF–C–OF(1)           | 119.8(2)        |
|                    | C–HF        | 1.093(4) [1.142] | HF–C–OF(2)           | 117.7(2)        |
| Water-1:           | OW(1)–H(1)  | 0.96(1) [0.98]   | H(1)–OW(1)–H(2)      | 107.4(5)        |
|                    | OW(1)–H(2)  | 1.00(2) [1.01]   | H(1)–OW(1)–H(3)      | 107.7(6)        |
|                    | OW(1)–H(3)  | 0.98(1) [1.00]   | H(2)–OW(1)–H(3)      | 96.9(8)         |
| Water-2:           | OW(2)–H(4)  | 0.96(1) [0.98]   | H(4)–OW(2)–H(5)      | 104.8(9)        |
|                    | OW(2)–H(5)  | 0.96(1) [0.97]   | H(4)–OW(2)–H(6)      | 111.8(8)        |
|                    | OW(2)–H(6)  | 1.03(6) [1.05]   | H(4)–OW(2)–H(7)      | 99.5(15)        |
|                    | OW(2)–H(7)  | 0.94(3) [0.96]   |                      |                 |
| Hydrogen bonds:    |             |                  | H(1)–OW(1)---H(3)'   | 110.2(4)        |
|                    |             |                  | H(1)–OW(1)---H(7)    | 109.1(5)        |
|                    |             |                  | H(2)–OW(1)---H(6)    | 105.2(10)       |
|                    |             |                  | H(2)–OW(1)---H(3)'   | 92.9(6)         |
|                    |             |                  | H(3)–OW(1)---H(6)    | 107.8(11)       |
|                    |             |                  | H(3)–OW(1)---H(7)    | 91.0(6)         |
|                    |             |                  | H(6)–OW(1)---H(3)'   | 110.2(9)        |
|                    |             |                  | H(6)–OW(1)---H(7)    | 106.9(9)        |
|                    |             |                  | H(3)'–OW(1)---H(7)   | 87.0(4)         |
|                    |             |                  | H(4)–OW(2)---H(2)    | 105.4(4)        |
|                    |             |                  | H(4)–OW(2)---H(1)    | 101.5(4)        |
|                    |             |                  | H(4)–OW(2)---H(5)    | 114.6(5)        |
|                    |             |                  | H(5)–OW(2)---H(1)    | 111.6(8)        |
|                    |             |                  | H(5)–OW(2)---H(2)    | 106.3(7)        |
|                    |             |                  | H(6)–OW(2)---H(1)    | 121.6(16)       |
|                    |             |                  | H(6)–OW(2)---H(5)'   | 111.5(16)       |
|                    |             |                  | H(7)–OW(2)---H(5)'   | 105.4(7)        |
|                    |             |                  | H(7)–OW(2)---H(1)    | 119.7(8)        |
|                    |             |                  | OW(2)–H(4)–OF(2)     | 165.3(3)        |
|                    | OW(2)–OF(2) | 2.828(8)         |                      |                 |
|                    | H(4)–OF(2)  | 1.886(7)         |                      |                 |
|                    | OW(1)–OW(1) | 2.801(8)         | OW(1)–H(3)–OW(1)     | 175.8(7)        |
|                    | H(3)–OW(1)  | 1.826(6)         |                      |                 |
|                    | OW(2)–OW(2) | 2.739(8)         | OW(2)–H(5)–OW(2)     | 177.2(10)       |
|                    | H(5)–OW(2)  | 1.779(6)         |                      |                 |
|                    | OW(1)–OW(2) | 2.782(8)         | OW(1)–H(1)–OW(2)     | 175.9(4)        |
|                    | H(1)–OW(2)  | 1.822(14)        | OW(1)–H(6)–OW(2)     | 175.7(24)       |
|                    | H(6)–OW(2)  | 1.751(60)        |                      |                 |
|                    | OW(1)–OW(2) | 2.767(7)         | OW(1)–H(2)–OW(2)     | 167.9(6)        |
|                    | H(2)–OW(2)  | 1.785(19)        | OW(1)–H(7)–OW(2)     | 174.6(11)       |
|                    | H(7)–OW(1)  | 1.827(31)        |                      |                 |
|                    |             |                  | H(1)---OW(2)---H(2)  | 120.1(4)        |
|                    |             |                  | H(3)'---OW(2)---H(2) | 104.5(4)        |
|                    |             |                  | H(5)'–OW(2)---H(1)   | 111.0(4)        |
|                    |             |                  | H(1)---OW(1)---Cu    | 113.9(4)        |
|                    |             |                  | H(2)---OW(1)---Cu    | 119.5(4)        |
|                    |             |                  | H(3)---OW(1)---Cu    | 109.7(6)        |

**Table 52A-1-004.** Cu(HCOO)<sub>2</sub> · 4H<sub>2</sub>O. Crystal structure of phase I [75Kay]. Root-mean-square amplitudes of thermal motion of hydrogens along the principal axes and angles between the axes and O–O hydrogen bonds.

| Atom | Amplitude | Angle [deg] |
|------|-----------|-------------|
| H-1  | 0.172(9)  | 14(10)      |
|      | 0.206(6)  | 81(11)      |
|      | 0.223(6)  | 79(12)      |
| H-2  | 0.204(15) | 51          |
|      | 0.213(8)  | 80(30)      |
|      | 0.245(14) | 41(13)      |
| H-3  | 0.149(25) | 22(8)       |
|      | 0.225(8)  | 87(9)       |
|      | 0.254(14) | 69(8)       |
| H-4  | 0.205(5)  | 20(18)      |
|      | 0.218(4)  | 71(18)      |
|      | 0.250(5)  | 89(6)       |
| H-5  | 0.186(28) | 37(42)      |
|      | 0.208(30) | 58(50)      |
|      | 0.252(20) | 73(25)      |
| H-6  | 0.152(50) | 14(30)      |
|      | 0.224(34) | 85(41)      |
|      | 0.268(36) | 77(24)      |
| H-7  | 0.148(29) | 19(15)      |
|      | 0.231(14) | 79(15)      |
|      | 0.258(16) | 75(15)      |

**Table 52A-1-005.** Cu(HCOO)<sub>2</sub> · 4H<sub>2</sub>O. Elastic stiffness [ $\cdot 10^{10}$  N m<sup>-2</sup>] at room temperature [73Kam].

|                  |                 |                  |
|------------------|-----------------|------------------|
| $c_{11} = 4.45$  | $c_{22} = 4.99$ | $c_{33} = 2.11$  |
| $c_{44} = 0.54$  | $c_{55} = 0.71$ | $c_{66} = 2.35$  |
| $c_{12} = 3.41$  | $c_{23} = 1.49$ | $c_{13} = 1.42$  |
| $c_{15} = -0.07$ | $c_{25} = 0.27$ | $c_{35} = -0.29$ |
| $c_{16} = -0.24$ |                 |                  |

**Table 52A-1-006.** Cu(DCOO)<sub>2</sub> · 4D<sub>2</sub>O. Direction cosines of the principal axes of the field gradient tensors at D of formate ions above (D<sub>F</sub>) and below  $\Theta_a$  [D<sub>F</sub>(1) and D<sub>F</sub>(2)] [69Sod].  $X_c \parallel \mathbf{a}$ ,  $Y_c \parallel \mathbf{b}$ ,  $Z_c \parallel \mathbf{c}^*$ .

|       |                    |             | $X_c$      | $Y_c$            | $Z_c$      |
|-------|--------------------|-------------|------------|------------------|------------|
| 291 K | D <sub>F</sub>     | $\phi_{xx}$ | 0.329(84)  | $\mp 0.495(76)$  | 0.805(14)  |
|       |                    | $\phi_{yy}$ | 0.735(36)  | $\pm 0.669(55)$  | 0.111(94)  |
|       |                    | $\phi_{zz}$ | -0.593(6)  | $\pm 0.555(5)$   | 0.584(7)   |
| 153 K | D <sub>F</sub> (1) | $\phi_{xx}$ | 0.267(172) | $\mp 0.544(144)$ | 0.796(41)  |
|       |                    | $\phi_{yy}$ | 0.756(60)  | $\pm 0.630(123)$ | 0.177(183) |
|       |                    | $\phi_{zz}$ | -0.598(5)  | $\pm 0.555(4)$   | 0.579(6)   |
|       | D <sub>F</sub> (2) | $\phi_{xx}$ | 0.357(192) | $\mp 0.507(174)$ | 0.785(25)  |
|       |                    | $\phi_{yy}$ | 0.738(92)  | $\pm 0.668(131)$ | 0.096(206) |
|       |                    | $\phi_{zz}$ | -0.573(4)  | $\pm 0.545(3)$   | 0.612(4)   |

**Table 52A-1-007.** Cu(DCOO)<sub>2</sub> · 4D<sub>2</sub>O. Principal values and asymmetry parameter  $\eta$  of field gradient tensors at D of formate ion above and below  $\Theta_a$  [69Sod].

|       |                    | $eQ\phi_{zz}/h$<br>kHz | $eQ\phi_{yy}/h$ | $eQ\phi_{xx}/h$ | $\eta$    |
|-------|--------------------|------------------------|-----------------|-----------------|-----------|
| 291 K | D <sub>F</sub>     | 155.3(25)              | −84.2(29)       | −71.0(24)       | 0.085(24) |
| 253 K | D <sub>F</sub>     | 157.2(19)              | −82.7(21)       | −74.5(18)       | 0.053(18) |
| 244 K | D <sub>F</sub> (1) | 157.9(17)              | −83.3(21)       | −74.8(19)       | 0.057(16) |
|       | D <sub>F</sub> (2) | 157.2(23)              | −82.5(19)       | −74.7(17)       | 0.050(15) |
| 153K  | D <sub>F</sub> (1) | 161.4(20)              | −83.4(21)       | −77.9(34)       | 0.034(20) |
|       | D <sub>F</sub> (2) | 160.4(17)              | −82.1(20)       | −78.2(17)       | 0.025(16) |

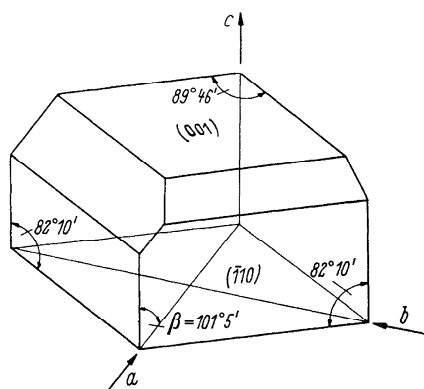
**Table 52A-1-008.** Cu(DCOO)<sub>2</sub> · 4D<sub>2</sub>O. Direction cosines of the principal axes of the field gradient tensors at D of water molecules in phase II at 153 K [69Sod].  $X_c \parallel \mathbf{a}$ ,  $Y_c \parallel \mathbf{b}$ ,  $Z_c \parallel \mathbf{c}^*$ . D<sub>a</sub>...D<sub>h</sub>: D at 8 different sites. For numbering of hydrogen atoms, see [66Oka].

|                |             | $X_c$       | $Y_c$       | $Z_c$       |
|----------------|-------------|-------------|-------------|-------------|
| D <sub>a</sub> | $\phi_{xx}$ | −0.773(66)  | 0.327(67)   | 0.544(133)  |
| D(2)           | $\phi_{yy}$ | 0.395(125)  | 0.424(55)   | −0.815(89)  |
|                | $\phi_{zz}$ | −0.497(6)   | 0.845(3)    | 0.199(9)    |
|                | $\phi_{xx}$ | −0.243(55)  | 0.874(84)   | 0.421(143)  |
| D <sub>c</sub> | $\phi_{xx}$ | −0.243(55)  | 0.874(84)   | 0.421(143)  |
| D(1')          | $\phi_{yy}$ | −0.298(41)  | −0.480(152) | 0.825(74)   |
|                | $\phi_{zz}$ | 0.923(3)    | 0.075(15)   | 0.377(6)    |
|                | $\phi_{xx}$ | −0.054(64)  | 0.038(32)   | 0.998(5)    |
| D <sub>b</sub> | $\phi_{xx}$ | −0.054(64)  | 0.038(32)   | 0.998(5)    |
| D(5)           | $\phi_{yy}$ | 0.853(5)    | −0.519(6)   | 0.066(71)   |
|                | $\phi_{zz}$ | 0.520(5)    | 0.854(3)    | −0.005(10)  |
|                | $\phi_{xx}$ | 0.531(127)  | 0.790(88)   | 0.308(15)   |
| D <sub>e</sub> | $\phi_{xx}$ | 0.531(127)  | 0.790(88)   | 0.308(15)   |
| D(4)           | $\phi_{yy}$ | −0.829(82)  | 0.560(125)  | −0.007(50)  |
|                | $\phi_{zz}$ | −0.178(9)   | −0.252(16)  | 0.951(5)    |
|                | $\phi_{xx}$ | 0.279(34)   | 0.513(111)  | −0.812(59)  |
| D <sub>d</sub> | $\phi_{xx}$ | 0.279(34)   | 0.513(111)  | −0.812(59)  |
| D(1)           | $\phi_{yy}$ | 0.241(36)   | −0.856(66)  | −0.458(106) |
|                | $\phi_{zz}$ | −0.930(3)   | −0.069(15)  | −0.362(7)   |
|                | $\phi_{xx}$ | −0.691(74)  | −0.083(110) | −0.715(59)  |
| D <sub>h</sub> | $\phi_{xx}$ | −0.691(74)  | −0.083(110) | −0.715(59)  |
| D(3)           | $\phi_{yy}$ | −0.495(100) | 0.776(12)   | 0.391(104)  |
|                | $\phi_{zz}$ | 0.523(6)    | 0.625(4)    | −0.580(6)   |
|                | $\phi_{xx}$ | −0.764(60)  | 0.645(69)   | 0.041(34)   |
| D <sub>f</sub> | $\phi_{xx}$ | −0.764(60)  | 0.645(69)   | 0.041(34)   |
| D(4')          | $\phi_{yy}$ | 0.608(76)   | 0.696(59)   | 0.381(18)   |
|                | $\phi_{zz}$ | 0.217(13)   | 0.316(19)   | −0.924(7)   |
|                | $\phi_{xx}$ | 0.073(61)   | 0.539(33)   | −0.839(26)  |
| D <sub>g</sub> | $\phi_{xx}$ | 0.073(61)   | 0.539(33)   | −0.839(26)  |
| D(7)           | $\phi_{yy}$ | −0.828(6)   | −0.437(41)  | −0.352(62)  |
|                | $\phi_{zz}$ | −0.556(5)   | 0.721(3)    | 0.414(7)    |

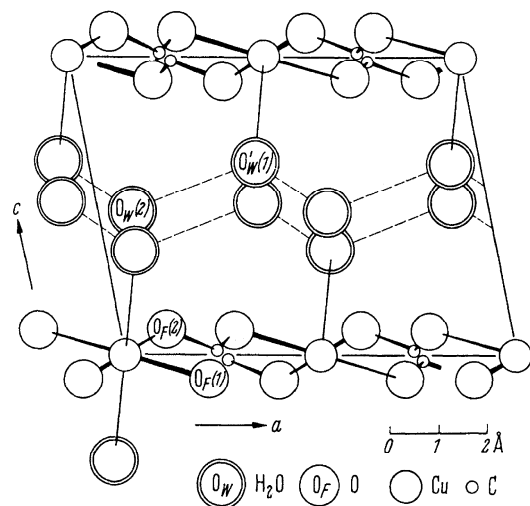
**Table 52A-1-009.** Cu(DCOO)<sub>2</sub> · 4D<sub>2</sub>O.  $|e^2qQ/h|$  and  $\eta$  of D in water molecules in phase II at 153 K. For assignment, see [69Sod]. D<sub>a</sub>...D<sub>h</sub>: D at 8 different sites.

|                | $ e^2qQ/h $<br>[kHz] | $\eta$    | Assignment             |
|----------------|----------------------|-----------|------------------------|
| D <sub>a</sub> | 215.5(37)            | 0.074(20) | D(2)                   |
| D <sub>c</sub> | 216.6(23)            | 0.079(27) | D(1') >O <sub>I'</sub> |
| D <sub>b</sub> | 213.6(36)            | 0.136(21) | D(5)                   |
| D <sub>e</sub> | 220.6(47)            | 0.091(40) | D(4) >O <sub>II</sub>  |
| D <sub>d</sub> | 214.2(23)            | 0.104(28) | D(1)                   |
| D <sub>h</sub> | 214.0(32)            | 0.094(17) | D(3) >O <sub>I</sub>   |
| D <sub>f</sub> | 220.7(43)            | 0.112(36) | D(4')                  |
| D <sub>g</sub> | 215.0(33)            | 0.134(20) | D(7) >O <sub>II'</sub> |

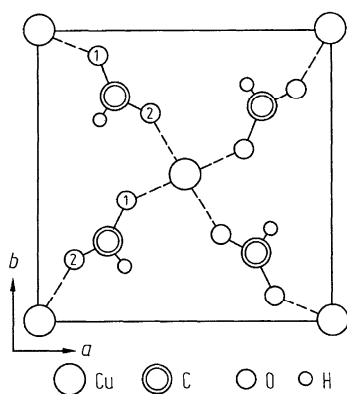




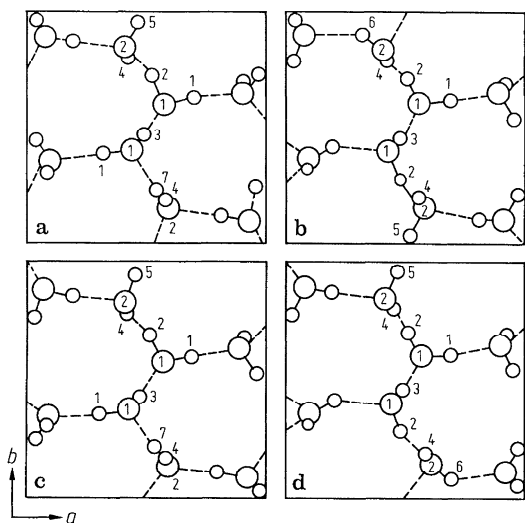
**Fig. 52A-1-001.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ . Crystal form [66Oka].



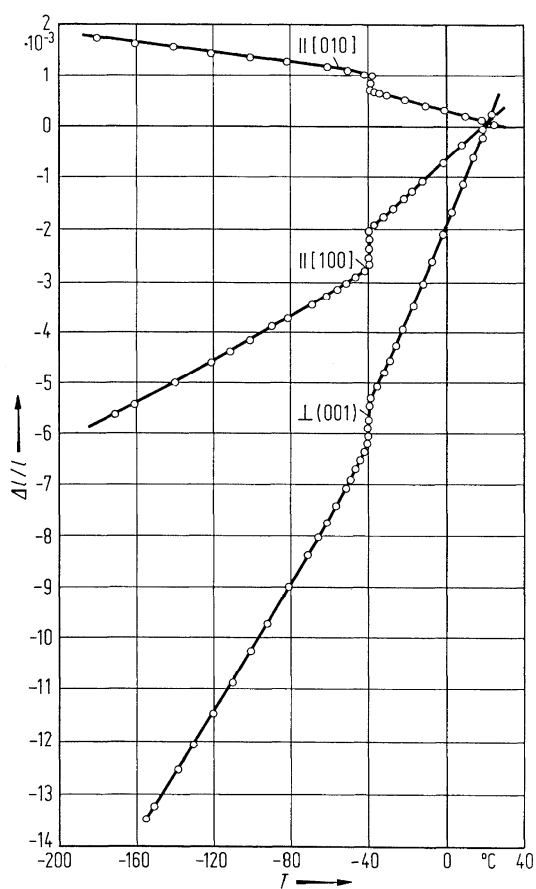
**Fig. 52A-1-002.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ . Crystal structure of phase I [54Kir]. Projection along *b*. Broken lines show the layer of water molecules. O<sub>F</sub>: O belonging to formate. O<sub>W</sub>: O belonging to water.



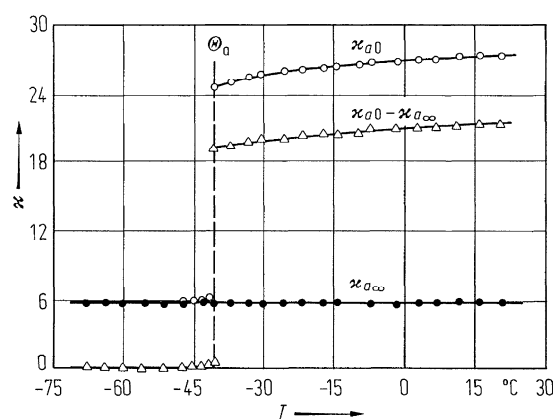
**Fig. 52A-1-003.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ . Crystal structure of phase I [75Kay]. Copper formate layer near *z* = 0.



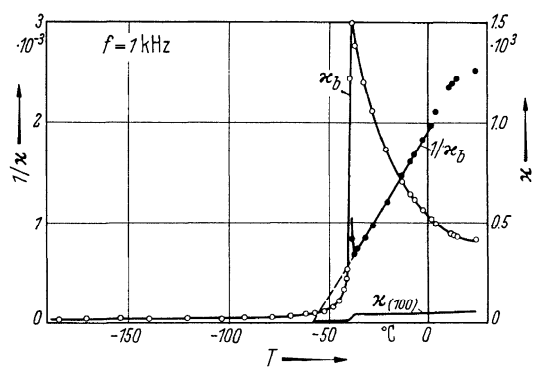
**Fig. 52A-1-004.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ . Crystal structure of phase I [75Kay]. Schematic representation of four possible fully hydrogen bonded water layers. The structures in (a) and (b) probably make up the water layer in the paraelectric phase, although the same occupancies may be derived from (c) and (d). (a) and (b) contain  $2_1$  screw axes and (c) and (d)  $a$  glide planes. The screw axes are retained through the transition. Large circles denote oxygen atoms, small circles hydrogen atoms.



**Fig. 52A-1-005.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\Delta l/l$  vs.  $T \parallel [100]$ ,  $[010]$  and  $\perp (001)$  [68Seo].  $\Delta l/l$ : linear thermal expansion.



**Fig. 52A-1-006.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\kappa_{a0}$ ,  $\kappa_{a\infty}$ ,  $\kappa_{a0} - \kappa_{a\infty}$  vs.  $T$  [78Ham].  $\kappa_{a0}$ ,  $\kappa_{a\infty}$ : dielectric constants along the  $a$  axis at static and high-frequency limit, respectively.



**Fig. 52A-1-007.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\kappa_b$ ,  $1/\kappa_b$ ,  $\kappa_{(100)}$  vs.  $T$  [65Oka].

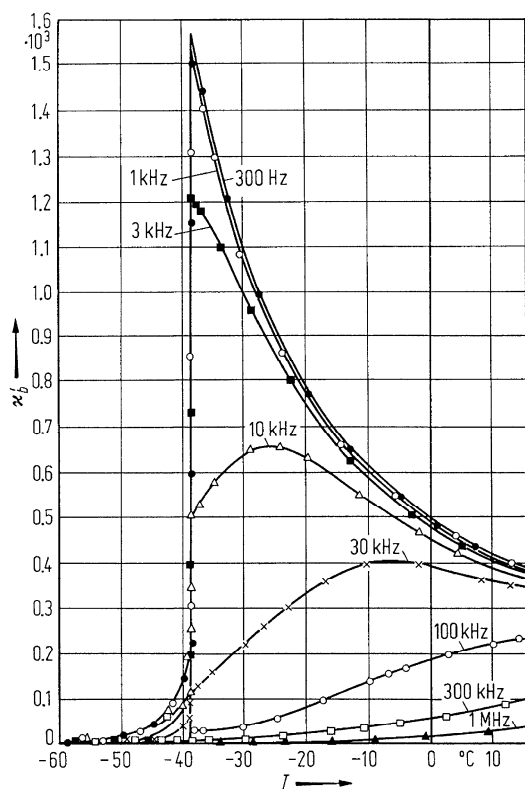


Fig. 52A-1-008.  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\kappa'_b$  vs.  $T$  [69Mak]. Parameter:  $f$ .

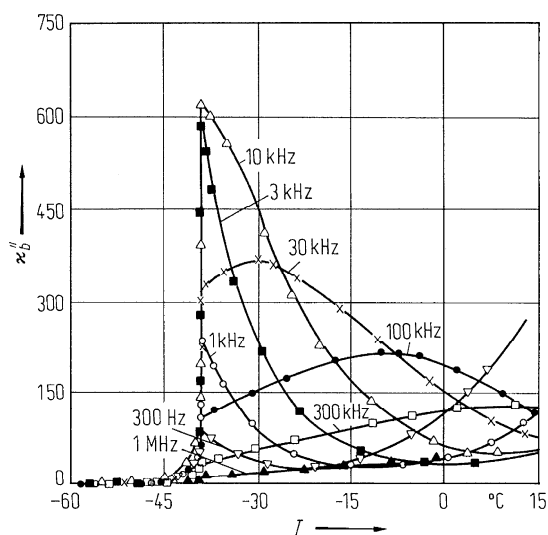
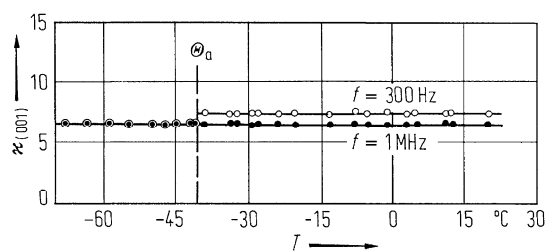
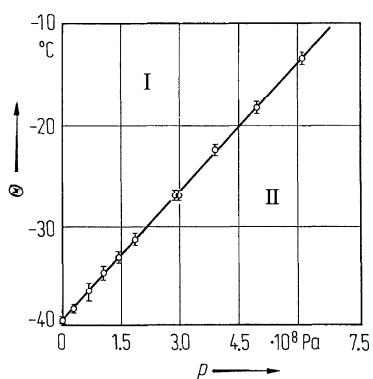


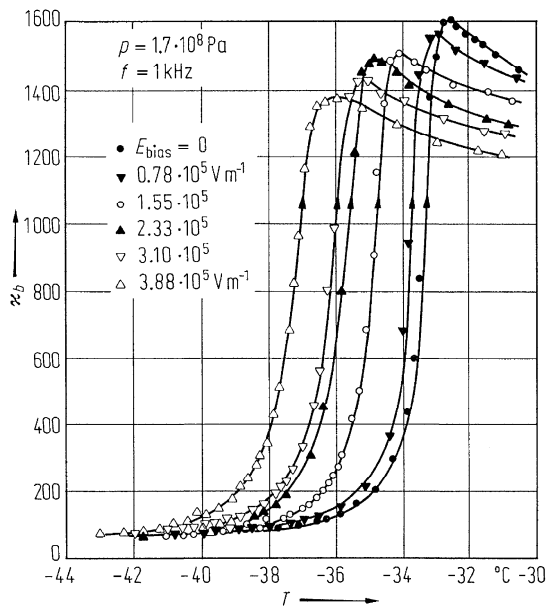
Fig. 52A-1-009.  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\kappa''_b$  vs.  $T$  [69Mak]. Parameter:  $f$ .



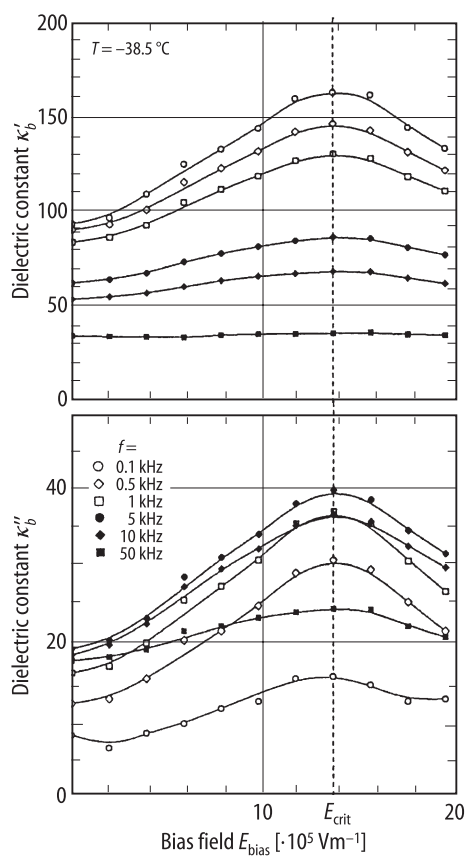
**Fig. 52A-1-010.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\kappa_{(001)}$  vs.  $T$  [78Ham]. Parameter:  $f$ .  $\kappa_{(001)}$ ; dielectric constant for  $E \perp (001)$ .



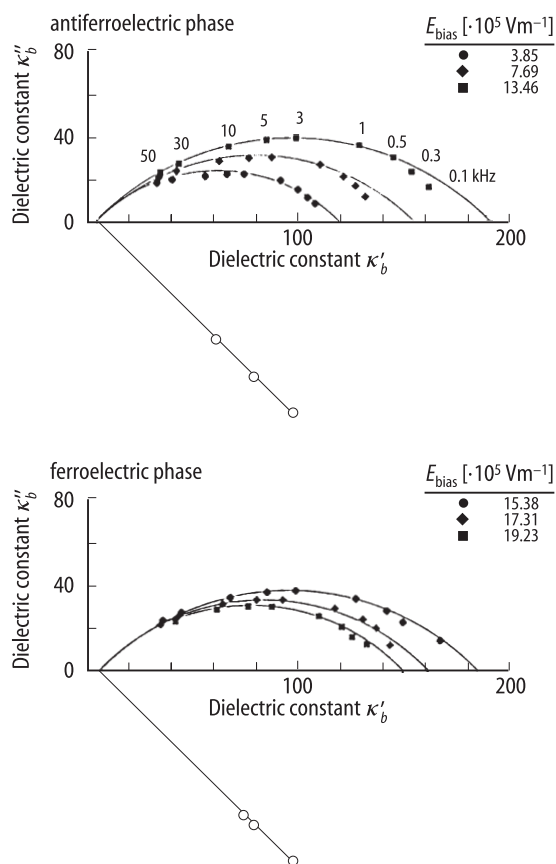
**Fig. 52A-1-011.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\Theta$  vs.  $p$  [73Ges].



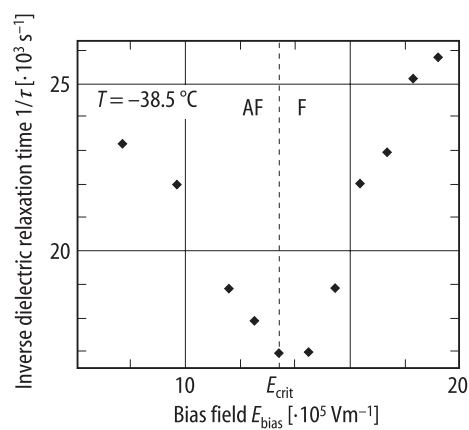
**Fig. 52A-1-012.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\kappa_b$  vs.  $T$  [77Fuj]. Parameter:  $E_{\text{bias}}$ .  $p = 1.7 \cdot 10^8 \text{ Pa}$ .



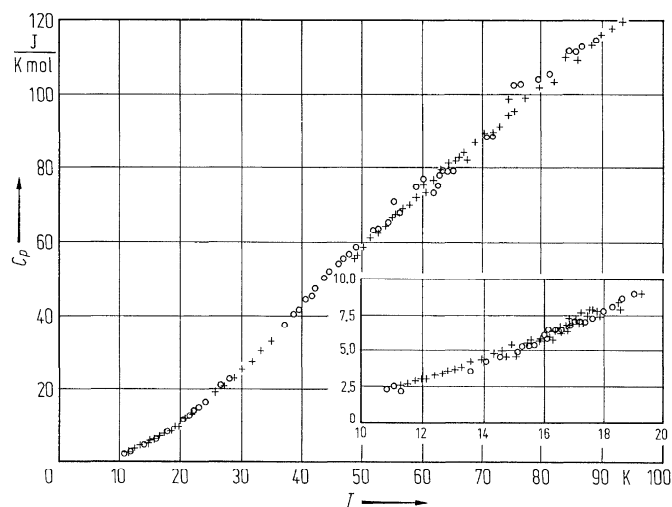
**Fig. 52A-1-013.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\kappa'_b, \kappa''_b$  vs.  $E_{\text{bias}}$  at  $T = -38.5^\circ\text{C}$  [92Yas]. Parameter:  $f$ .  $E_{\text{crit}}$ : transition field from antiferro- to ferroelectric state.



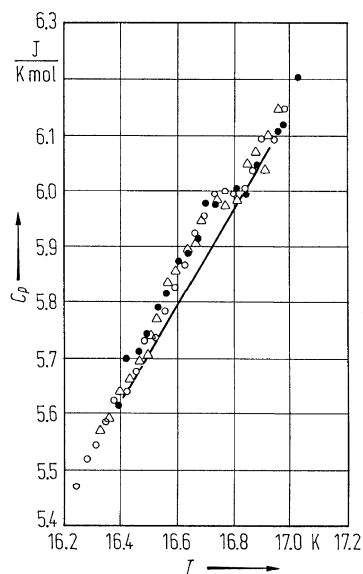
**Fig. 52A-1-014.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ . Cole-Cole diagram of complex dielectric constant [92Yas]. Parameter:  $E_{\text{bias}}$ . Open circle: center of Cole-Cole arc.



**Fig. 52A-1-015.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $1/\tau$  vs.  $E_{\text{bias}}$  at  $T = -38.5\text{ }^\circ\text{C}$  [92Yas].  $\tau$ : dielectric relaxation time.

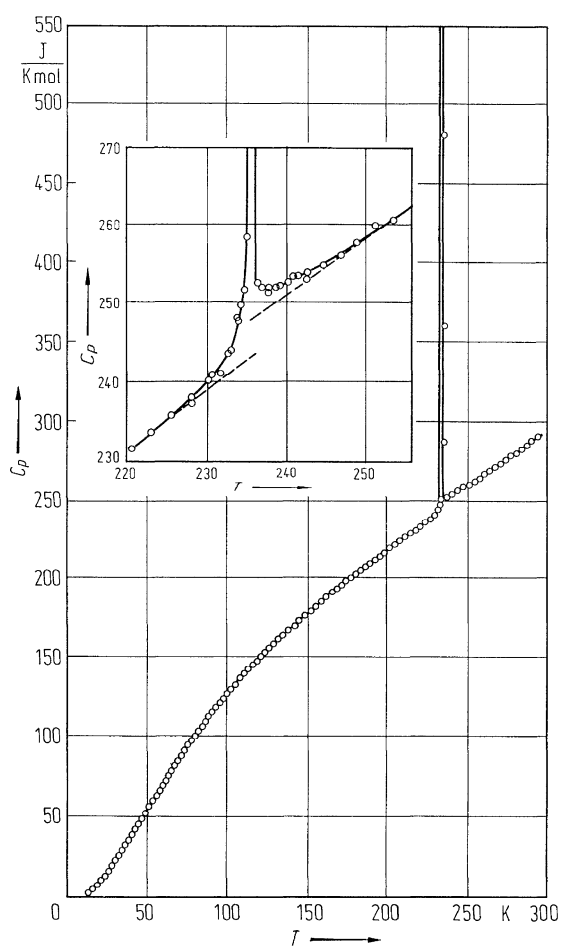


**Fig. 52A-1-016.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $C_p$  vs.  $T$  near the antiferromagnetic Néel temperature [62Ska].  $C_p$ : molar heat capacity at constant pressure.



**Fig. 52A-1-017.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $C_p$  vs.  $T$  [75Yam].  $C_p$ : molar heat capacity at constant pressure. Different symbols correspond to different measurements.





**Fig. 52A-1-018.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $C_p$  vs.  $T$  [76Mat].  $C_p$ : molar heat capacity at constant pressure.

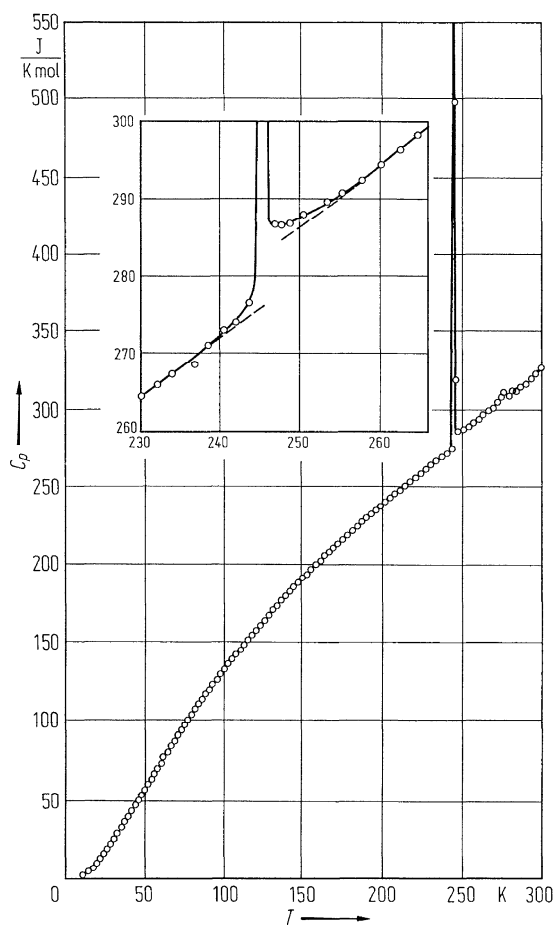


Fig. 52A-1-019.  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{D}_2\text{O}$ .  $C_p$  vs.  $T$  [76Mat].  $C_p$ : molar heat capacity at constant pressure.

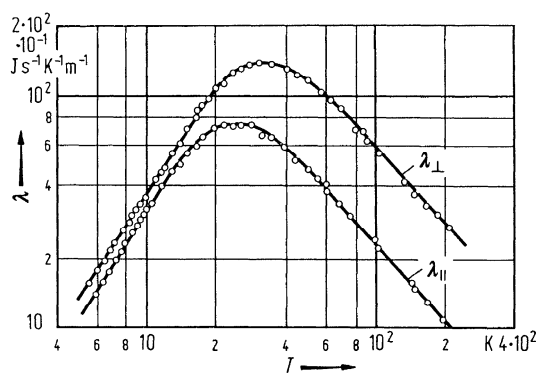
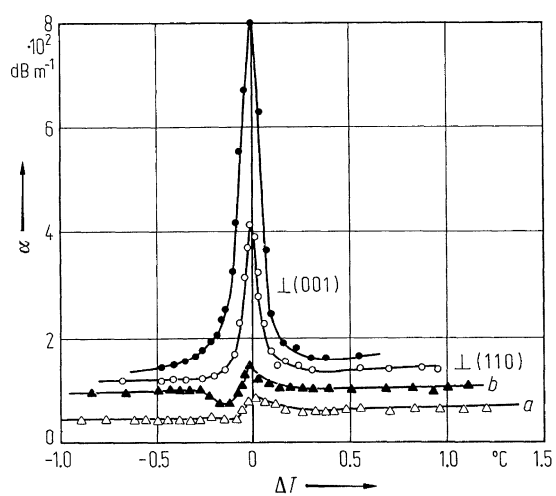


Fig. 52A-1-020.  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\lambda_{\perp}$ ,  $\lambda_{\parallel}$  vs.  $T$  [72Hir].  $\lambda_{\perp}$ ,  $\lambda_{\parallel}$ : thermal conductivity  $\perp$  (001),  $\parallel$  [001], respectively.



**Fig. 52A-1-021.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\alpha$  vs.  $\Delta T$  [73Kam].  $\alpha$ : attenuation coefficients for the longitudinal sound wave propagating along the  $a$  axis, the  $b$  axis, and  $\perp$  to the (110) habit plane and the (001) habit plane.  $\Delta T = T - \Theta_a$ ,  $f = 30$  MHz.

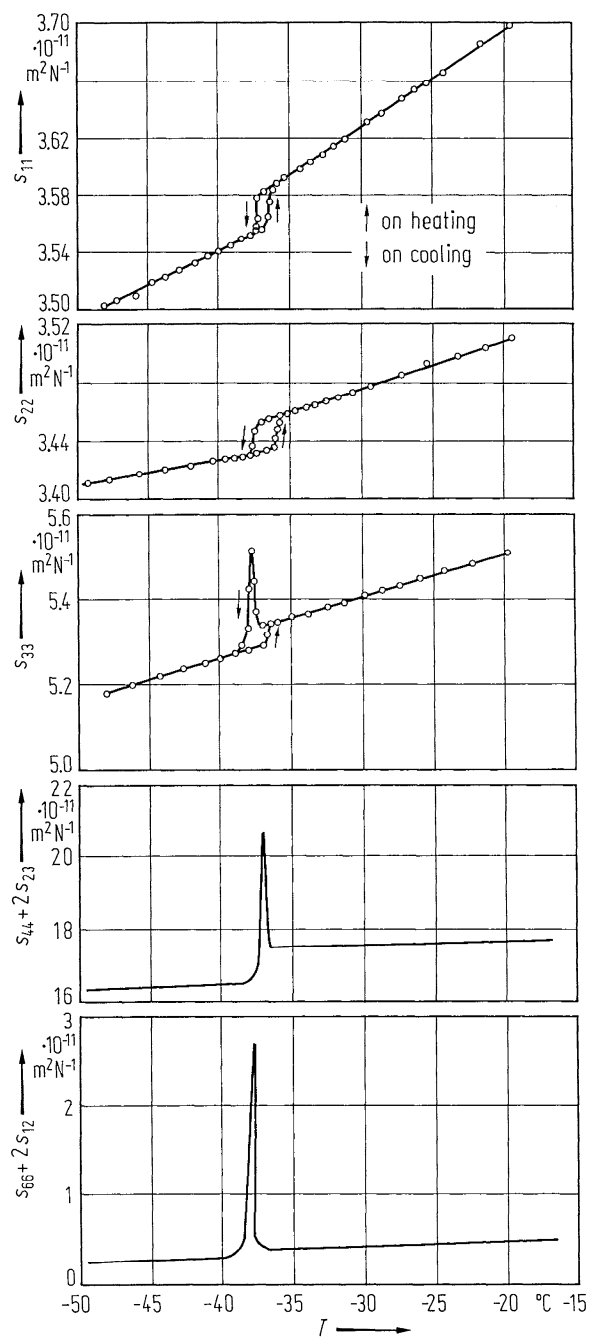
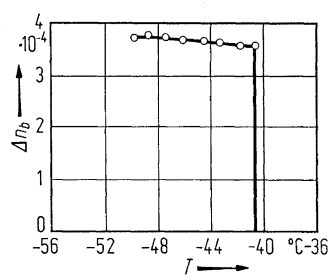
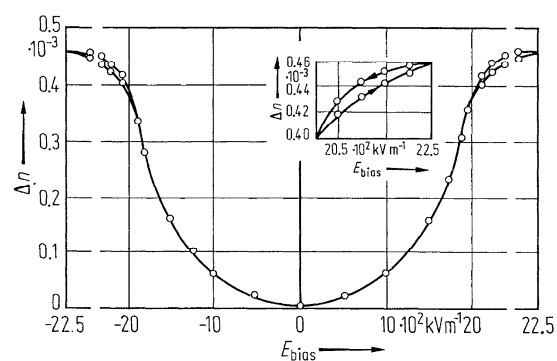


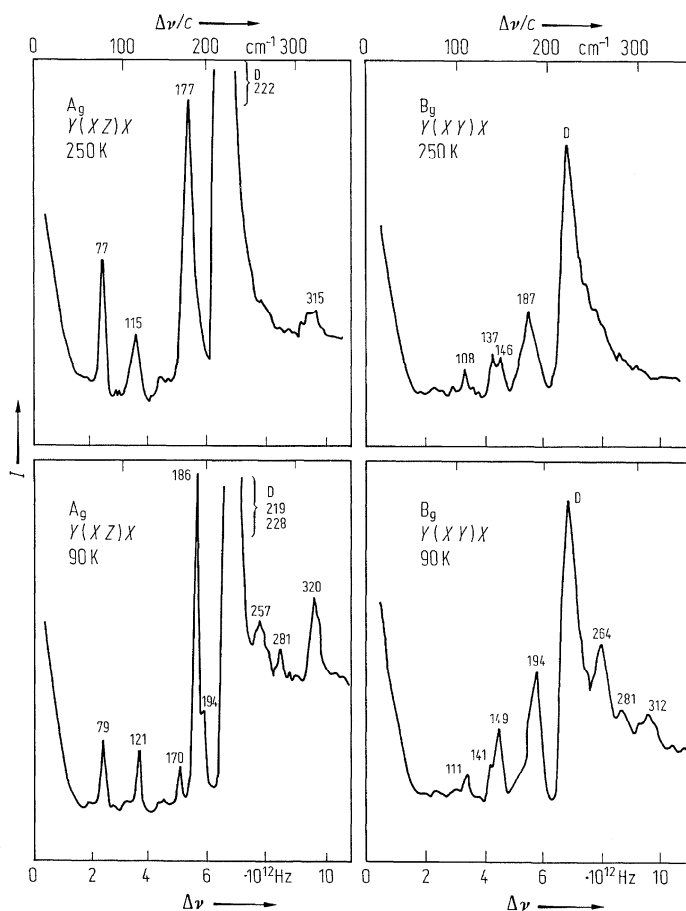
Fig. 52A-1-022.  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $s_{\lambda\mu}$  vs.  $T$  [74Sas].



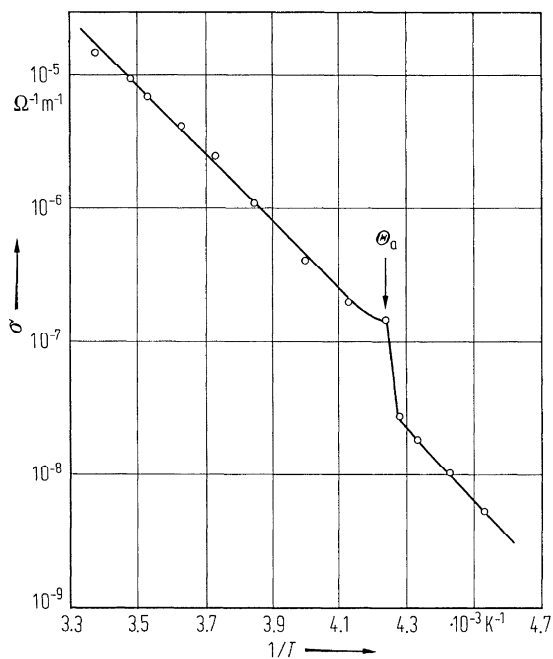
**Fig. 52A-1-023.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\Delta n_b$  vs.  $T$  [70Apk].  $\lambda = 632.8$  nm.



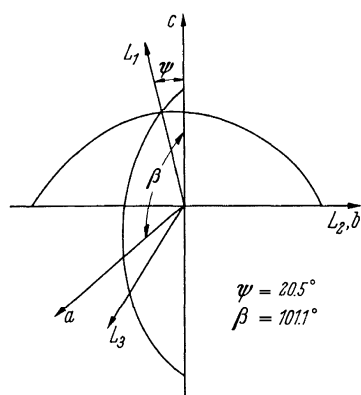
**Fig. 52A-1-024.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\Delta n$  vs.  $E_{\text{bias}}$  [70Apk].  $T = -40.5$  °C,  $\lambda = 632.8$  nm. The insert indicates an enlarged version of  $E_{\text{bias}}$  between  $20$  and  $22.5 \cdot 10^2 \text{ kV m}^{-1}$ .



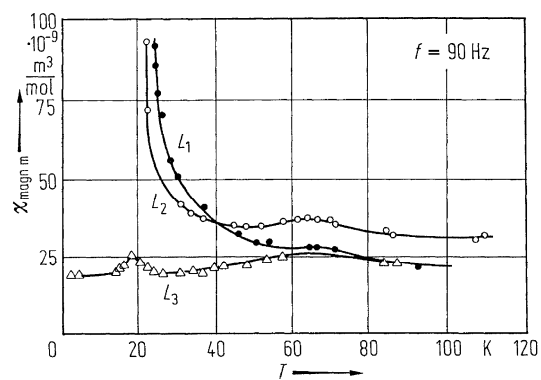
**Fig. 52A-1-025.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $I$  vs.  $\Delta\nu$  [73Can].  $I$ : Raman scattering intensity for the low frequency region. Upper two spectra are in the paraelectric (250 K), and the lower two are in the antiferroelectric phase (90 K). Peak frequencies are indicated in the figure in units of  $\text{cm}^{-1}$ . D is a laser discharge line.



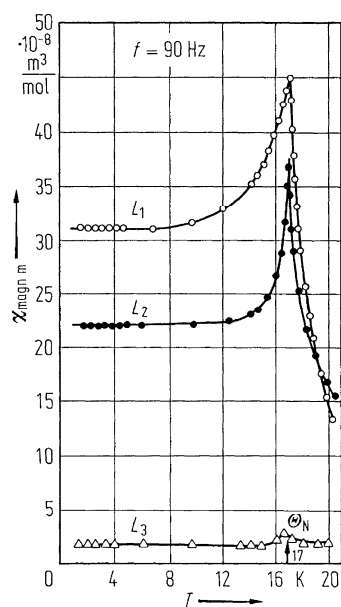
**Fig. 52A-1-026.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ . Protonic dc conductivity  $\sigma$  vs.  $1/T$  [75Web]. Electrodes were saturated cupric formate tetrahydrate solutions of diethylene glycol 2-methoxy ethyl ether and distilled water.  $\sigma$  was measured  $\perp$  to the naturally occurring (110) face.



**Fig. 52A-1-027.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ . Relation between the crystallographic axes ( $a$ ,  $b$ ,  $c$ ) and the magnetic axes ( $L_1$ ,  $L_2$ ,  $L_3$ ) [56Shi].

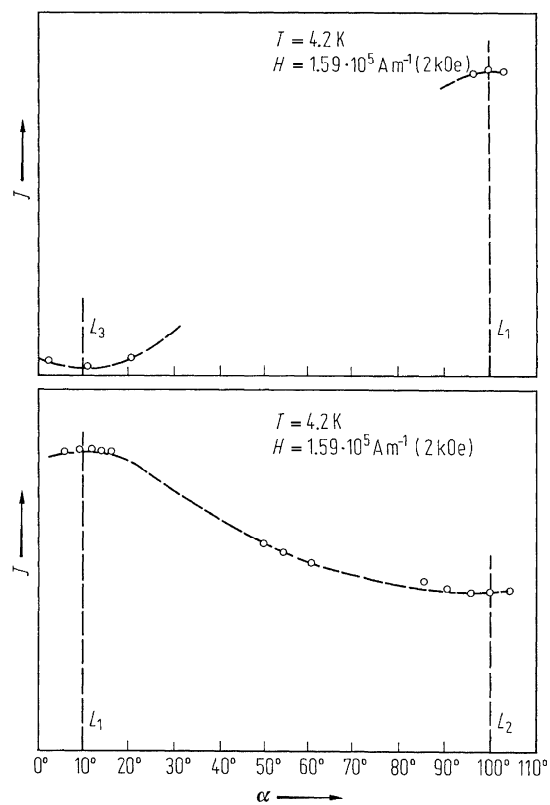


**Fig. 52A-1-028.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\chi_{\text{magn m}}$  vs.  $T$  [63Kob].  $\chi_{\text{magn m}}$ : molar magnetic susceptibilities along the  $L_1$ ,  $L_2$ , and  $L_3$  axes. See Fig. 52A-1-027.

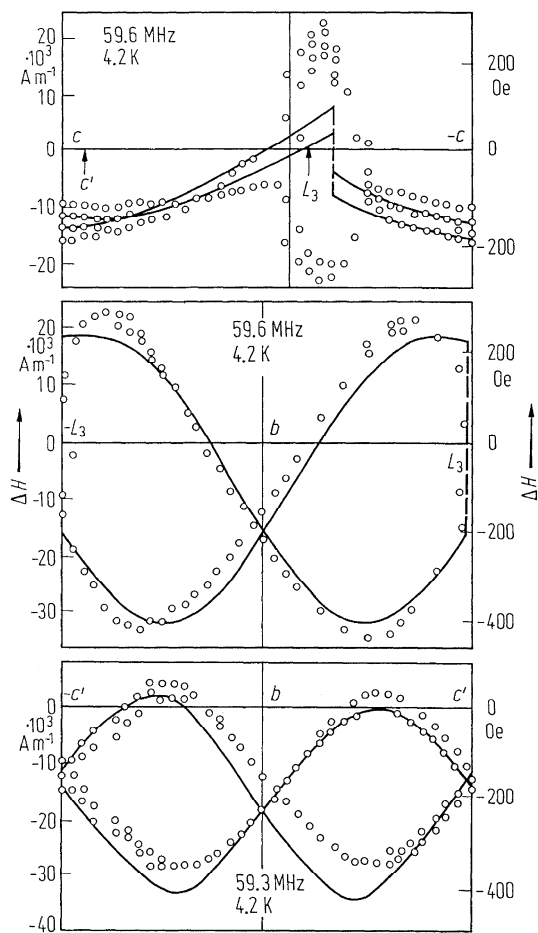


**Fig. 52A-1-029.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\chi_{\text{magn m}}$  vs.  $T$  [63Kob].  $\chi_{\text{magn m}}$ : molar magnetic susceptibilities along the  $L_1$ ,  $L_2$ , and  $L_3$  axes.  $\Theta_N$ : Néel temperature. See Fig. 52A-1-027.

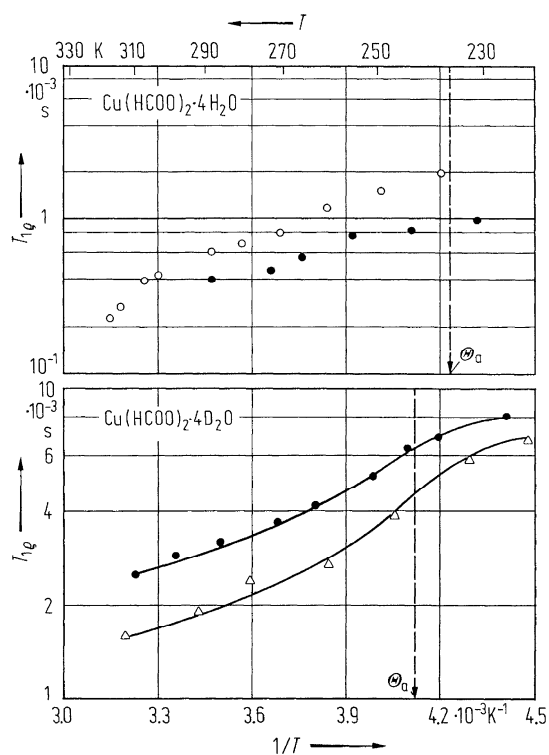




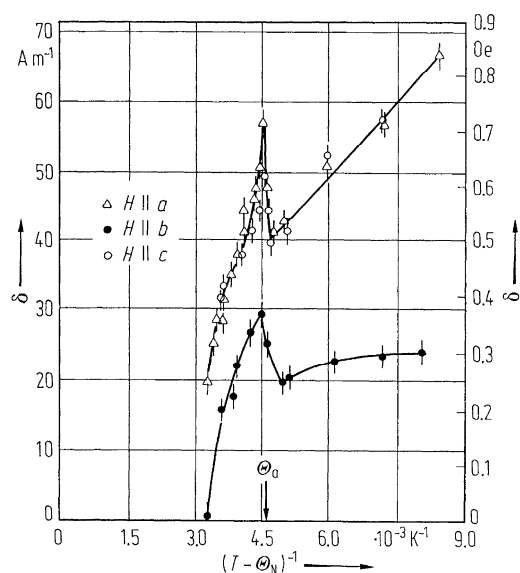
**Fig. 52A-1-030.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $J$  vs.  $\alpha$  [63Kob].  $J$ : magnetic polarization,  $\alpha$ : angle. See Fig. 52A-1-027 for  $L_1, L_2$ .



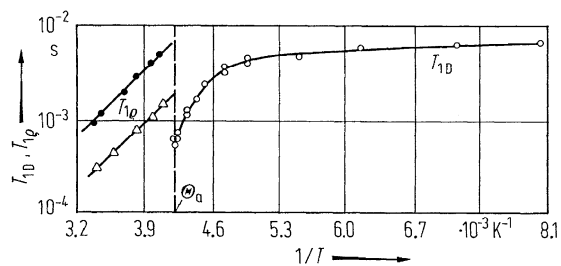
**Fig. 52A-1-031.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{D}_2\text{O}$ .  $\Delta H$  vs. rotation angle [71Yam].  $\Delta H$ : shift of resonance field from free proton. Circles: experimental results; lines: calculated.  $c'$  represents the axis perpendicular to  $ab$  plane.



**Fig. 52A-1-032.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ ,  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{D}_2\text{O}$ .  $T_{1\rho}$  vs.  $T^{-1}$  [74Bon].  $T_{1\rho}$ : proton spin-lattice relaxation time in the rotating frame.  $H_1$ : r.f. field intensity. Open circles:  $H_1 = 3.18 \cdot 10^3 \text{ A m}^{-1}$ ; full circles:  $H_1 = 1.59 \cdot 10^3 \text{ A m}^{-1}$ ; triangles:  $H_1 = 0.8 \cdot 10^3 \text{ A m}^{-1}$ .



**Fig. 52A-1-033.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $\delta$  vs.  $(T - \Theta_N)^{-1}$  [74Mas].  $\delta$ : paramagnetic shift of the formate hydrogen resonance line.  $H = 278.5 \cdot 10^3 \text{ A m}^{-1}$ .



**Fig. 52A-1-034.**  $\text{Cu}(\text{HCOO})_2 \cdot 4\text{H}_2\text{O}$ .  $T_{1\rho}$ ,  $T_{1D}$  vs.  $T^{-1}$  [74Zum].  $T_{1\rho}$ : proton spin-lattice relaxation time in the rotating frame.  $H_1$ : r.f. field intensity. Full circles:  $H_1 = 3.18 \cdot 10^3 \text{ A m}^{-1}$ ; triangles:  $H_1 = 1.59 \cdot 10^3 \text{ A m}^{-1}$ .  $T_{1D}$ : proton spin lattice relaxation time in the dipolar frame.

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