

Antireflection coating on medium with refractive index n2

Calculation of R and T from eq.6.26. To be more general we call the matrix elements M_{ik} , including a refractive index n_1 in the first medium, and setting $A_3/A_1 = x$, $A_1'/A_1 = y$, and $k' = k$

we have for the system of linear equations

Given

$$x \cdot e^{i \cdot k \cdot d} = M_{11} \cdot (1 + y) + M_{12} \cdot (-n_1 + n_1 \cdot y)$$

$$-n_3 \cdot x \cdot e^{i \cdot k \cdot d} = M_{21} \cdot (1 + y) + M_{22} \cdot (-n_1 + n_1 \cdot y)$$

Find(x, y)

$$\begin{bmatrix} \frac{-2}{[\exp(i \cdot k \cdot d) \cdot (M_{21} + M_{22} \cdot n_1 + n_3 \cdot M_{11} + n_3 \cdot M_{12} \cdot n_1)]} \cdot n_1 \cdot (M_{21} \cdot M_{12} - M_{22} \cdot M_{11}) \\ \frac{-(-n_3 \cdot M_{12} \cdot n_1 - M_{22} \cdot n_1 + M_{21} + n_3 \cdot M_{11})}{(M_{21} + M_{22} \cdot n_1 + n_3 \cdot M_{11} + n_3 \cdot M_{12} \cdot n_1)} \end{bmatrix}$$

$$t = \left[\frac{-2}{[\exp(i \cdot k \cdot d) \cdot (M_{21} + M_{22} \cdot n_1 + n_3 \cdot M_{11} + n_3 \cdot M_{12} \cdot n_1)]} \cdot n_1 \cdot (M_{21} \cdot M_{12} - M_{22} \cdot M_{11}) \right]$$

$$r = \frac{-(-n_3 \cdot M_{12} \cdot n_1 - M_{22} \cdot n_1 + M_{21} + n_3 \cdot M_{11})}{(M_{21} + M_{22} \cdot n_1 + n_3 \cdot M_{11} + n_3 \cdot M_{12} \cdot n_1)}$$

$$\bar{t} \cdot t = \frac{-2 \cdot [n_1 \cdot (M_{21} \cdot M_{12} - M_{22} \cdot M_{11})]}{M_{21} + M_{22} \cdot n_1 + n_3 \cdot M_{11} + n_3 \cdot M_{12} \cdot n_1} \cdot \frac{-2 \cdot [n_1 \cdot (M_{21} \cdot M_{12} - M_{22} \cdot M_{11})]}{M_{21} + M_{22} \cdot n_1 + n_3 \cdot M_{11} + n_3 \cdot M_{12} \cdot n_1}$$

$$R = \left[\frac{-(-n_3 \cdot M_{12} \cdot n_1 - M_{22} \cdot n_1 + M_{21} + n_3 \cdot M_{11})}{(M_{21} + M_{22} \cdot n_1 + n_3 \cdot M_{11} + n_3 \cdot M_{12} \cdot n_1)} \right]^2$$