

Numerical calculation

$$n1 := 1 \quad n2 := 1.5 \quad n3 := 2 \quad i := \sqrt{-1}$$

for a single interface, that is

$$M11 := 1 \quad M12 := 0$$

$$M21 := 0 \quad M22 := 1$$

$$tt := \frac{-2 \cdot [n1 \cdot (M21 \cdot M12 - M22 \cdot M11)]}{M21 + M22 \cdot n1 + n3 \cdot M11 + n3 \cdot M12 \cdot n1} \cdot \frac{-2 \cdot [n1 \cdot (M21 \cdot M12 - M22 \cdot M11)]}{M21 + M22 \cdot n1 + n3 \cdot M11 + n3 \cdot M12 \cdot n1}$$

$$tt = 0.444$$

$$R := \left[\frac{-(-n3 \cdot M12 \cdot n1 - M22 \cdot n1 + M21 + n3 \cdot M11)}{(M21 + M22 \cdot n1 + n3 \cdot M11 + n3 \cdot M12 \cdot n1)} \right]^2$$

$$R = 0.111$$

One sees that R+TT is not 1 and tt is not the transmitted power

However if $n3 \cdot tt$ is the transmitted power T, one has

$$T := n3 \cdot tt \quad T = 0.889 \quad \text{and} \quad T + R = 1$$

and if $n1$ is not 1 we have more generally to write

$$T := \frac{n3}{n1} \cdot tt$$

For antireflection coating one has eq. 6.27

$$r = \left[\frac{-(-n_3 \cdot MM_{12} \cdot n_1 + MM_{21})}{(MM_{21} + n_3 \cdot MM_{12} \cdot n_1)} \right]$$

$$MM_{12}(nn_2) = \frac{-i}{nn_2} \quad MM_{21}(nn_2) = -i \cdot nn_2$$

Since -i cancels out we have

$$MM_{12}(nn_2) := \frac{1}{nn_2} \quad MM_{21}(nn_2) := nn_2$$

$$nn_2 := 1.1, 1.11 \dots 2 \quad nn_1 := 1 \quad nn_3 := 1.5$$

$$R(nn_2) := \left[\frac{-(-nn_3 \cdot MM_{12}(nn_2) \cdot nn_1 + MM_{21}(nn_2))}{(MM_{21}(nn_2) + nn_3 \cdot MM_{12}(nn_2) \cdot nn_1)} \right]^2$$

