

### A3SPHTINS

#### Spherical aberration of a thin lens.

Calculation of focal length  $f$  and  $f''$  (corrected)  
and longitudinal Spherical Aberration.  
All length in cm.

#### Input data

$$n \equiv 1.5 \quad r1 \equiv 20 \quad r2 \equiv -20 \quad x_o \equiv -40 \quad r_o \equiv 2$$

#### 1. Calculation of $f$ and $x_i$

$$f := \frac{1}{(n-1) \cdot \left( \frac{1}{r1} - \frac{1}{r2} \right)} \quad f := 20$$

Calculation of  $x_i$

$$x_i := \frac{1}{\left( \frac{1}{f} \right) + \frac{1}{x_o}} \quad x_i = 40$$

#### 2. Calculation of $ff$ , shape and position factor and $x_i$

$$a(x_o) := \left[ \left( \frac{1}{r1} - \frac{1}{x_o} \right)^2 \cdot \left( \frac{1}{r1} - \frac{n+1}{x_o} \right) \right] \quad b(x_o) := \left( \frac{1}{x_o} + \frac{n-1}{r1} - \frac{n}{r2} \right)^2$$

$$c(x_o) := \left[ \frac{n^2}{r2} - \frac{n+1}{x_o} - \frac{(n^2-1)}{r1} \right]$$

$$ff(x_o) := \frac{1}{\left[ \frac{1}{f} + \frac{n-1}{n^2} \cdot \left( \frac{r_o^2}{2} \right) \cdot (a(x_o) - b(x_o) \cdot c(x_o)) \right]}$$

$$ff(x_o) = 19.778$$

Image distance for no Sph Abb

$$x_{i1}(x_o) := \frac{1}{\left( \frac{1}{x_o} + \frac{1}{f} \right)}$$

$$x_{i1}(x_o) = 40$$

Image distance for Sph Abb

$$x_{iisph}(x_o) := \frac{1}{\left( \frac{1}{x_o} + \frac{1}{ff(x_o)} \right)}$$

$$x_{iisph}(x_o) = 39.12$$

#### 3. Calculation of LSA

$$LSA_{xi}(x_o) := x_{i1}(x_o) - x_{iisph}(x_o)$$

$$LSA_{xi}(x_o) = 0.88$$

#### 4. Calculation of lateral spherical aberration LAT

$$\text{LAT} := \text{LSAxi}(x_0) \cdot \frac{\rho}{\text{xiisph}(x_0)} \quad \rho := 4$$

$$\text{LAT} = 0.09$$