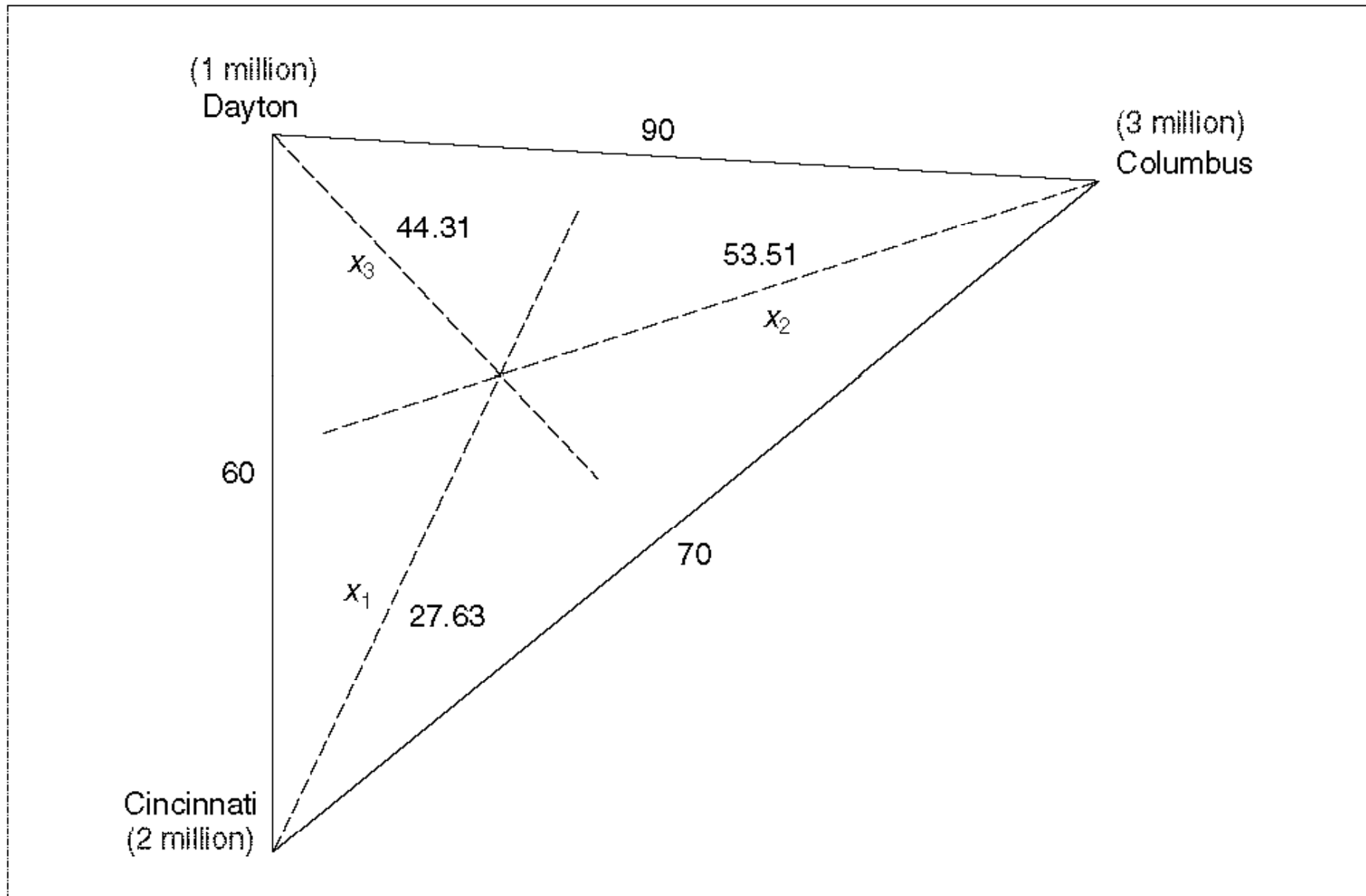


Figure 3.1 A LOCATION DETERMINED BY ANGLE BISECTORS



SOURCE: Claunh, Goehring, and Chan (1992). Reprinted with permission.

Figure 3.2 BLOCK DIAGRAM OF THE NEW YORK-NEW HAVEN
DEVELOPMENT EXAMPLE

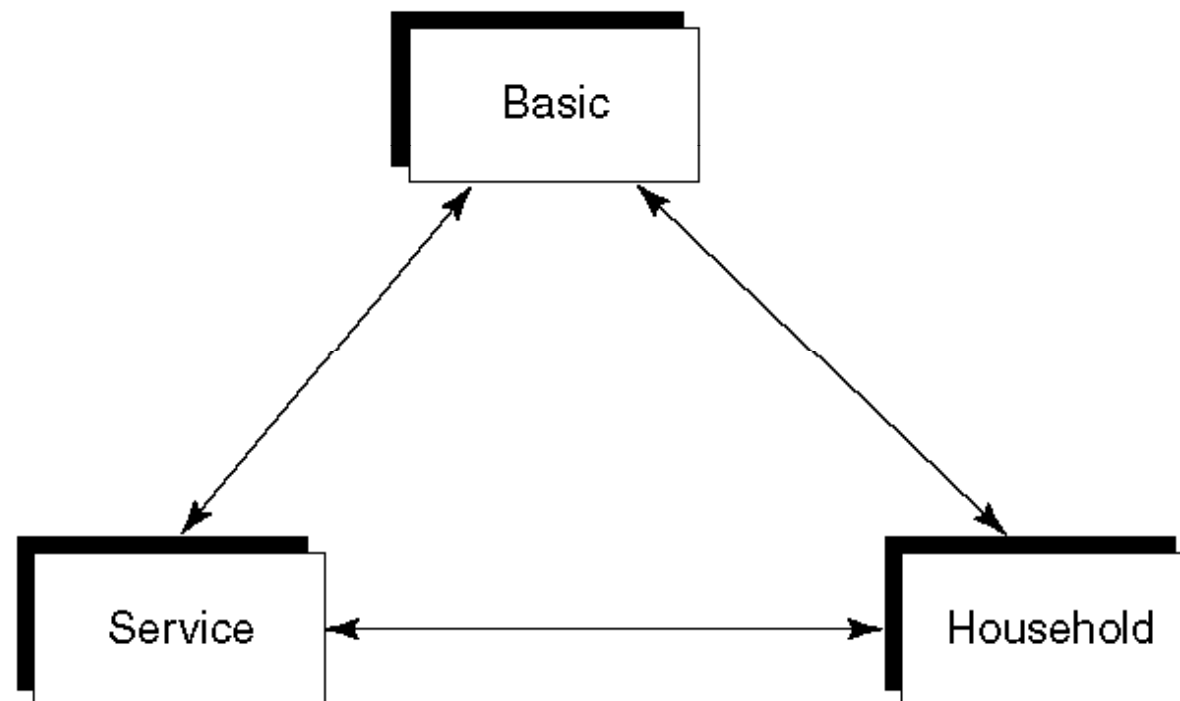


Figure 3.3 LOGIC FLOW CHART OF THE NEW YORK-NEW HAVEN EXAMPLE

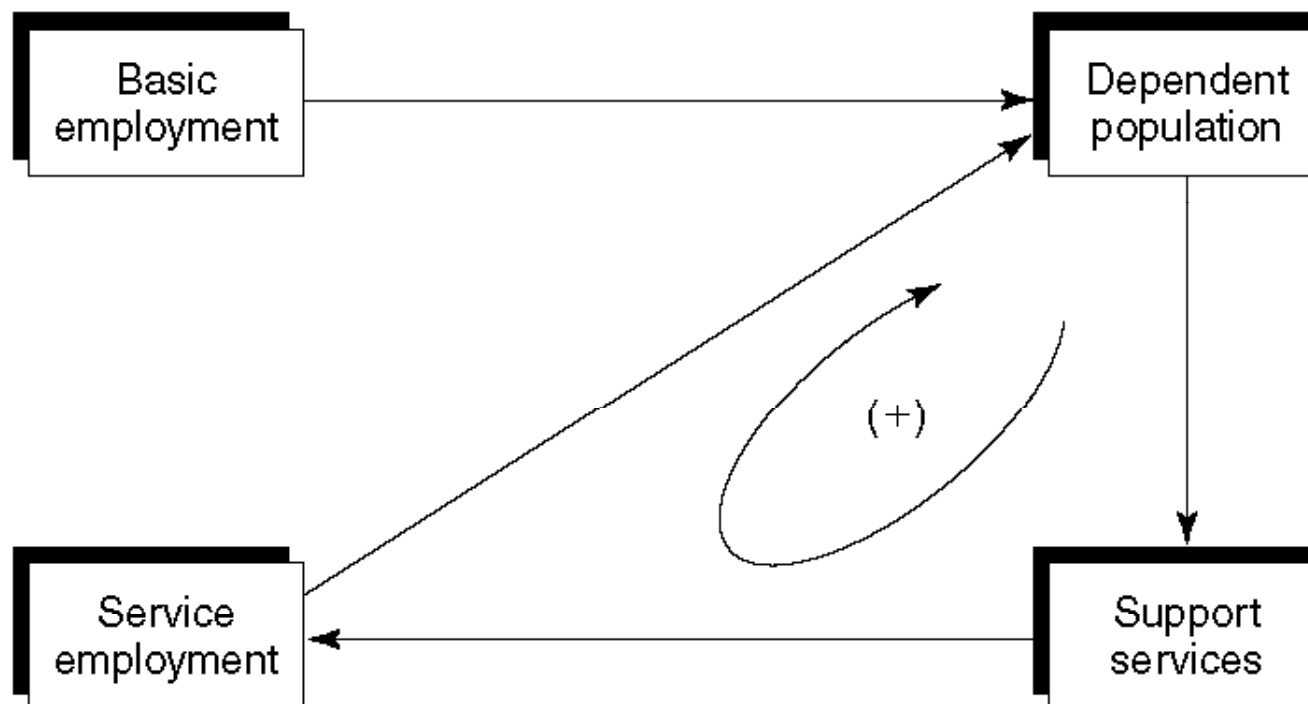


Table 3.1 ILLUSTRATION OF A DETERMINISTIC SIMULATION ON REGIONAL ECONOMIC DEVELOPMENT

| Time n | Basic emp E^B | Basic emp pop | Support service emp E^R | Support service pop | Total emp E | Total pop N |
|-------------|--------------------|---------------------|---------------------------------|---------------------------|---|--|
| 1 | E^B | $f E^B$ | $af E^B$ | $af^2 E^B$ | $(1 + af) E^B$ | $f(1 + af) E^B$ |
| 2 | | | $a^2 f^2 E^B$ | $a^2 f^3 E^B$ | $(1 + af + a^2 f^2) E^B$ | $f(1 + af + a^2 f^2) E^B$ |
| 3 | | | $a^3 f^3 E^B$ | $a^3 f^4 E^B$ | $(1 + af + a^2 f^2 + a^3 f^3) E^B$ | $f(1 + af + a^2 f^2 + a^3 f^3) E^B$ |
| ... | | | ... | ... | ... | ... |
| ∞ | | | 0 | 0 | $(1 + af + a^2 f^2 + a^3 f^3 + ..) E^B$ | $f(1 + af + a^2 f^2 + a^3 f^3 + ..) E^B$ |

Figure 3.4 LIMITS TO GROWTH MODEL

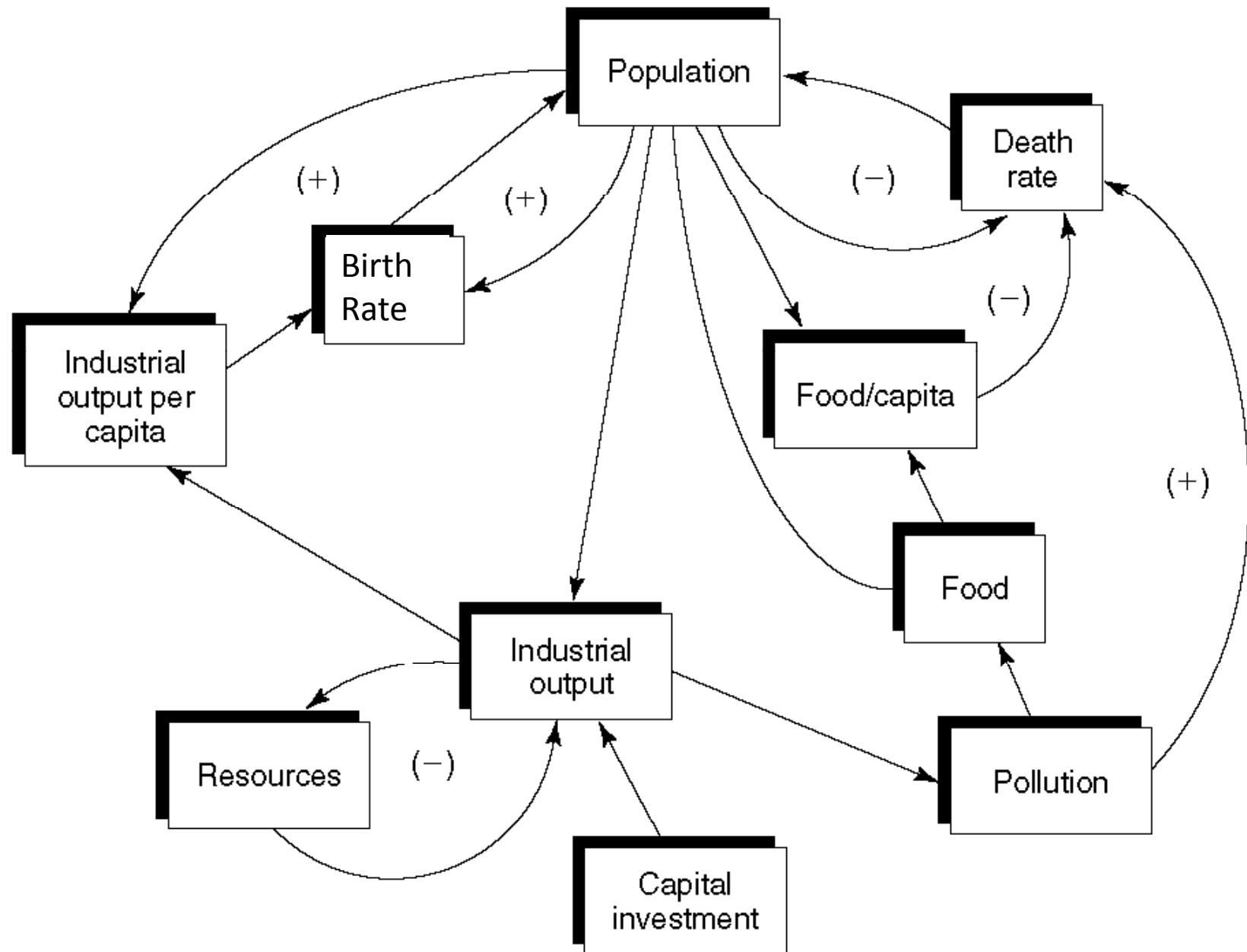


Figure 3.5 WORLD FORECAST THROUGH 2100

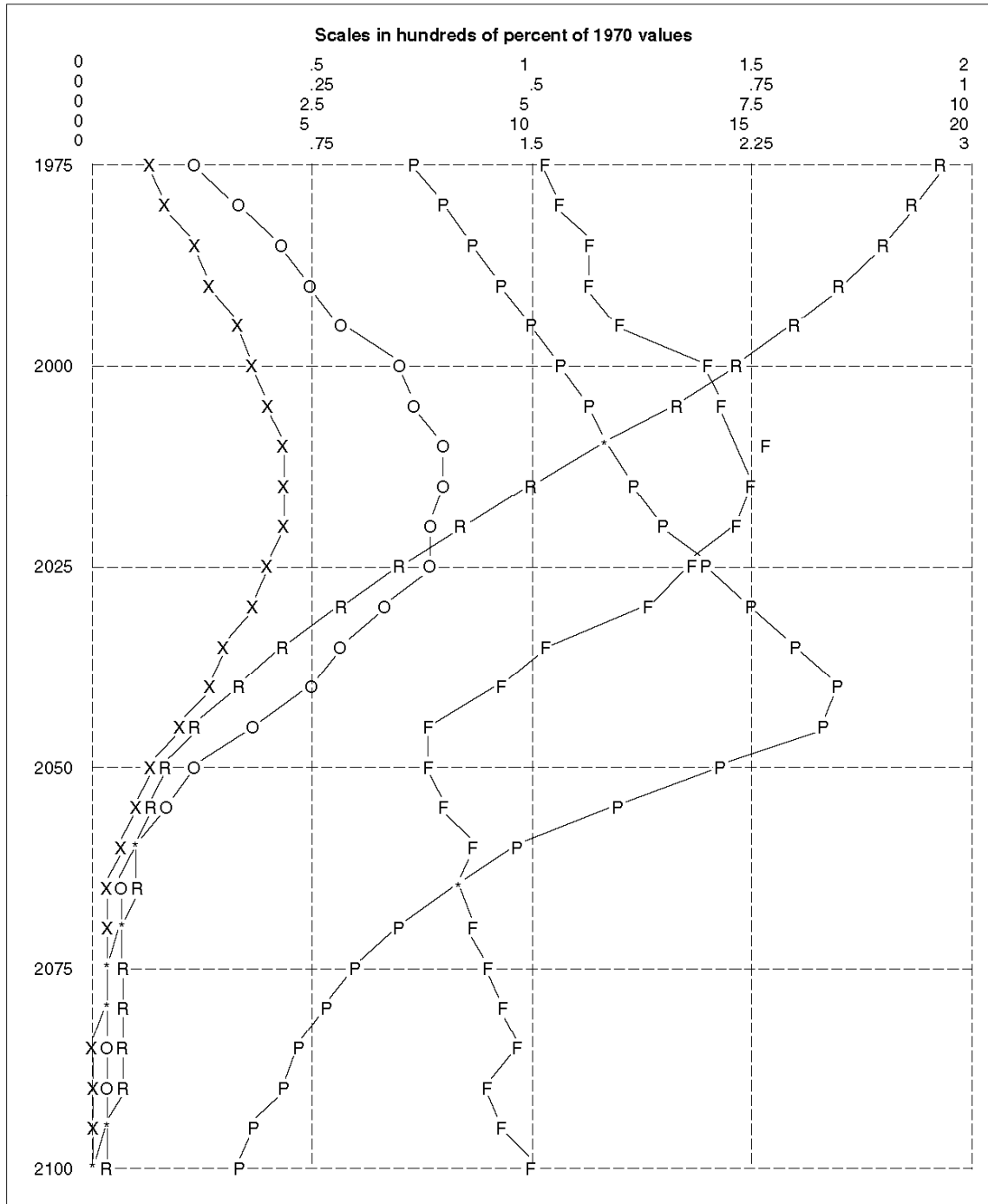
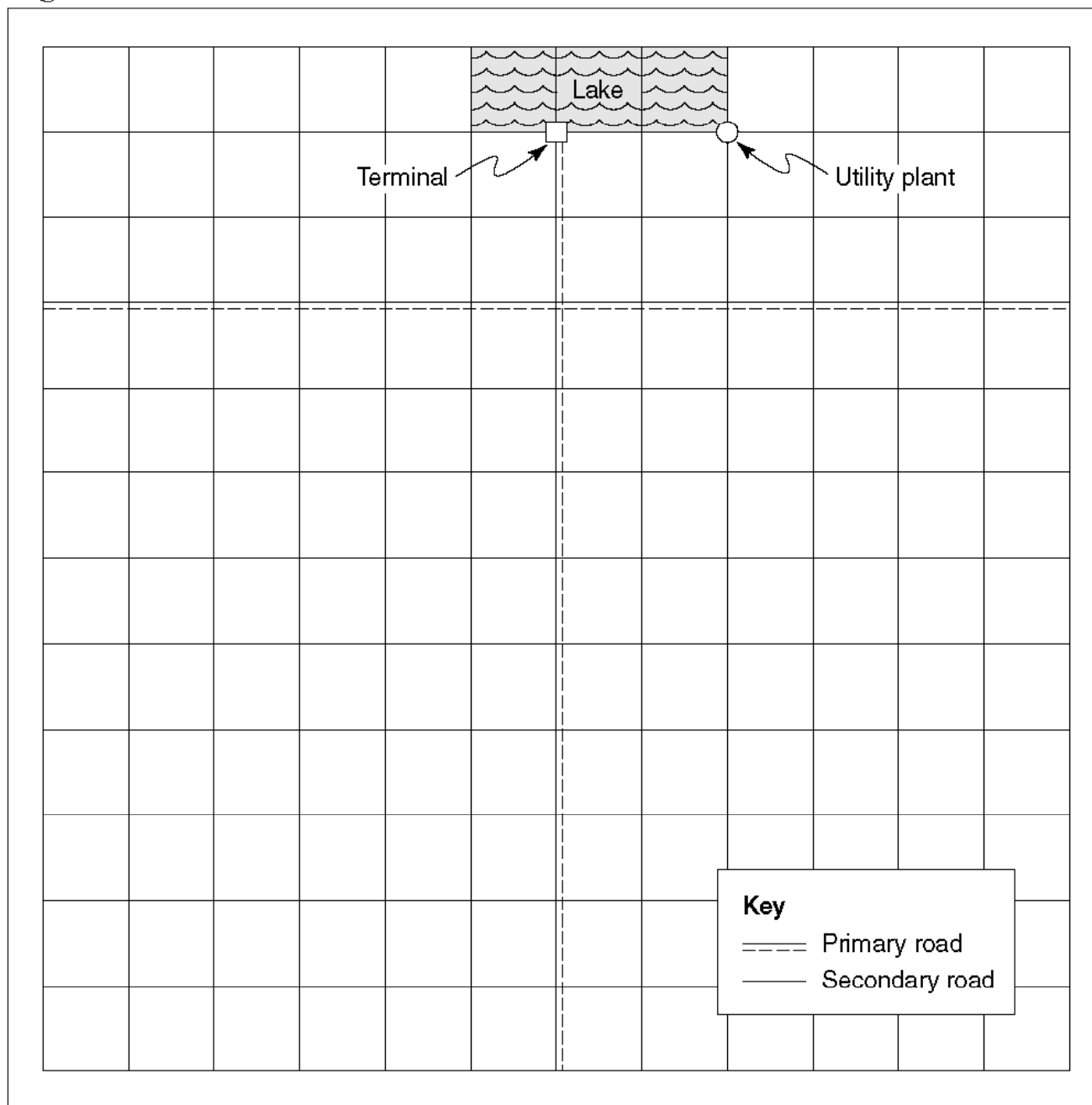


Figure 3.6 THE CLUG PLAYING BOARD

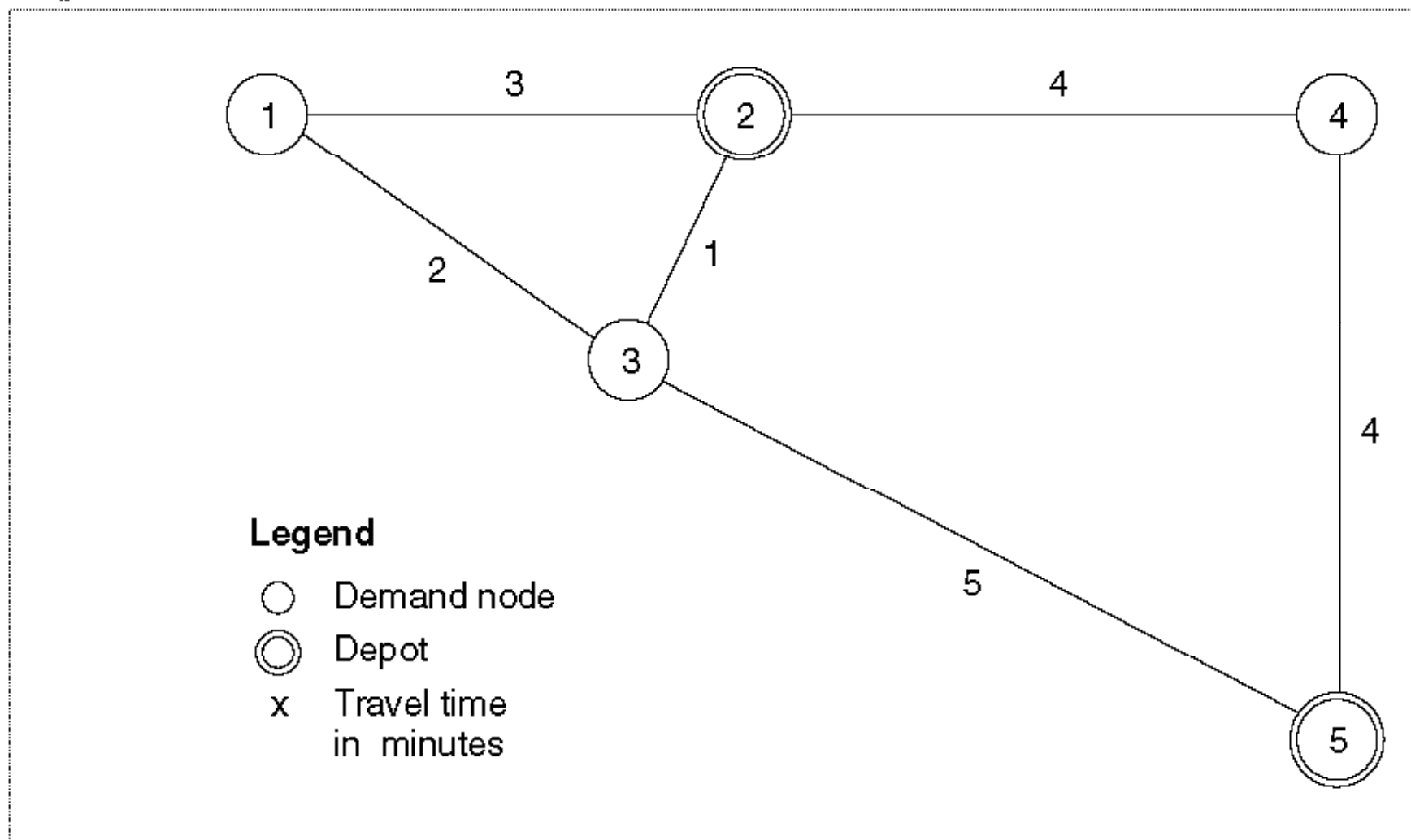


SOURCE: Feldt (1972). Reprinted with permission.

Table 3.2 PROBABILITY OF BUILDING LOSS

| Age of building | Probability of loss | Losing numbers |
|-----------------|---------------------|----------------|
| 0 | 0.056 | 3 |
| 1 | 0.111 | 5 |
| 2 | 0.167 | 7 |
| 3 | 0.195 | 2, 7 |
| 4 | 0.250 | 2, 7, 11 |
| 5 | 0.306 | 2, 7, 9 |
| 6 | 0.362 | 3, 7, 8 |
| 7 | 0.417 | 5, 7, 8 |
| 8 | 0.445 | 6, 7, 8 |
| 9 | 0.500 | 3, 6, 7, 8 |
| 10 | 0.555 | 5, 6, 7, 8 |

Figure 3.7 SAMPLE NETWORK FOR HYPERCUBE MODEL



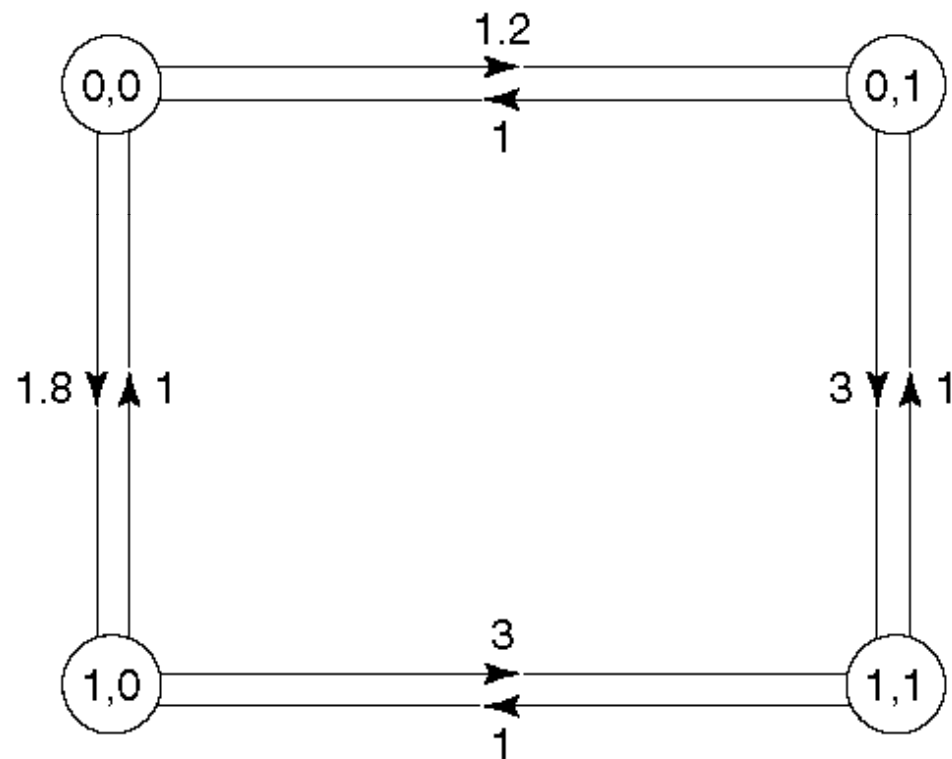
SOURCE: Ahituv and Berman (1988). Reprinted with permission.

Table 3.3 DISPATCHING RULES FOR THE HYPERCUBE NETWORK

| State | Server vehicle location | Demand node | | | | |
|--------|-------------------------------|-------------|---|---|---|---|
| | | 1 | 2 | 3 | 4 | 5 |
| (0, 0) | 2 | ✓ | ✓ | ✓ | — | — |
| | 5 | — | — | — | ✓ | ✓ |
| (0, 1) | 2 | ✓ | ✓ | ✓ | ✓ | ✓ |
| (1, 0) | 5 | ✓ | ✓ | ✓ | ✓ | ✓ |
| (1, 1) | not relevant | | | | | |

SOURCE: Ahituv and Berman (1988). Reprinted with permission.

Figure 3.8 TRANSITION BETWEEN STATES IN A HYPERCUBE MODEL



SOURCE: Ahituv and Berman (1988). Reprinted with permission.

Figure 3.9 A CONVEX EXPECTED TOTAL-COST FUNCTION



Figure 3.10 Tree representation of Bayes' Rule

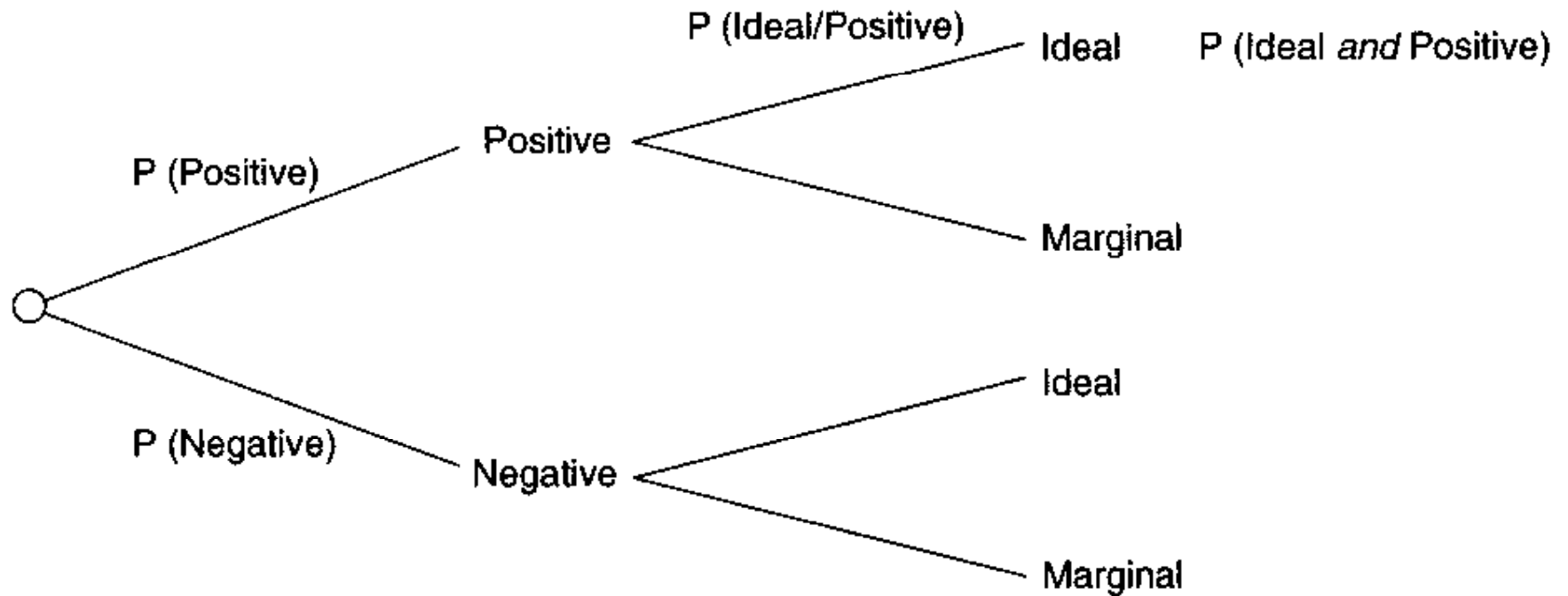
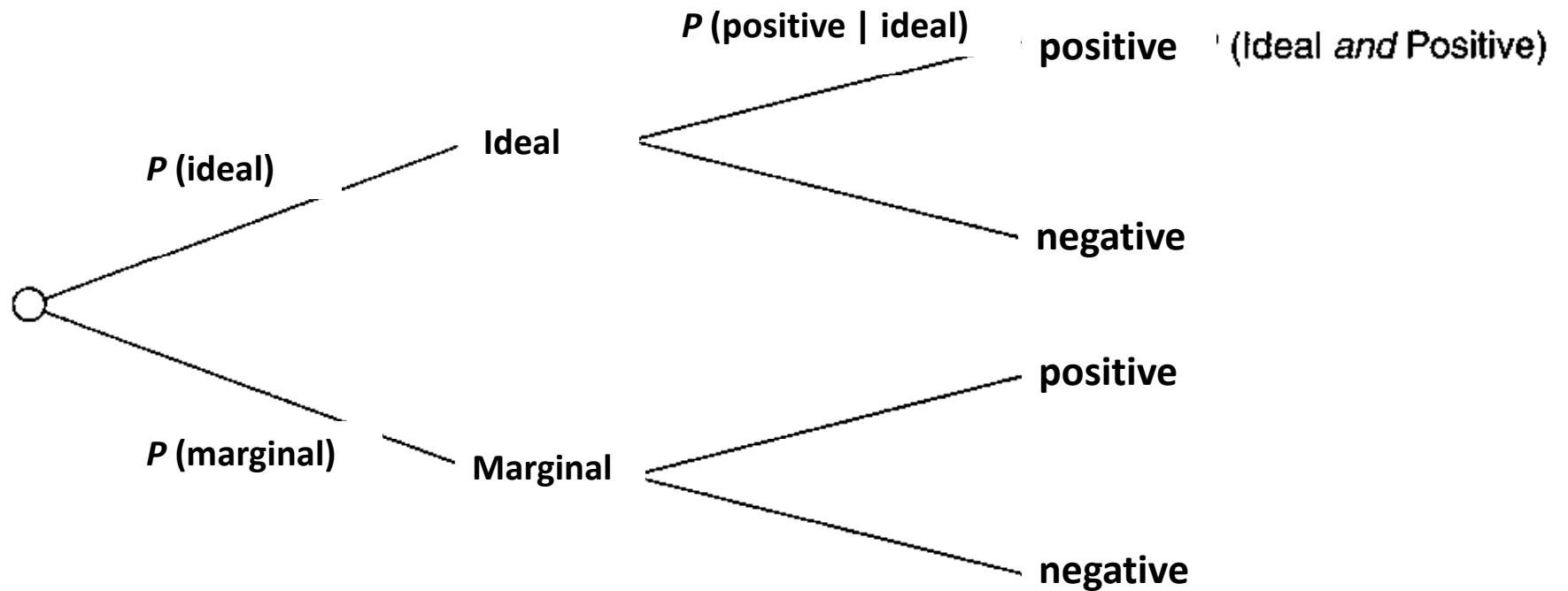


Figure 3.10A Bayes' rule revisited



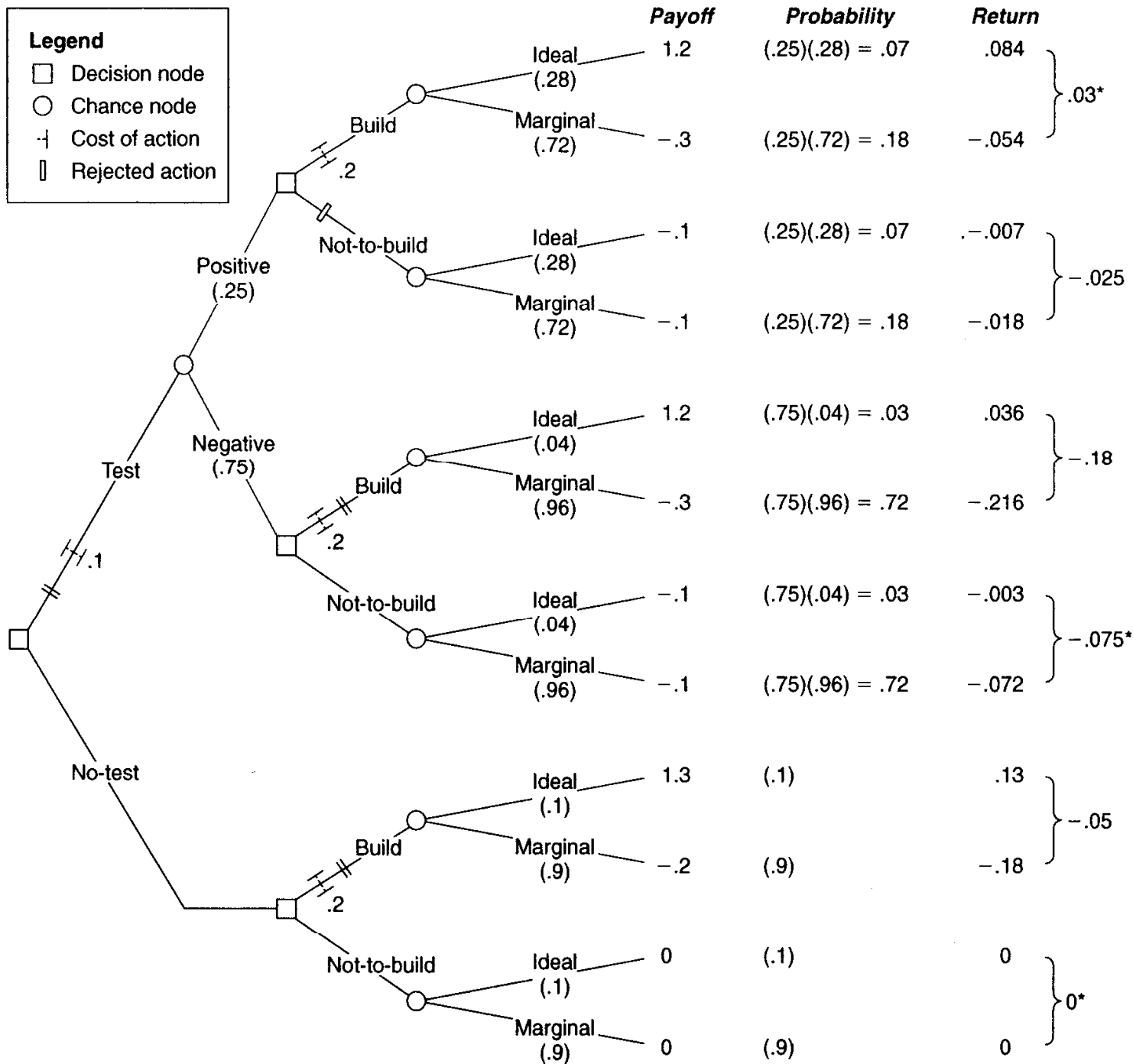


Figure 3.11
Decision Tree
with returns

Figure 3.12 An Example Influence Diagram

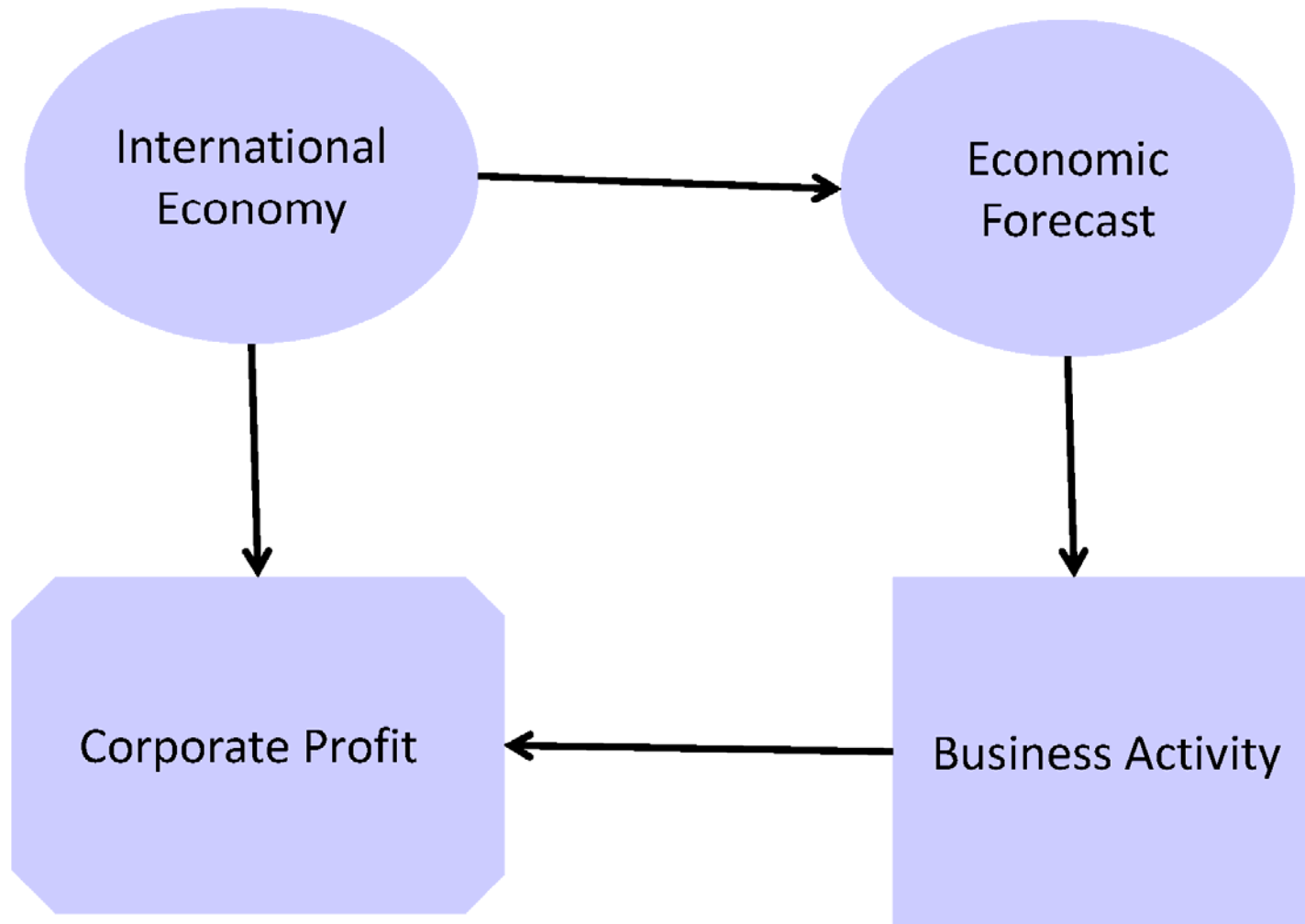


Figure 3.13 Two-class example

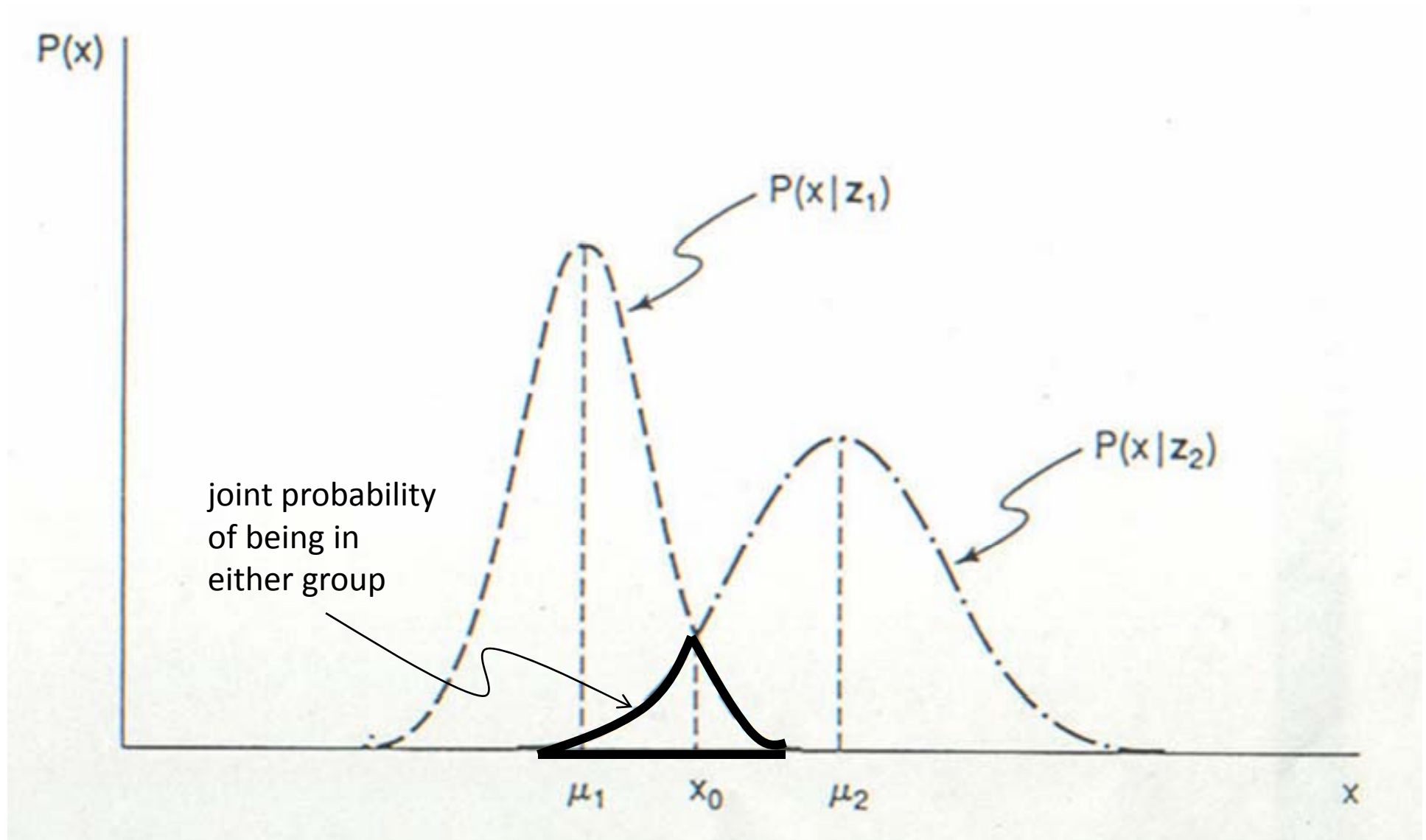


Figure 3.14 ARROW DIAGRAM FOR ECONOMIC-BASE EXAMPLE

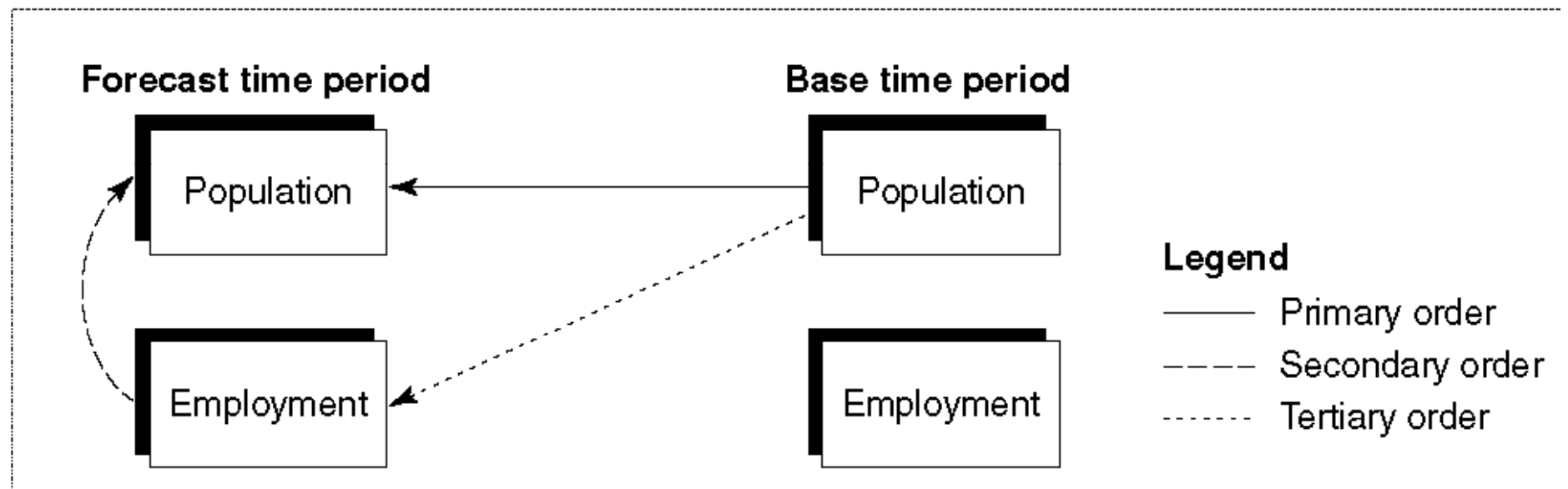
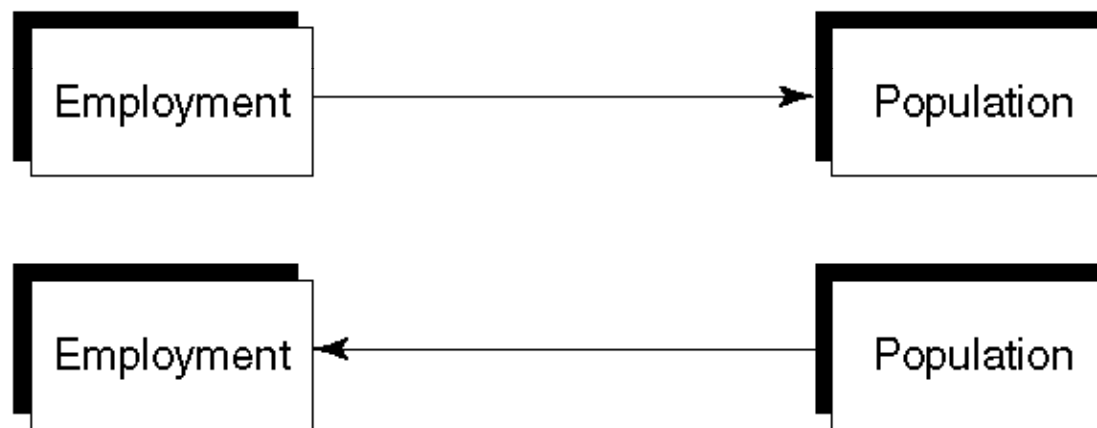


Figure 3.15 PATH ANALYSIS FOR THE ECONOMIC-BASE EXAMPLE



Both have the same
correlation coefficient

Figure 3.16 CORRELATION COEFFICIENTS

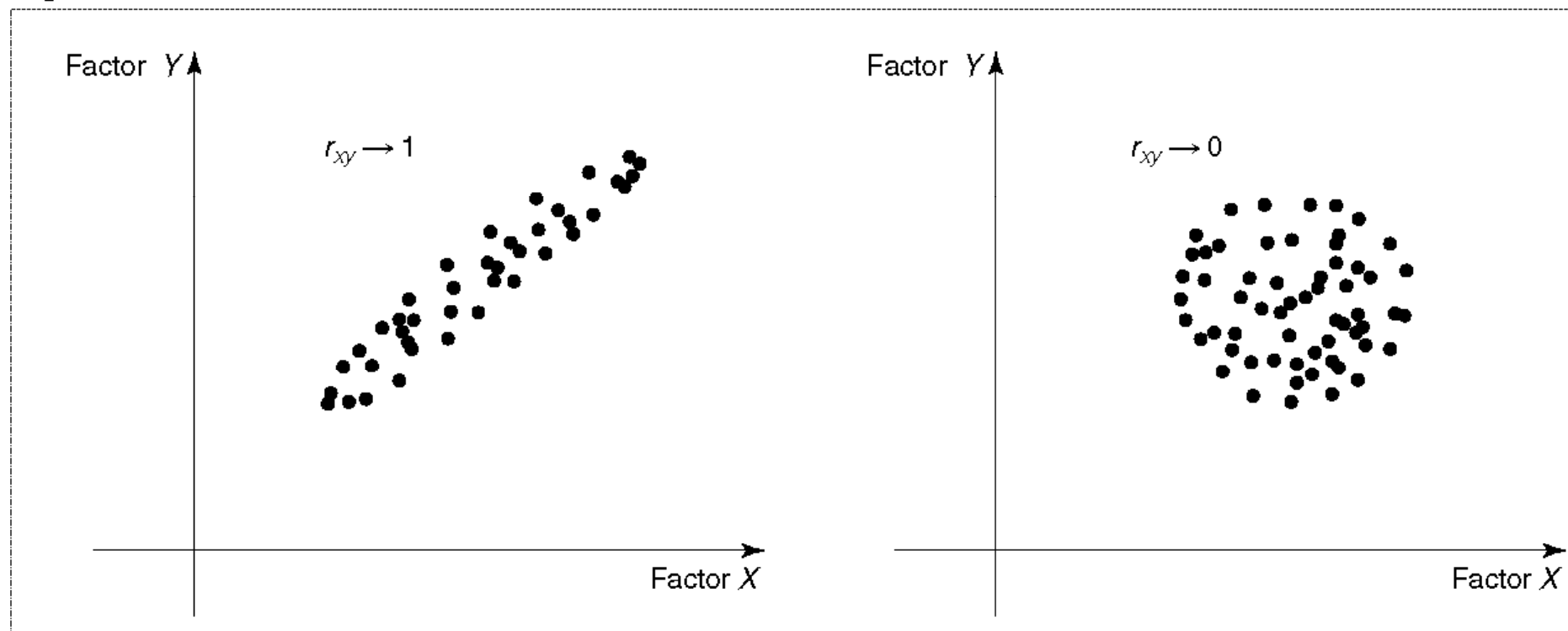
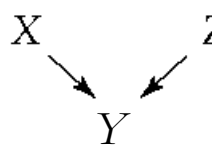

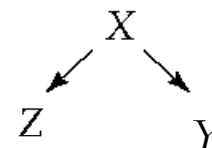

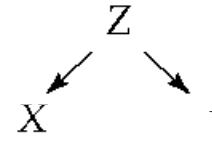
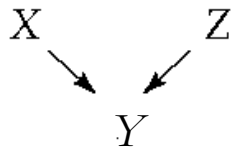
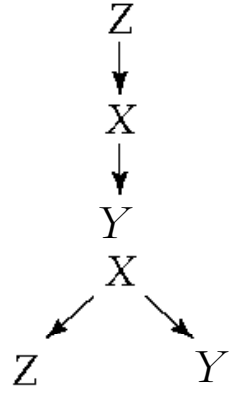
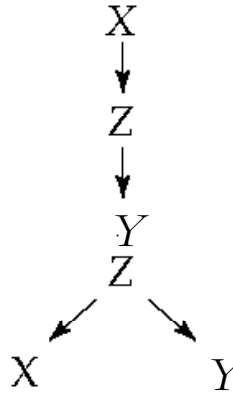


Table 3.4 TYPOLOGY OF 2-ARROW MODELS

| Model type | Arrow diagram | Econometric equations |
|---|---|--|
| Both X and Z independently affect Y. |  <pre> graph TD X --> Y Z --> Y </pre> | $\begin{aligned} X &= b_1 \\ a_{21} X + Y + a_{23} Z &= b_2 \\ Z &= b_3 \end{aligned}$ |
| X, partially caused by Z, causes Y. |  <pre> graph TD Z --> X X --> Y </pre> | $\begin{aligned} X + a_{13} Z &= b_1 \\ a_{21} X + Y &= b_2 \\ Z &= b_3 \end{aligned}$ |
| The primary variable X causes both Z and Y. |  <pre> graph TD X --> Z X --> Y </pre> | $\begin{aligned} X &= b_1 \\ a_{21} X + Y &= b_2 \\ a_{31} X + Z &= b_3 \end{aligned}$ |
| The secondary variable Z intervenes between X and Y. |  <pre> graph TD X --> Z Z --> Y </pre> | $\begin{aligned} X &= b_1 \\ Y + a_{23} Z &= b_2 \\ a_{31} X + Z &= b_3 \end{aligned}$ |
| The primary variable X and the supposedly dependently variable Y are correlated but not casually connected. |  <pre> graph TD X --> Z Y --> Z </pre> | $\begin{aligned} X + a_{13} Z &= b_1 \\ Y + a_{23} Z &= b_2 \\ Z &= b_3 \end{aligned}$ |

SOURCE: De Neufville and Stafford (1971). Reprinted with permission.

Table 3.5 RESULTS OF PATH ANALYSIS

| Grouping of models | Arrow diagram | Path analysis prediction | Condition |
|--------------------|---|----------------------------------|------------------------------------|
| Y in the middle |  <pre> graph TD X --> Y Z --> Y </pre> | $r_{XZ} = 0$ | $r_{XY} \neq 0$ $r_{YZ} \neq 0$ |
| X in the middle |  <pre> graph TD Z --> X X --> Y Y --> Z Y --> Y </pre> | $r_{XY} = \frac{r_{YZ}}{r_{XZ}}$ | $r_{XY} \neq 0$ $r_{XZ} \neq 0$ |
| Z in the middle |  <pre> graph TD X --> Z Z --> Y Y --> X Y --> Y </pre> | $r_{XY} = r_{XZ}r_{YZ}$ | $r_{XZ} \neq 0$ $r_{YZ} \neq 0$ |

SOURCE: De Neufville and Stafford (1971). Reprinted with permission.

Table 3.6 CORRELATION MATRIX BETWEEN VARIABLES IN THE CENTRAL BERKSHIRE MODEL

| | N | E^R | E^B | ΔN | ΔE^R | ΔE^B | u |
|--------------|--------|---------|---------|------------|--------------|--------------|--------|
| E^R | 0.6722 | | | | | | |
| E^B | 0.7284 | 0.9028 | | | | | |
| ΔN | 0.1892 | -0.3478 | -0.0167 | | | | |
| ΔE^R | 0.7042 | 0.9885 | 0.9113 | -0.3026 | | | |
| ΔE^B | 0.5747 | 0.4634 | 0.6423 | 0.2719 | 0.5801 | | |
| u | 0.8455 | 0.5413 | 0.5331 | 0.1559 | 0.5697 | 0.3929 | |
| t' | 0.8063 | 0.5342 | 0.4937 | 0.0859 | 0.5609 | 0.3613 | 0.9821 |

SOURCE: Foot (1981). Reprinted with permission.

Table 3.7 DISAGGREGATE CALIBRATION OF A MAXIMUM LIKELIHOOD MODEL

| Individual n | Time to location 1 τ_{n1} (min) | Time to location 2 τ_{n2} (min) | Locational choice k |
|-------------------|---|---|--------------------------|
| 1 | 5 | 7 | 1 |
| 2 | 4 | 6 | 1 |
| 3 | 6 | 4 | 2 |

SOURCE: Kanafani (1983). Reprinted with permission.

Table 3.8 DATABASE FOR CALIBRATING AN AGGREGATE LOCATION CHOICE MODEL

| Shopping center k | Average time τ_k | Average cost c_k | No of patrons at center k |
|------------------------|--------------------------|-----------------------|--------------------------------|
| 1 | 15 | 3 | 50 |
| 2 | 10 | 4 | 40 |
| 3 | 20 | 7 | 10 |

Table 3.9 REPLICATION TEST DATA FOR LOGIT MODEL

| Shopper | Time to location 1 τ_1 (min) | Time to location 2 τ_2 (min) | $\delta\tau = \tau_2 - \tau_1$ (min) | Cost to location 1 c_1 (\$) | Cost to location 2 c_2 (\$) | $\delta c = c_2 - c_1$ (\$) | Locational decision |
|---------|---|---|---|-------------------------------------|-------------------------------------|--------------------------------|------------------------|
| 1 | 25 | 30 | -5 | 3.00 | 1.00 | 2 | 1 |
| 2 | 10 | 15 | -5 | 1.00 | 1.00 | 0 | 1 |
| 3 | 50 | 40 | 10 | 5.00 | 1.00 | 4 | 2 |
| Average | — | — | 0 | — | — | 2 | — |

Table 3.10 EXISTING INTERZONAL TRAVEL

| From/to | Zone 1 | Zone 2 | Zone 3 | Zone 4 | V_i |
|---------|--------|--------|--------|--------|-------|
| Zone 1 | | 500 | 200 | 300 | 1000 |
| Zone 2 | | 800 | 100 | 500 | 1400 |
| Zone 3 | | | | | |
| Zone 4 | | | | | |
| V_j | | 1300 | 300 | 800 | 2400 |

SOURCE: Dickey (1983). Reprinted with permission.

Table 3.11 INTERZONAL TRAVEL TIMES (IN MINUTES)

| From/to | Zone 1 | Zone 2 | Zone 3 | Zone 4 |
|---------|--------|--------|--------|--------|
| Zone 1 | 3 | 8 | 5 | 10 |
| Zone 2 | 8 | 3 | 10 | 5 |
| Zone 3 | 5 | 10 | 3 | 20 |
| Zone 4 | 10 | 5 | 20 | 3 |

SOURCE: Dickey (1983). Reprinted with permission.

Figure 3.17 TRIP DISTRIBUTION PLOTS

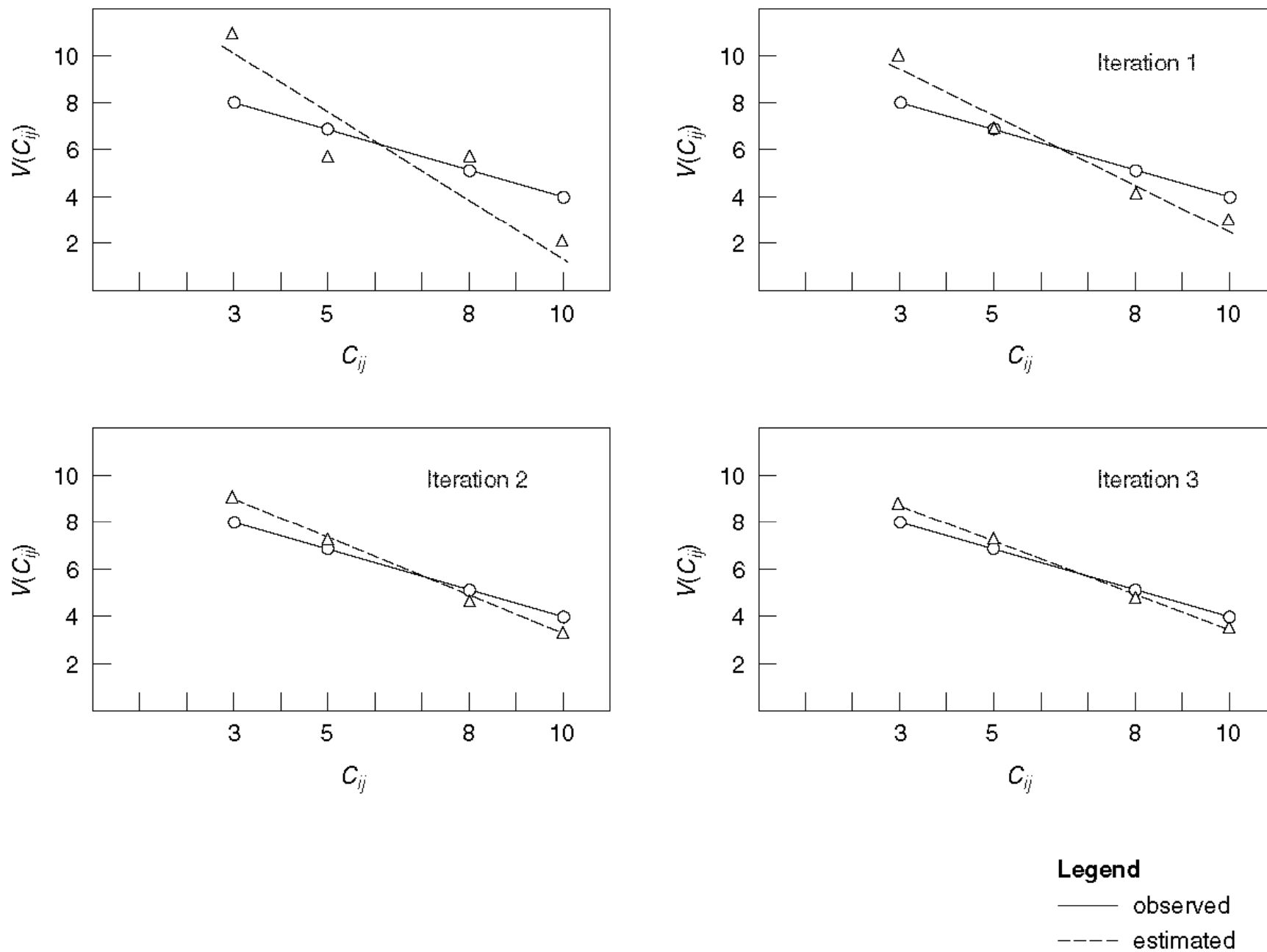


Table 3.12 CHI-SQUARE TEST

| Time Interval (min) | 3 | 5 | 8 | 10 |
|--|---------|--------|---------|--------|
| Observed y_i | 800 | 700 | 500 | 400 |
| Estimated \hat{y}_i | 857.28 | 707.90 | 457.40 | 377.00 |
| $(y_i - \hat{y}_i)$ | -57.28 | -7.90 | 42.60 | 23.00 |
| $(y_i - \hat{y}_i)^2$ | 3281.00 | 62.41 | 1814.76 | 529 |
| $(y_i - \hat{y}_i)^2 / \hat{y}_i$ | 3.83 | 0.09 | 3.97 | 1.40 |
| $\Sigma_i (y_i - \hat{y}_i)^2 / \hat{y}_i$ | 3.83 | 3.92 | 7.88 | 9.29 |

Table 3.13 Observed inter-zonal travel of doubly-constrained model

| From/to | $j = 1$ | $j = 2$ | $j = 3$ | V_i |
|---------|---------|---------|---------|--------|
| $i = 1$ | 1,800 | 3,100 | 100 | 5,000 |
| $i = 2$ | 3,100 | 1,500 | 400 | 5,000 |
| $i = 3$ | 15,100 | 25,400 | 4,500 | 45,000 |
| V_j | 20,000 | 30,000 | 5,000 | 55,000 |

Table 3.14 Calibration of a doubly-constrained model

| | Iteration number | | | | | | |
|-------|------------------|---------------------|--------|--------|--------|--------|--------|
| | 1 | | 2 | | 3 | | 4 |
| k_1 | 1 | | 0.9148 | | 0.9125 | | 0.9125 |
| k_2 | 1 | | 1.3312 | | 1.3437 | | 1.3437 |
| k_3 | 1 | | 0.9833 | | 0.9824 | | 0.9824 |
| l_1 | | 0.1187 ¹ | | 0.1164 | | 0.1164 | |
| l_2 | | 0.1058 | | 0.1073 | | 0.1073 | |
| l_3 | | 0.0965 | | 0.0961 | | 0.0961 | |

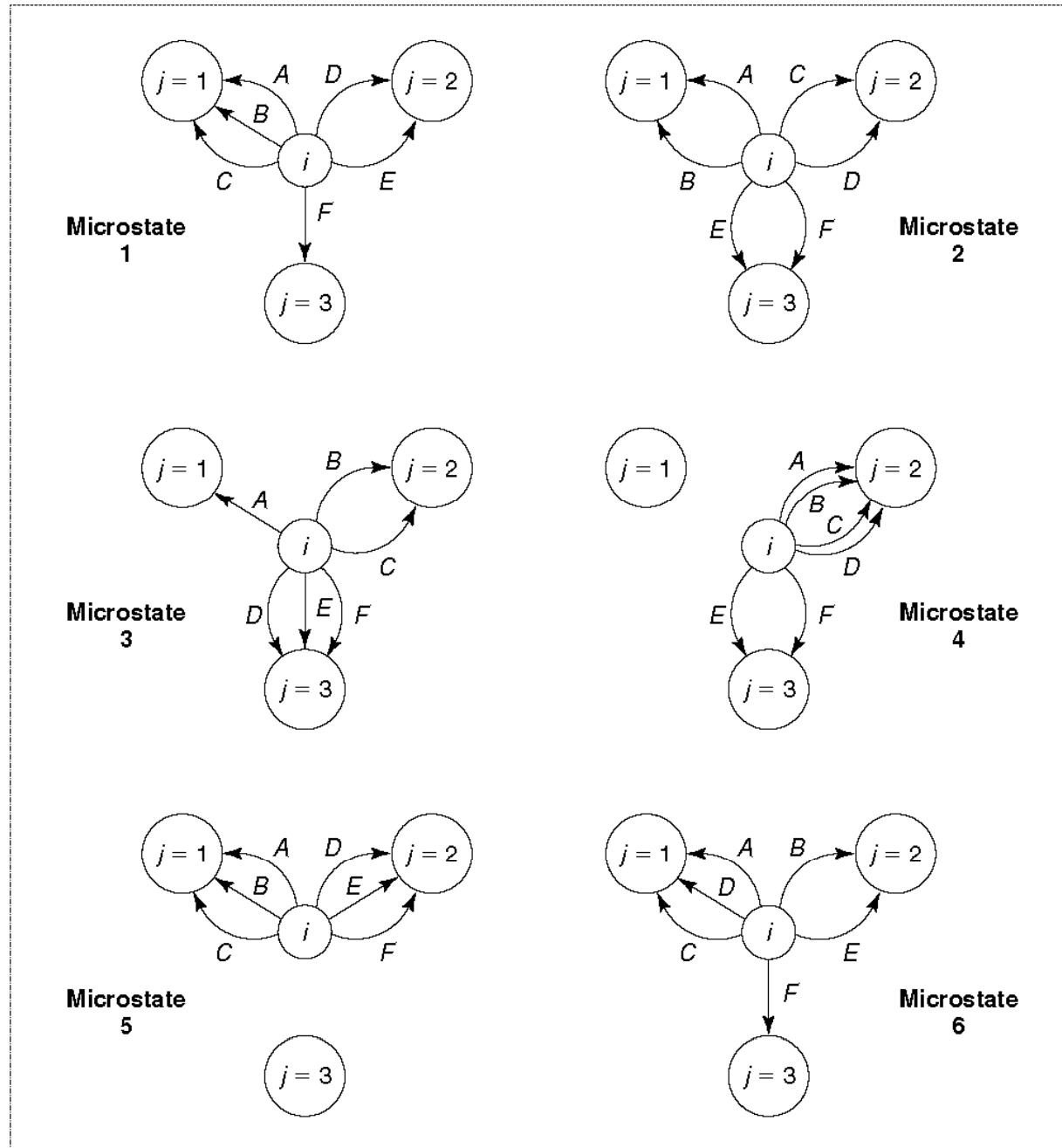
¹ All these nine values are to be multiplied by 10^{-4} . For example, 0.1187 is actually 0.1187×10^{-4} .

Table 3.15 Estimated inter-zonal travels in a doubly-constrained model

| From / to | $j = 1$ | $j = 2$ | $j = 3$ | V_i |
|-----------|---|------------------|------------------|--------|
| $i = 1$ | 1,563 (-15.2) ^{1} | 3,178 (+2.5) | 257 (+61.1) | 4,998 |
| $i = 2$ | 3,209 (+3.4) | 1,313 (-14.3) | 478 (+16.3) | 5,000 |
| $i = 3$ | 15,238 (+1.0) | 25,498 (+0.4) | 4,265 (-5.51) | 45,001 |
| V_j | 20,010 | 29,989 | 5,000 | 54,999 |

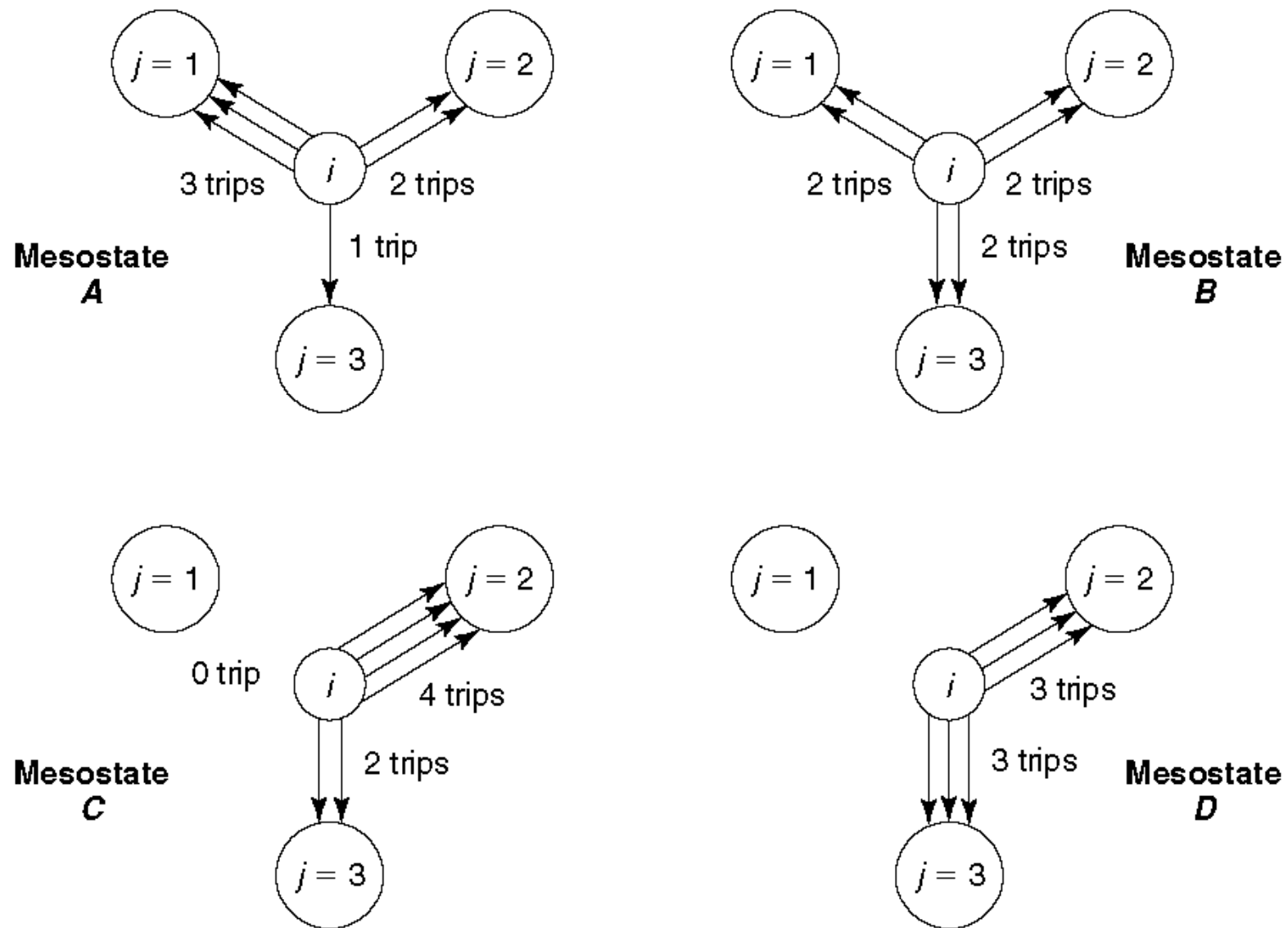
¹ Numbers in parenthesis indicate the percentage errors between observed and estimated inter-zonal travel.

Figure 3.17 SYSTEM MICROSTATES



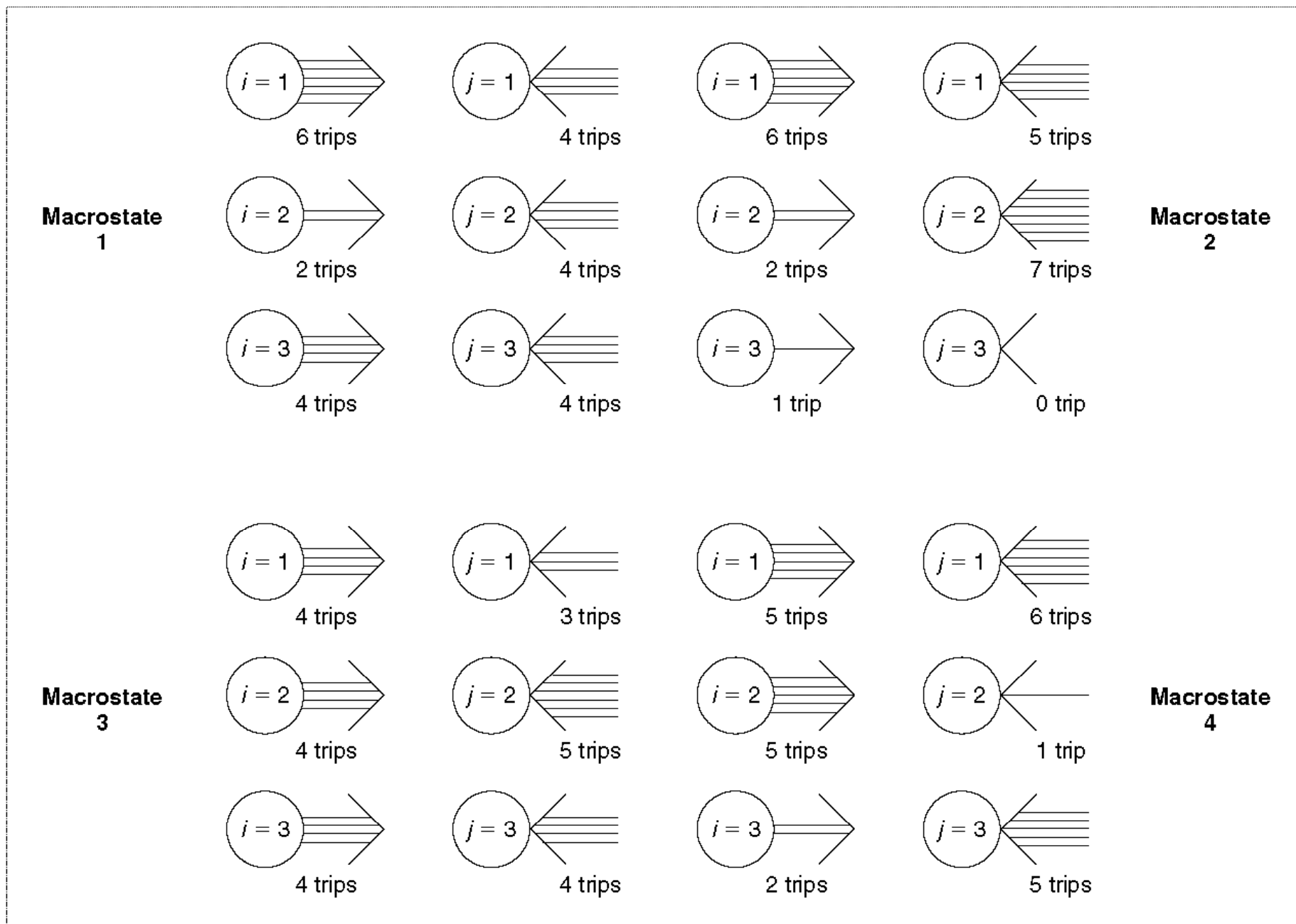
SOURCE: Putman (1978). Reprinted with permission.

Figure 3.19 SYSTEM MESOSTATES



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Figure 3.20 SYSTEM MACROSTATES



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